SGOOD: Substructure-enhanced Graph-Level Out-of-Distribution Detection

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ABSTRACT

Graph-level representation learning is important in a wide range of applications. Existing graph-level models are generally built on i.i.d. assumption for both training and testing graphs. However, in an open world, models can encounter out-of-distribution (OOD) testing graphs that are from different distributions unknown during training. A trustworthy model should be able to detect OOD graphs to avoid unreliable predictions, while producing accurate indistribution (ID) predictions. To achieve this, we present SGOOD, a novel graph-level OOD detection framework. We find that substructure differences commonly exist between ID and OOD graphs, and design SGOOD with a series of techniques to encode task-agnostic substructures for effective OOD detection. Specifically, we build a super graph of substructures for every graph, and develop a twolevel graph encoding pipeline that works on both original graphs and super graphs to obtain substructure-enhanced graph representations. We then devise substructure-preserving graph augmentation techniques to further capture more substructure semantics of ID graphs. Extensive experiments against 11 competitors on numerous graph datasets demonstrate the superiority of SGOOD, often surpassing existing methods by a significant margin. The code is available at [https://anonymous.4open.science/r/SGOOD-0958.](https://anonymous.4open.science/r/SGOOD-0958)

KEYWORDS

Out-of-distribution Detection, Trustworthy Model, Reliability, Graph Classification

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1 INTRODUCTION

Graphs are widely used to represent complex structured data, e.g., chemical compounds, proteins, and social networks. Graph-level representation learning, which extracts meaningful representations of these graphs, is crucial for applications in biochemistry [\[16,](#page-9-0) [29\]](#page-9-1) and social network analysis [\[7,](#page-9-2) [30\]](#page-9-3). Existing graph-level learning models are based on the closed-world assumption, in which testing graphs encountered at deployment are drawn i.i.d. from the same distribution as the training graph data. However, in reality, the models are actually in an open world, where test graphs can come from different, previously unseen distributions, making them out-of-distribution (OOD) w.r.t. in-distribution (ID) training graphs [\[20,](#page-9-4) [21,](#page-9-5) [38\]](#page-9-6). Consequently, the models trained solely by ID graphs tend to make incorrect predictions on OOD data [\[13\]](#page-9-7), which raises reliability concerns in safety-critical applications, e.g., drug discovery [\[1\]](#page-9-8). A trustworthy graph-level learning model should be capable of identifying OOD test graphs to avoid unreliable predictions.

While initial efforts have been made to explore graph-level OOD detection [\[10,](#page-9-9) [21,](#page-9-5) [24\]](#page-9-10), these methods primarily rely on messagepassing graph neural networks (GNNs) [\[12,](#page-9-11) [17\]](#page-9-12) to first get node representations and then generate graph-level representations solely based on these nodes. Substructure patterns, which are high-level graph structures and contain rich graph semantics [\[38,](#page-9-6) [44\]](#page-10-1), have yet to be leveraged for graph-level OOD detection. Intuitively, an OOD detector that can distinguish both node-level structures and substructure patterns would be more effective. However, leveraging substructures for OOD detection is challenging due to the absence of OOD graphs during training, making it difficult to determine in advance which substructure patterns should be learned for identifying OOD samples. Existing substructure learning methods, e.g., hierarchical GNNs [\[9,](#page-9-13) [18,](#page-9-14) [39\]](#page-9-15) and subgraph GNNs [\[42,](#page-10-2) [46\]](#page-10-3), typically learn task-specific substructures that are tailored to discriminate

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Table 1: The percentage of OOD graphs with substructures never appeared in ID graphs.

• • Graph embedding \bigcirc :Substructure

Figure 1: Substructure-enhanced graph-level OOD detection

between labeled classes in the training set. We argue that such taskspecific substructures are not sufficient for OOD detection. Instead, the detector should be able to learn a diverse set of substructure patterns from ID training graphs, including task-agnostic substructures not associated with specific classification tasks. As illustrated in Figure 1, the two ID graphs can be classified into different classes based on the presence of a task-specific triangle substructure (in blue). However, to identify the OOD graph, we need to compare its substructures to the task-agnostic ones such as the 6-node cycle (in green), to detect the irregular substructure (in orange). Therefore, effectively leveraging substructures for graph-level OOD detection requires considering task-agnostic information [\[32\]](#page-9-16), a capability lacking in existing OOD detection methods.

In this paper, we develop SGOOD, a novel framework that explicitly encodes task-agnostic substructures and their relationships into effective representations for graph-level OOD detection. The design of SGOOD is supported by empirical findings that demonstrate the crucial role of task-agnostic substructures in distinguishing between ID and OOD graphs. Given a dataset of graphs (see Table [2](#page-4-0) for data statistics), we apply community detection [\[3\]](#page-9-17) to extract task-agnostic substructures. The substructures are task-agnostic since the adopted community detection is independent of specific learning tasks. Then the percentage of OOD graphs with substructures that never appeared in ID graphs per dataset is reported in Table [1.](#page-1-0) Observe that such percentage values are high, more than 44% in 4 out of 6 datasets. The results validate that task-agnostic substructures can reveal differences between ID and OOD graphs. As illustrated in Figure [1,](#page-1-1) if a method can preserve the task-agnostic substructures of ID graphs into embeddings, OOD graphs with unseen substructures will have embeddings distant from those of ID graphs, making them easy to detect.

Therefore, we design a series of techniques in SGOOD to effectively encode task-agnostic substructures and generate substructureenhanced graph representations for graph-level OOD detection. Specifically, we first build a super graph G_i of substructures for every graph G_i to obtain task-agnostic substructures and their relationships. Then, a two-level graph encoding pipeline is designed to work on G_i and G_i in sequence to learn expressive substructureenhanced graph representations. We prove that SGOOD with the pipeline is strictly more expressive than 1&2-WL, which theoretically justifies the power of preserving substructure patterns for

OOD detection. Moreover, to capture more information about taskagnostic substructures in training ID graphs, we design substructurepreserving graph augmentation techniques, which utilize the super graph of substructures to ensure that the substructures in a graph are modified as a whole. At test time, given a graph G_i and its super graph G_i , our OOD detector obtains the graph-level representations of both, which are then used for OOD score estimation. Extensive experiments compare SGOOD with 11 baselines across 8 real-world graph datasets with various OOD types. SGOOD consistently outperforms existing methods, for example, achieving a 9.58% absolute improvement in AUROC over the runner-up baseline on the IMDB-M dataset. In summary, our contributions are:

- We present SGOOD, a leading method that highlights the importance of task-agnostic substructures and effectively leverages them to enhance graph-level OOD detection.
- We design a two-level graph encoding pipeline by leveraging a super graph of substructures, empowering SGOOD to learn graph representations enhanced with substructures.
- We further develop substructure-preserving graph augmentations via super graphs of substructures, to strengthen SGOOD's ability in distinguishing OOD graphs.
- Extensive experiments demonstrate the superiority of SGOOD for graph-level OOD detection, achieving significant improvements over existing methods across multiple datasets.

2 PRELIMINARIES

We consider graph-level classification, which aims to classify a collection of graphs into different classes. Let $G_i = (V_i, E_i)$ be a graph, where V_i and E_i are node set and edge set, respectively. Let $x_u \in \mathbb{R}^c$ denote the attribute vector of node $u \in V_i$ in graph G_i . Denote X as the in-distribution (ID) graph space and let $\mathcal{Y} = \{1, 2, ..., C\}$ be the label space. In graph-level classification, the training set $D_{tr}^{in} = \{ (G_i, y_i) \}_{i=1}^n$ is drawn i.i.d. from the joint data distribution P_X y. Every graph sample in D_{tr}^{in} contains a graph G_i with label y_i . Let f be a learning model trained by the training set D_{tr}^{in} , and f is deployed to predict the label of a testing graph.

Graph-level Out-Of-Distribution Detection. At test time, graphlevel OOD detection can be treated as a task to decide whether a testing graph G_i in testing set D_{test} is from the ID P_X or from other irrelevant distributions (i.e., OOD). A typical way for OOD detection is to develop an OOD detector by leveraging the representations generated from the classification model f that is trained via ID training graphs in D_{tr}^{in} . Specifically, the OOD detector has a scoring function $S(G_i)$ for every testing graph $G_i \in D_{test}$. Testing graphs with low scores $S(G_i)$ are regarded as ID, while the graphs with high scores are OOD. As stated in [\[26\]](#page-9-18), a score threshold λ is typically set so that a high fraction of ID data (e.g., 95%) is correctly classified.

3 THE SGOOD METHOD

Solution Overview. The main goal of SGOOD is to effectively encode task-agnostic substructures and their relationships into representations for graph-level OOD detection. As illustrated in Figure [2,](#page-2-0) SGOOD generates substructure-enhanced graph representations and further improves representation quality by substructurepreserving graph augmentations. Given a graph G_i , we first build

its super graph G_i of task-agnostic substructures, in which a super node represents a substructure in G_i and edges connect super nodes by following the substructure connectivity in graph G_i . A two-level graph encoding pipeline is designed over both G_i and G_i for learning graph-level representations that are enhanced by substructures. Furthermore, substructure-preserving graph augmentations are designed to preserve more information on task-agnostic substructures, making OOD graphs with unseen substructure patterns easier to detect. Specifically, given a graph G_i , we augment it by first performing dropping, sampling, and substitution on its super graph G_i and then mapping the changes to G_i accordingly. In this way, the substructures in G_i are modified as a whole. SGOOD is trained using a combination of classification loss \mathcal{L}_{CE} and contrastive loss \mathcal{L}_{CL} . In test time, given a test graph G_i , we first obtain graph-level representations of both G_i and its super graph G_i , concatenate and normalize the representations to compute the OOD score $S(G_i)$.

3.1 Substructure-Enhanced Graph Encoding

Given a graph G_i , we first describe how to get its super graph G_i of task-agnostic substructures, and then present a two-level graph encoding pipeline to generate substructure-enhanced graph representations.

As SGOOD utilizes task-agnostic substructures, we treat substructure detection as a pre-processing step, and it is not our focus on how to detect substructures. There exist off-the-shelf methods [\[4,](#page-9-19) [6\]](#page-9-20) to detect task-agnostic substructures. By default, we use modularity-based community detection [\[3\]](#page-9-17). We also test other subgraph detection methods and find that the modularity-based substructures are effective in SGOOD, as validated in Table [6.](#page-6-0)

Super Graph of Substructures. Let a substructure $q_{i,i}$ of graph G_i be a connected subgraph of G_i . Specifically, a subgraph $g_{i,j}$ = $(V_{i,j}, E_{i,j})$ is a substructure of $G_i = (V_i, E_i)$ iff $V_{i,j} \subseteq V_i$, $E_{i,j} \subseteq E_i$, and $g_{i,j}$ is connected. The substructures ${g_{i,j}}_{j=1}^{n_i}$ of a graph G_i
and $g_{i,j}$ is connected. The substructures ${g_{i,j}}_{j=1}^{n_i}$ of a graph G_i satisfy the following properties: (i) the node sets of substructures are non-overlapping, (ii) the union of the nodes in all substructures is the node set of G_i , and (iii) every substructure is a connected subgraph of G_i . Then we construct the super graph G_i by regarding every substructure $q_{i,j}$ as a super node in G_i , and connect super nodes by inserting edges via Definition [3.1.](#page-2-1) Super graph G_i is a higher-order view depicting the relationships between the substructures of a graph G. We also add self-loops in super graph \mathcal{G}_i .

Definition 3.1 (A Super Graph of Substructures). A super graph of substructures constructed from the input graph $G_i = (V_i, E_i)$ is denoted as $G_i = (V_i, \mathcal{E}_i)$, where every super node $g_{i,j}$ in node set $V_i = \{g_{i,j}\}_{j=1}^{n_i}$ represents a substructure of G_i , and every edge in \mathcal{E}_i connecting two super nodes, and the edge set $\mathcal{E}_i = \{ (g_{i,j}, g_{i,k}) | \exists u \in$ $V_{i,j} \wedge v \in V_{i,k}, (u, v) \in E_i$.

Two-level Graph Encoding. Given a graph G_i and its super graph \mathcal{G}_i , we present a two-level graph encoding pipeline, as shown in Figure [2.](#page-2-0) The idea is that, in addition to learning representations over G_i , we further utilize the super graph G_i to encode substructure information into graph representations, to better preserve distinguishable substructure patterns for effective OOD detection. The two-level graph encoding first adopts GNNs to learn node representations with initial features over graph G_i . For every node $v \in V_i$, its representation $\mathbf{h}_{v}^{(l+1)}$ at $(l+1)$ -layer is obtained by Eq. [\(1\)](#page-2-2). Different GNNs have different aggregation and combination functions $f_{\rm AGGR}$, $f_{\rm COMB}$. By default, we adopt Graph Isomorphism Network (GIN) [\[36\]](#page-9-21) as the backbone. The GIN for G_i has L_1 layers.

$$
\mathbf{h}_v^{(l+1)} = f_{\text{COMB}}^{(l+1)}(\mathbf{h}_v^{(l)}, f_{\text{AGGR}}^{(l+1)}(\mathbf{h}_u^{(l)}, u \in N_{G_i}(v))), \tag{1}
$$

where $\mathbf{h}_v^{(l)} \in \mathbb{R}^d$ is the intermediate representation of node v from the *l*-th layer GNNs with hidden dimension *d*, $f_{\rm AGGR}^{(l+1)}$ is the function that aggregates node features from v's neighborhood $N_{G_i}(v)$ in graph G_i , $f_{\text{COMB}}^{(l+1)}$ is the function that updates node v's representation
by combining the representations of its neighbors with its own. and initially $\mathbf{h}_v^{(0)} = \mathbf{x}_v$.

Next, we obtain the representations of substructures $g_{i,j}$ in G_i by leveraging the node representations above. As shown in Eq. [\(2\)](#page-2-3), given a node v, we first concatenate all representations $h_v^{(l)}$ for $l =$ 1, ..., L_1 using f_{CAT} to get \mathbf{h}_v that preserves multi-scale semantics. Then, for a substructure $q_{i,j}$ of graph G_i , we obtain the substructure representation $\mathbf{h}_{q_{i,j}}^{(0)}$ by integrating \mathbf{h}_v of all v in $q_{i,j}$ via DeepSet pooling $[43]$ f_{POOL} in Eq. [\(2\)](#page-2-3).

$$
\mathbf{h}_{g_{i,j}}^{(0)} = f_{\text{POOL}}(\{\mathbf{h}_v | v \in V_{i,j}\}), \mathbf{h}_v = f_{\text{CAT}}(\{\mathbf{h}_v^{(l)}\}_{l=1}^{L_1})
$$
(2)

Note that $\mathbf{h}_{q_{i,j}}^{(0)}$ only considers the nodes inside substructure $g_{i,j}$ and the original graph topology G_i . To further consider the relationships depicted in the super graph G_i of substructures, we regard $h_{q_{i,j}}^{(0)}$ as the initial features of super node $g_{i,j}$ in \mathcal{G}_i , and employ a L_2 -layer GIN over G_i to learn substructure-enhanced graph representations by Eq. [\(3\)](#page-2-4) and [\(4\)](#page-2-5).

$$
\mathbf{h}_{g_{i,j}}^{(l+1)} = f_{\text{COMB}}^{(l+1)}(\mathbf{h}_{g_{i,j}}^{(l)}, f_{\text{AGGR}}^{(l+1)}(\mathbf{h}_{g_{i,k}}^{(l)}, g_{i,k} \in N_{\mathcal{G}_i}(g_{i,j}))),\tag{3}
$$

where $N_{\mathcal{G}_i}(g_{i,j})$ is the neighbors of super node $g_{i,j}$ in \mathcal{G}_i .

Lastly, in Eq. [\(4\)](#page-2-5), we get the final representation $\mathbf{h}_{g_{i,j}}$ of every super node $g_{i,j}$ by concatenating the representation of $g_{i,j}$ in every layer of the L_2 -layer GIN, and obtain the graph representation \mathbf{h}_{G_i} by readout f_{OUT} that is sum pooling.

$$
\mathbf{h}_{\mathcal{G}_i} = f_{\text{OUT}}(\{\mathbf{h}_{g_{i,j}} | g_{i,j} \in \mathcal{V}_i\}), \mathbf{h}_{g_{i,j}} = f_{\text{CAT}}(\{\mathbf{h}_{g_{i,j}}^{(l)}\}_{l=0}^{L_2}) \tag{4}
$$

Remark that the representation $\mathbf{h}_{\mathcal{G}_i}$ of super graph \mathcal{G}_i of graph G_i is used to train the loss \mathcal{L}_{CE} for classification. Meanwhile, as explained shortly, for OOD detection during testing, we further consider another representation of graph G_i obtained by aggregating node representations. Existing studies, such as hierarchical pooling [\[9,](#page-9-13) [18,](#page-9-14) [39\]](#page-9-15) and subgraph GNNs [\[42,](#page-10-2) [46\]](#page-10-3), learn task-specific substructures for the graph classification task. On the other hand, we leverage task-agnostic substructures. We conduct experiments to demonstrate that our SGOOD is more effective than these methods for graph-level OOD detection.

3.2 Substructure-Preserving Augmentations

Intuitively, if more information about task-agnostic substructures in training ID graphs is preserved, it is easier to distinguish OOD graphs with unseen substructure patterns. To achieve this, we design substructure-preserving graph augmentations by leveraging the super graph G_i of graph G_i , to improve the performance further. However, it is challenging to achieve this. Substructures with subtle differences have different semantics. It is important to keep the substructures of a graph intact while performing augmentations. Common augmentation techniques like edge permutation and node dropping directly on graphs G_i may unexpectedly destroy meaningful substructures, and hamper OOD detection effectiveness.

To tackle the issue, we first perform augmentations on the super graph G_i by regarding substructures as atomic nodes, and then map the augmentations to the original graph G_i with modifications over substructures as a whole. Specifically, we propose three substructure-level graph augmentations below, namely substructure dropping (SD), super graph sampling (SG), and substructure substitution (SS). The default augmentation ratio is set to 0.3.

- Substructure Dropping (SD). Given a graph G_i with its super graph G_i , a fraction of super nodes in G_i (*i.e.*, the corresponding substructures in G_i) are discarded randomly. Remark that selected substructures are dropped as a whole.
- Super Graph Sampling (SG). In the super graph G_i , we start from a random node, sample a fixed-size subgraph in G_i , and drop the rest nodes and edges. The changes are mapped to G_i accordingly. Depth-first search is chosen as the sampling strategy [\[40\]](#page-9-22).
- Substructure Substitution (SS). Given a graph G_i in class c with super graph G_i of substructures, we randomly substitute a fraction of nodes in G_i (i.e., substructures in G_i) with other substructures from the graphs of the same class c . To avoid drastic semantic change of the whole graph, only super nodes with degree one (excluding self-loops) in G_i take part in the substitution.

3.3 Model Training and OOD Scoring

3.3.1 Two-stage model training. We adopt a cross-entropy loss \mathcal{L}_{CE} for classification. After getting representation \mathbf{h}_{Gi} for the super graph G_i of graph G_i , we apply a linear transformation to get prediction logits $\widehat{y_i}$, evaluated against the ground-truth class label y_i to get \mathcal{L}_{CE} by Eq. [\(5\)](#page-3-0) for a mini-batch of *B* training graphs.

$$
\mathcal{L}_{CE} = -\frac{1}{B} \sum_{i=1}^{B} \sum_{c=1}^{C} \mathbb{1}(y_i = c) \log(\hat{y}_{i,c})
$$
 (5)

Then we adopt the substructure-preserving graph augmentations in Section [3.2](#page-3-1) to get contrastive loss \mathcal{L}_{CL} . Specifically, given a mini-batch of *B* training graphs ${G_i}_{i=1}^B$ and their super graphs $\{\mathcal{G}_i\}_{i=1}^B$, we transform the super graphs to get $\widehat{\mathcal{G}}_{i,0} = \mathcal{T}_0(\mathcal{G}_i)$ and $\widehat{\mathcal{G}}_{i,1} = \mathcal{T}_1(\mathcal{G}_i)$, where \mathcal{T}_0 and \mathcal{T}_1 are two augmentations chosen among $A = \{I, SD, SG, SS\}$, where I indicates no augmentation. Graph G_i is transformed accordingly via \mathcal{T}_0 and \mathcal{T}_1 to obtain $\widehat{G}_{i,0}$

and $\widehat{G}_{i,1}$ respectively. Then, the representations $\mathbf{h}_{\widehat{G}_{i,0}}$ and $\mathbf{h}_{\widehat{G}_{i,1}}$ of the two augmented super graphs can be calculated by applying Eq.[\(1\)](#page-2-2)-[\(4\)](#page-2-5). We transform $\mathbf{h}_{\widehat{\mathcal{G}}_t}$ and $\mathbf{h}_{\widehat{\mathcal{G}}_t}$ by a shared projection head $\psi(\cdot)$, which is a 2-layer MLP, followed by l_2 -normalization, to obtain $\mathbf{u}_{\widehat{G}_{i,0}} = \psi(\mathbf{h}_{\widehat{G}_{i,0}})/||\psi(\mathbf{h}_{\widehat{G}_{i,0}})||$ and $\mathbf{u}_{\widehat{G}_{i,1}} = \psi(\mathbf{h}_{\widehat{G}_{i,1}})/||\psi(\mathbf{h}_{\widehat{G}_{i,1}})||$ respectively. We get \mathcal{L}_{CL} by

$$
\mathcal{L}_{CL} = \frac{1}{2B} \sum_{i=1}^{B} \sum_{a \in \{0,1\}} -\log \frac{\exp (\mathbf{u}_{\widehat{g}_{i,a}}^{\mathsf{T}} \mathbf{u}_{\widehat{g}_{i,1-a}}/\tau)}{\sum_{j=1}^{B} \mathbb{I} \left(j \neq i\right) \sum_{k \in \{0,1\}} \exp (\mathbf{u}_{\widehat{g}_{i,a}}^{\mathsf{T}} \mathbf{u}_{\widehat{g}_{j,1-k}}/\tau)},\tag{6}
$$

where τ is a temperature parameter.

The overall training loss is the combination of \mathcal{L}_{CE} and \mathcal{L}_{CL} , weighted by α :

$$
\mathcal{L} = \mathcal{L}_{CE} + \alpha \mathcal{L}_{CL}.
$$
 (7)

The training procedure of SGOOD consists of two stages. In the first pre-training stage, the parameters are solely updated by minimizing \mathcal{L}_{CI} for T_{PT} epochs. In the second stage, the parameters are fine-tuned under the combined overall loss $\mathcal L$ for T_{FT} epochs. This training procedure achieves better performance than directly training \mathcal{L} , as shown in Figure [4](#page-7-0) when pretraining T_{PT} is 0.

3.3.2 Graph-level OOD scoring. Recall that the main goal of SGOOD is to let the representations of ID data and OOD data to be distant from each other. Given a testing graph $G_i \in D_{test}$, we use the standard Mahalanobis distance [\[19\]](#page-9-23) to quantify its OOD score. If G_i is with large Mahalanobis distance from the ID training data, it tends to be OOD.

As shown in Figure [2,](#page-2-0) in addition to the representation $\mathbf{h}_{\mathcal{G}_i}$ of the super graph G_i of a testing graph G_i , SGOOD also aggregates the node representations of G_i to get $\mathbf{h}_{G_i} = f_{\text{OUT}}(\{\mathbf{h}_v | v \in V_i\})$. Representations $\mathbf{h}_{\mathcal{G}_i}$ and \mathbf{h}_{G_i} are concatenated together to estimate the OOD score $S(G_i)$:

$$
S(G_i) = \max_{c \in [C]} (\mathbf{z}_i - \boldsymbol{\mu}_c)^\top \widehat{\Sigma}^{-1} (\mathbf{z}_i - \boldsymbol{\mu}_c), \mathbf{z}_i = \frac{f_{\text{CAT}}(\mathbf{h}_{G_i}, \mathbf{h}_{G_i})}{||f_{\text{CAT}}(\mathbf{h}_{G_i}, \mathbf{h}_{G_i})||_2}, \quad (8)
$$

where $[C] = \{1, \ldots, C\}$, μ_c and $\widehat{\Sigma}$ are the class centroid for class c and covariance matrix of training ID graphs, respectively.

3.4 Theoretical Analysis

We analyze the expressive power of SGOOD (using message-passing GNNs as the backbone) in comparison to 1&2-WL, a key tool for evaluating the expressivity of GNNs [\[36\]](#page-9-21). In Proposition [3.2,](#page-3-2) we demonstrate that SGOOD is more expressive than 1&2-WL, enabling it to distinguish structural patterns beyond the capability of 1&2-WL, and consequently, message-passing GNNs. The analysis, together with our empirical findings in Section [1,](#page-0-0) explains the power of SGOOD for graph-level OOD detection.

Proposition 3.2. When the GNNs adopted in SGOOD are with sufficient number of layers, and the f_{POOL} function in Eq.[\(2\)](#page-2-3) and f_{OUT} function in Eq.[\(4\)](#page-2-5) are injective, then SGOOD is strictly more expressive than 1&2-WL.

PROOF. We first prove that SGOOD is at least as powerful as 1&2-WL in Lemma [3.3.](#page-4-1) Then, we prove that SGOOD can distinguish 2-regular graphs that 1&2-WL cannot distinguish in Lemma [3.5.](#page-4-2) SGOOD: Substructure-enhanced Graph-Level Out-of-Distribution Detection CIKM '24, October 21 - 25, 2024, Boise, Idaho, USA

Combining these two Lemmas, we prove that SGOOD is strictly more expressive than $1&82-WL$. □

Lemma 3.3. For graphs $G_1 = (V_1, E_1)$ and $G_2 = (V_2, E_2)$ identified as non-isomorphic by 1&2-WL, SGOOD projects them into different representations $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ in Eq. [\(4\)](#page-2-5).

Proof. Let $\mathcal{H}_1^G = \{ \mathbf{h}_v | v \in V_1 \}$ and $\mathcal{H}_2^G = \{ \mathbf{h}_v | v \in V_2 \}$ be the multisets of node representations of G_1 and G_2 generated by GIN in Eq. [\(2\)](#page-2-3), respectively. Let $G_1 = (\mathcal{V}_1, \mathcal{E}_1)$ and $G_2 = (\mathcal{V}_2, \mathcal{E}_2)$ be the super graphs of G_1 and G_2 respectively. We consider two cases: (1) $|\mathcal{V}_1| \neq |\mathcal{V}_2|$, (2) $|\mathcal{V}_1| = |\mathcal{V}_2|$.

For case (1), G_1 and G_2 are two graphs with different number of nodes. Thus, G_1 and G_2 can be easily determined as non-isomorphic by 1&2-WL. It is proved that GIN with sufficient number of layers and all injective functions is as powerful as 1&2-WL [\[36\]](#page-9-21). As GIN is adopted in SGOOD as GNN backbone with sufficient number of layers and f_{OUT} function in Eq.[\(4\)](#page-2-5) is injective, representations \mathbf{h}_{G_1} and $\overline{\mathbf{h}_{\mathcal{G}_2}}$ generated by SGOOD are different.

For case (2), let
$$
|V_1| = |V_2| = K
$$
, $\mathcal{H}_1^{\mathcal{G}} = {\mathbf{h}_{g_{1,j}}^{(0)}} | g_{1,j} \in V_1$ and

 $\mathcal{H}_2^{\mathcal{G}} = \{\mathbf{h}_{q_2,i}^{(0)} | g_{2,i} \in V_2\}$ be the multisets of initial node representations of \mathcal{G}_1 and \mathcal{G}_2 calculated by Eq.[\(2\)](#page-2-3), respectively. Using GIN with sufficient number of layers, we get $\mathcal{H}_1^G \neq \mathcal{H}_2^G$ [\[36\]](#page-9-21). As stated in Section [3.1,](#page-2-6) the substructures ${g_{i,j}}\}_{j=1}^{n_i}$ of a graph G_i satisfy the following properties: (i) the substructures are non-overlapping, (ii) the union of nodes in all substructures is the node set of G_i . Thus, {{h_v|v ∈ g_{1,j}}}^K₁ (resp. {{h_v|v ∈ g_{2,j}}}^K_{j=1}) is a partition of \mathcal{H}_1^G (resp. \mathcal{H}_2^G). Then, we have {{h_v|v ∈ g_{1,j}}}^K_{j=1} ≠ {{h_v|v ∈ g_{2,j}}}^K_{j=1}. As f_{POOL} function in Eq.[\(2\)](#page-2-3) is injective, we have $\{f_{\text{POOL}}(\{\mathbf{h}_v | v \in \mathbb{R}\})\}$ $g_{1,j}$ }) $\}_{j=1}^K$ \neq { $f_{\text{POOL}}(\{\mathbf{h}_v | v \in g_{2,j}\})\}_{j=1}^K$, that is $\mathcal{H}_1^{\mathcal{G}} \neq \mathcal{H}_2^{\mathcal{G}}$. As GIN and f_{OUT} function in Eq.[\(4\)](#page-2-5) are both injective, we derive that $\textbf{h}_{\mathcal{G}_1}$ and $\textbf{h}_{\mathcal{G}_2}$ generated on $\mathcal{H}^{\mathcal{G}}_1$ and $\mathcal{H}^{\mathcal{G}}_2$ are different.

Combining cases (1) and (2), we prove Lemma [3.3.](#page-4-1) \square

Next, we prove that SGOOD can distinguish n -node 2-regular graphs that 1&2-WL cannot distinguish in Lemma [3.5.](#page-4-2) Before that, we first give the definition of 2-regular graphs. Note that we only consider undirected graphs in this paper.

Definition 3.4 (2-regular graph). A graph is said to be regular of degree 2 if all local degrees are 2.

Lemma 3.5. Given two non-isomorphic n-node 2-regular graphs G_1 and G_2 that 1&2-WL cannot distinguish, SGOOD projects them into different graph representations $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ in Eq. [\(4\)](#page-2-5).

PROOF. Based on the definition of a 2-regular graph, we can say that G_1 and G_2 consist of one or more disconnected cycles. Let r_1 and r_2 be the number of cycles in G_1 and G_2 . Let $\mathcal{G}_1 = (\mathcal{V}_1, \mathcal{E}_1)$ and $\mathcal{G}_2 = (\mathcal{V}_2, \mathcal{E}_2)$ be the constructed super graphs of G_1 and G_2 . We consider two cases: (1) $r_1 \neq 1 \land r_2 \neq 1$, (2) $(r_1 = 1 \land r_2 \neq 1) \lor (r_1 \neq$ $1 \wedge r_2 = 1$.

For case (1), G_1 and G_2 consist of disconnected circles. As G_1 and G_2 are constructed by modularity-based community detection method [\[3\]](#page-9-17), in Lemma 3.4 of [\[2\]](#page-9-24), for graphs of disconnected circles, there is always a clustering with maximum modularity, in which each cluster consists of a connected subgraph. As a result, $\forall g_{1,j} \in$ \mathcal{V}_1 is a circle in G_1 , and $|\mathcal{V}_1| = r_1$. Similarly, $\forall g_{2,i} \in \mathcal{V}_2$ is a circle

Table 2: Data Statistics.

Dataset	OOD Type					# Class # ID Train # ID Val # ID Test # OOD Test
ENZYMES [27]	Unseen Classes	6	480	60	60	60
IMDB-M [27]	Unseen Classes	3	1200	150	150	150
$IMDB-B [27]$	Unseen Classes	2	800	100	100	100
REDDIT-12K [37] Unseen Classes		11	6997	875	875	875
BACE [35]	Scaffold	2	968	121	121	121
BBBP [35]	Scaffold	2	1303	164	164	164
DrugOOD [15]	Protein Target	2	800	100	100	100
HIV [35]	Scaffold	2	26319	3291	3291	3291

in G_2 , and $|\mathcal{V}_2| = r_2$. Let $\mathcal{N}_1 = {\left\{|V_{1,j}|\right\}}_{j=1}^{|\mathcal{V}_1|}$ and $\mathcal{N}_2 = {\left\{|V_{2,j}|\right\}}_{j=1}^{|\mathcal{V}_2|}$. Since G_1 and G_2 are non-isomorphic, we have $\exists n_{1,i} \in \mathcal{N}_1 : \forall n_{2,i} \in$ $N_2, n_{1,j} \neq n_{2,j}$. As a result, we have $N_1 \neq N_2$. Then, we have $\{\{\mathbf{h}_v|v \in V_{1,j}\}\}_{j=1}^{|\mathcal{V}_1|} \neq \{\{\mathbf{h}_v|v \in V_{2,j}\}\}_{j=1}^{|\mathcal{V}_2|}$. As froot function in Eq.[\(2\)](#page-2-3) is injective, we have $\mathcal{H}_1^{\mathcal{G}} = \{f_{\text{POOL}}(\{h_v | v \in g_{1,j}\})\}_{j=1}^{|\mathcal{V}_1|}$, $\mathcal{H}_2^{\mathcal{G}} = \{f_{\text{POOL}}(\{\mathbf{h}_v | v \in g_{2,j}\})\}_{j=1}^{|\mathcal{V}_2|}$, and $\mathcal{H}_1^{\mathcal{G}} \neq \mathcal{H}_2^{\mathcal{G}}$. As shown in the proof of Lemma [3.3,](#page-4-1) we have $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ generated on $\mathcal{H}^{\mathcal{G}}_1$ and $\mathcal{H}_2^{\mathcal{G}}$ are different.

For case (2), we consider $r_1 = 1 \wedge r_2 \neq 1$, and the proof when $r_2 =$ $1 \wedge r_1 \neq 1$ is similar. G_1 consists of one single circle, and G_2 consists of r_2 disconnected circles. For G_2 and \mathcal{G}_2 , $\forall g_{2,j} \in \mathcal{V}_2$ is a circle in G_2 , and $|\mathcal{V}_2| = r_2$ following the conclusion in case (1). For G_1 and G_1 , we consider two cases: (i) $|V_1| = r_1 = 1$, and (ii) $|V_1| > 1$. For case (i), $V_1 = \{g_{1,1}\}\$, where $g_{1,1} = G_1$. Let $\mathcal{N}_1 = \{|V_{1,j}|\}_{j=1}^{|\mathcal{V}_1|} = \{|V_{1,1}|\}$ and $\mathcal{N}_2 = \{ |V_{2,j}| \}_{j=1}^{|\mathcal{V}_2|}$. As $|\mathcal{N}_1| \neq |\mathcal{N}_2|$, we have $\mathcal{N}_1 \neq \mathcal{N}_2$. Similar to case (1), we conclude that graph representations $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ generated on $\mathcal{H}_1^{\mathcal{G}}$ and $\mathcal{H}_2^{\mathcal{G}}$ are different. For case (ii), $\mathcal{V}_1 = \{g_{1,j}\}_{j=1}^{|\mathcal{V}_1|}$, where $∀g_{1,j} ∈ V_1$ is a chain and two nearby chain are connected in G_1 . In other words, G_1 is a $|V_1|$ -circle while G_2 consists of $|V_2|$ isolated nodes. Thus, G_1 and G_2 can be distinguished as non-isomorphic by 1&2-WL. By [\[36\]](#page-9-21), when we encode G_1 and G_2 by Eq. [\(3\)](#page-2-4) with sufficient layers of GIN, and generate $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ by Eq. [\(4\)](#page-2-5), where f_{OUT} is injective, $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ are different. Combining cases (i) and (ii), we prove SGOOD generates different $\mathbf{h}_{\mathcal{G}_1}$ and $\mathbf{h}_{\mathcal{G}_2}$ for G_1 and G_2 in case (2).

Combining cases (1) and (2), we prove Lemma [3.5.](#page-4-2) \square

4 EXPERIMENTS

We evaluate SGOOD in graph-level OOD detection against 11 baseline methods across 8 real-world datasets.

4.1 Experimental Setup

4.1.1 Datasets. We adopt real-world datasets that encompass diverse types of OOD graphs, as listed in Table [2.](#page-4-0) These datasets are curated from mainstream graph classification benchmarks [\[15,](#page-9-28) [27,](#page-9-25) [35\]](#page-9-27) into OOD detection scenarios. The OOD graph data is generated following [\[21,](#page-9-5) [24\]](#page-9-10). All ID graphs are randomly split into training, validation, and testing with ratio 8:1:1, following the settings of standard graph classification [\[14,](#page-9-29) [27\]](#page-9-25). The testing set consists of the same number of ID graphs and OOD graphs.

Table 3: Overall OOD detection performance by AUROC, AUPR, and FPR95 in percentage % (mean ± std). ↑ indicates larger values are better and vice versa. Bold: best. Underline: runner-up.

		ENZYMES			IMDB-M		IMDB-B			REDDIT-12K	
Method	AUROCT AUPRT			FPR95. AUROCT AUPRT FPR95. AUROCT AUPRT				FPR95.	AUROCT AUPRT		FPR95.
MSP				$61.34\text{+}3.79$ $61.65\text{+}6.64$ $89.67\text{+}2.26$ $42.75\text{+}1.52$ $51.04\text{+}1.93$ $95.73\text{+}1.63$ $58.13\text{+}2.31$ $59.63\text{+}1.22$ $91.40\text{+}4.16$ $50.63\text{+}0.87$ $48.60\text{+}1.08$ $95.95\text{+}1.25$							
Energy				54.69±9.18 56.90±8.85 89.33±3.55 24.50±19.73 37.26±11.78 96.40±2.25 49.58±17.76 59.03±13.06 92.80±3.55 55.10±0.48 56.52±0.78 97.19±0.58							
ODIN				$63.70_{\pm2.70}$ $65.72_{\pm4.77}$ $92.66_{\pm3.26}$ $40.12_{\pm2.96}$ $50.08_{\pm2.44}$ $96.66_{\pm1.03}$ $58.25_{\pm2.94}$ $61.36_{\pm0.49}$ $92.20_{\pm2.92}$ $51.74_{\pm2.03}$ $54.53_{\pm1.26}$ $96.45_{\pm0.73}$							
MAH				$67.37\scriptstyle\pm 3.67$ $63.81\scriptstyle\pm 2.15$ $83.33\scriptstyle\pm 9.60$ $69.26\scriptstyle\pm 3.67$ $63.64\scriptstyle\pm 2.14$ $60.93\scriptstyle\pm 9.06$ $76.77\scriptstyle\pm 4.37$ $76.88\scriptstyle\pm 6.30$ $81.40\scriptstyle\pm 7.14$ $72.68\scriptstyle\pm 0.87$ $74.47\scriptstyle\pm 0.48$ $80.75\scriptstyle\pm 2.05$							
GNNSafe 56.85±8.91 56.13±8.26 97.00±3.71 21.93±1.76 36.88±1.68 95.46±1.42 70.49±14.80 75.67±15.71 87.80±5.81 51.68±0.08 53.97±0.52 95.59±2.80											
GraphDE $61.35\scriptstyle{\pm 3.99}$ $66.26\scriptstyle{\pm 2.98}$ 99.00 $\scriptstyle{\pm 0.81}$ 66.87 $\scriptstyle{\pm 4.25}$ 62.60 $\scriptstyle{\pm 4.47}$ 93.06 $\scriptstyle{\pm 8.24}$ 26.91 $\scriptstyle{\pm 3.35}$ 42.73 $\scriptstyle{\pm 2.06}$ 100.00 $\scriptstyle{\pm 0.00}$ 59.40 $\scriptstyle{\pm 0.81}$ 83.06 $\scriptstyle{\pm 0.30}$ 81.											
GOOD-D 67.21±6.41 64.86±6.32 82.33±8.31 61.89±4.87 66.91±7.60 95.20±4.55 52.58±10.21 55.69±10.56 99.20±1.00 56.11±0.10 59.56±0.16 93.67±0.34											
AAGOD				65.02±4.41 82.78±2.83 70.76±5.48 68.15±4.45 81.56±22.32 72.51±1.11 67.86±4.79 86.33±4.03 60.25±2.16 61.44±1.61 92.53±1.55							
				OCGIN 68.11±4.61 68.90±4.19 89.67±3.70 47.51±9.47 50.76±4.53 98.27±17.70 60.78±5.21 57.80±5.10 8780±9.15 59.33±1.26 60.02±1.88 90.00±2.01							
GLocalKD 71.46±3.21 64.93±4.44 78.67±6.37 19.82±1.57 35.39±0.49 98.27±1.13 79.39±4.71 85.56±3.33 87.40±5.42 49.60±1.06 51.75±0.72 97.60±0.35											
OGGTL				73.22+1.83 73.61+3.19 82.33+2.70 54.07+12.93 58.20+7.86 86.40+6.49 37.39+18.82 47.11+14.06 98.80+2.40 51.62+0.019 53.33+0.01 96.79+0.06							
											SGOOD 74.40±1.42 72.53±2.51 73.66±7.03 78.84±2.00 72.54±3.21 45.46±6.62 80.41±3.16 83.49±3.59 81.20±2.28 74.95±0.79 74.93±0.93 75.17±2.72
		BACE			BBBP		DrugOOD			HIV	
Method	AUROCT	AUPR ₁		FPR95. AUROCT AUPRT		FPR95. AUROCT AUPRT			FPR95 AUROCT	AUPR ¹	FPR95 .
MSP				$46.34_{\pm6.10}$ $48.65_{\pm3.08}$ $97.02_{\pm2.18}$ $57.37_{\pm4.28}$ $56.84_{\pm3.36}$ $94.63_{\pm2.26}$ $52.86_{\pm5.26}$ $54.49_{\pm4.33}$ $98.80_{\pm0.01}$ $50.75_{\pm1.88}$ $50.49_{\pm0.91}$ $95.52_{\pm0.50}$							
Energy			$46.05 \scriptstyle{\pm 6.66}$ 49.68 $\scriptstyle{\pm 4.16}$ 97.36 $\scriptstyle{\pm 2.92}$					$56.56_{\pm 4.16}$ $55.74_{\pm 2.78}$ $92.68_{\pm 2.62}$ $52.81_{\pm 5.36}$ $54.98_{\pm 4.36}$ $98.20_{\pm 1.16}$ $50.97_{\pm 2.13}$ $50.49_{\pm 0.91}$ $95.50_{\pm 0.59}$			
ODIN		$45.51 \scriptstyle{\pm 3.85}$ $48.28 \scriptstyle{\pm 3.76}$ 97.02 $\scriptstyle{\pm 1.53}$				$54.78_{\pm3.46}$ $54.63_{\pm3.69}$ $96.34_{\pm1.80}$ $51.09_{\pm3.79}$ $52.70_{\pm2.66}$ $99.00_{\pm1.09}$				50.16±0.73 49.95±0.58 94.60±1.07	
MAH			73.78±1.97 75.33±2.32 86.78±6.32					$53.77_{\pm{4.27}}$ $52.57_{\pm{3.81}}$ $93.29_{\pm{2.51}}$ 66.90 $_{\pm{4.14}}$ 64.30 $_{\pm{4.43}}$ 81.60 $_{\pm{4.58}}$	58.10±3.60 57.18±3.18 91.89±1.32		
GNNSafe 47.61±7.50 51.52±5.91 98.18±2.05						$47.04_{\pm2.40}$ 51.52 \pm 5.90 98.41 \pm 0.99 50.44 \pm 0.57 51.14 \pm 0.30 96.01 \pm 0.33					$50.98 \scriptstyle{\pm 6.82}$ 55.13 $\scriptstyle{\pm 6.81}$ 96.01 $\scriptstyle{\pm 0.33}$
GraphDE 47.32±1.52 51.1±2.57 94.21±4.58						$50.88_{\pm 2.78}$ $51.47_{\pm 3.84}$ $94.63_{\pm 2.34}$ 60.19 $_{\pm 4.32}$ 62.59 $_{\pm 2.47}$ 88.80 $_{\pm 5.60}$			52.38±1.86 54.14±3.21 94.89±0.84		
GOOD-D 70.42±2.22 73.21±3.34 88.26±1.78						$54.15\text{+}1.10$ $58.58\text{+}1.93$ $99.39\text{+}0.41$ $60.52\text{+}3.33$ $63.09\text{+}2.54$ $98.40\text{+}1.27$				$59.69_{\pm0.62}$ 57.10 \pm .14 92.03 \pm 0.61	
AAGOD	71.41±2.37 71.82±1.72 90.63±1.95							$58.16\text{+}1.54$ $59.35\text{+}1.32$ $93.5\text{+}0.76$ $60.29\text{+}3.23$ $66.2\text{+}3.36$ $95.33\text{+}0.47$ $55.72\text{+}0.69$ $54.29\text{+}0.51$ $92.2\text{+}0.3$			
	OCGIN 59.71±5.20 61.43±5.18 93.39±4.44							$47.78_{\pm 5.72}$ $47.27_{\pm 2.98}$ $94.76_{\pm 2.70}$ $57.95_{\pm 5.80}$ $59.50_{\pm 7.00}$ $94.20_{\pm 3.12}$ $54.06_{\pm 0.47}$ $52.14_{\pm 0.26}$ $92.81_{\pm 1.01}$			
GLocalKD $45.34_{\pm2.11}$ $55.39_{\pm2.35}$ $98.68_{\pm1.11}$								$43.77_{\pm 2.23}$ $45.84_{\pm 1.20}$ $98.29_{\pm 1.00}$ $45.72_{\pm 0.97}$ $50.90_{\pm 3.33}$ $100.00_{\pm 0.00}$ $46.81_{\pm 2.90}$ $46.95_{\pm 2.01}$ $97.05_{\pm 0.19}$			
OGGTL	80.84±2.00 79.93±1.26 66.44±8.89							58.73±2.19 60.47±1.38 91.46±2.21 67.59±7.93 70.90±5.80 83.00±11.22 51.78±0.19 53.71±0.22 96.41±0.05			

- ENZYMES comprises protein networks representing enzymes. 'Non-enzymes' protein networks from the PROTEINS dataset [\[27\]](#page-9-25) are introduced as OOD.
- IMDB-M includes social networks categorized into three classes. We designate social networks from the IMDB-B dataset [\[27\]](#page-9-25), labeled with 'Action', as OOD graphs, noting that the 'Action' class is absent in IMDB-M.
- IMDB-B regards graphs labeled as 'Comedy' and 'Sci-Fi' in IMDB-M as OOD graphs, as these classes are absent in IMDB-B.
- REDDIT-12K is a large-scale social network dataset [\[37\]](#page-9-26). Graphs in the dataset REDDIT-BINARY [\[37\]](#page-9-26), which are social networks with classes different from REDDIT-12K, are introduced as OOD.
- BACE consists of molecules for property prediction. In our adaptation for OOD detection, we use the training set of the original BACE as ID graphs. OOD graphs are introduced by incorporating graphs from the provided test set, wherein molecules exhibit scaffolds distinct from those present in training set.
- BBBP is constructed similarly to BACE. OOD graphs have molecular scaffolds different from ID graphs.
- DrugOOD is a curated OOD dataset consisting of various molecular graphs. We use the provided curator to generate both ID and OOD graphs that have different protein targets.
- HIV is a large-scale molecular graph dataset [\[35\]](#page-9-27). Graphs with scaffolds different from ID graphs are regarded as OOD.
- 4.1.2 Baselines. We compare with 11 competitors in 3 categories.
- General OOD detection methods, including MSP [\[13\]](#page-9-7), Energy [\[23\]](#page-9-30), ODIN [\[22\]](#page-9-31), and MAH [\[19\]](#page-9-23). MSP, Energy, and ODIN estimate OOD scores directly from classification logits at test time. MSP uses the maximum softmax score as OOD score while Energy uses energy function. ODIN combines temperature scaling with gradient-based input perturbations to enlarge the differences between OOD and ID samples. MAH measures Mahalanobis distance between test samples and ID training data.
- Graph-level OOD detection methods, including GNNSafe [\[33\]](#page-9-32), GraphDE [\[21\]](#page-9-5), GOOD-D [\[24\]](#page-9-10) and AAGOD [\[10\]](#page-9-9). GNNSafe incorporates GNNs in the energy model and detects OOD samples using energy scores. In our paper, we use graph labels to directly run the basic version of GNNSafe from its Section 3.1 [\[33\]](#page-9-32). GraphDE is a probabilistic model-based approach developed for debiased learning and OOD detection in graph data. GOOD-D is an unsupervised OOD detection method that adopts contrastive learning to capture latent patterns of ID graphs. AAGOD is a post-hoc framework that adopts an adaptive amplifier to enlarge the gap between OOD and ID graphs.
- Graph-level anomaly detection methods, including OCGIN [\[45\]](#page-10-5), OCGTL [\[28\]](#page-9-33), and GLocalKD [\[25\]](#page-9-34). OCGIN combines deep one-class classification with GIN [\[36\]](#page-9-21) to detect outlier graphs at test time. OCGTL develops a one-class objective for graph anomaly detection. GLocalKD leverages knowledge distillation to detect both local and global graph anomalies.

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Table 4: ID graph classification performance measured by average ID ACC (in percentage %). / indicates that ID ACC is not applicable for unsupervised methods.

Method				ENZYMES IMDB-M IMDB-B REDDIT-12K BACE BBBP HIV		DrugOOD
MSP	37.33	48.27	69.80	48.91	80.83 87.44 96.62	79.20
Energy	37.33	48.27	69.80	48.91	80.83 87.44 96.62	79.20
ODIN	37.33	48.27	69.80	48.91	80.83 87.44 96.62	79.20
MAH	37.33	48.27	69.80	48.91	80.83 87.44 96.62	79.20
GNNSafe	17.66	30.13	50.20	27.42	56.69 79.14 96.58	64.40
GraphDE	46.00	37.86	69.80	40.68	77.68 88.90 96.20	77.00
GOOD-D						
AAGOD						
SGOOD	48.66	48.66	71.60	51.82	80.33 89.14 96.66	79.40

4.1.3 Evaluation and Implementation. Following [\[24,](#page-9-10) [33\]](#page-9-32), all methods are trained using ID training set and evaluated their OOD detection performance and ID classification performance in the test set. Hyperparameters are tuned using ID graphs from the validation set. All methods are evaluated five times on each dataset, and the reported performance metrics are based on the mean and standard deviation results on the test set. We use three commonly used metrics AUROC, AUPR and FPR95 for OOD detection evaluation [\[13,](#page-9-7) [33\]](#page-9-32). For the classification performance in ID graphs, we use Accuracy (ID ACC). Remark that the priority of the graph-level OOD detection task is to accurately identify OOD graphs, instead of improving the ID ACC. For SGOOD, we set the number of layers $L_1 = 3$ and $L_2 = 2$, and dimension d as 16. We set batch size 128. Training consists of 100 epochs for pre-training (T_{PT}) and 500 epochs for fine-tuning (T_{FT}) . We experiment with learning rates in the range {0.01, 0.001, 0.0001} for the initial stage, and set the learning rate to 0.001 and α to 0.1 for the refinement stage. For all baselines, we use the suggested parameters from their papers or obtained by grid search. Experiments are conducted on a Linux server equipped with an Nvidia RTX 3090 GPU card.

4.2 Overall Performance

OOD detection performance. Table [3](#page-5-0) reports the overall graphlevel OOD detection performance of all methods by AUROC, AUPR and FPR95 metrics on all datasets, by mean and standard deviation values. Observe that SGOOD consistently achieves superior OOD detection effectiveness under most settings. For instance, on IMDB-M, SGOOD has AUROC 78.84%, which indicates 9.58% absolute improvement over the best competitor with AUROC 69.26%. As another example on BACE molecule dataset, the AUROC of SGOOD is 84.39%, while the runner-up achieves AUROC 80.84%. The overall results in Table [3](#page-5-0) show that SGOOD effectively encode task-agnostic substructures into expressive representations for graph-level OOD detection, validating the power of our technical designs.

ID graph classification performance. Table [4](#page-6-1) reports the performanc on ID graph classification of all methods by Accuracy (ID ACC). The results of graph-level anomaly detection methods are not reported as ID ACC is not applicable. SGOOD achieves the best ID ACC on 7 out of 8 datasets. For instance, on ENZYMES, SGOOD has ID ACC 48.66%, while the ID ACC of the best competitor GraphDE is 46.00%, indicating a relative improvement of 5.8%. On REDDIT-12K, a large-scale dataset with 11 ID classes, SGOOD has ID ACC

Table 5: Ablation AUROC (%)

Figure 3: ID and OOD score distributions, with the dotted line indicating the mean of ID/OOD scores.

Table 6: Comparison between different substructure detection methods by AUROC (%).

SGOOD						ENZYMES IMDB-M IMDB-B BACE BBBP DrugOOD
w.o. substructures	67.38	69.26	76.8	73.78 53.77		66.90
Modularity	74.41	78.84	80.42	84.40 61.25		73.16
Graclus	71.12	74.64	78.86		79.54 56.62	67.94
LP.	68.09	75.48	78.46		76.63 54.90	68.95
BRICS				78.39	60.18	64.78

51.82%, outperforming the best competitor by a relative improvement of 5.9%. The results indicate that leveraging substructures benefits both OOD detection and graph classification.

4.3 Model Analysis

Ablation Study. In Table [5,](#page-6-2) SGOOD\A is SGOOD that ablates all augmentations in Section [3.2,](#page-3-1) i.e., α =0 in Eq. [\(7\)](#page-3-3); SGOOD (base) further ablates all substructure-related representations in Section [3.1.](#page-2-6) In Table [5,](#page-6-2) first observe that, from SGOOD (base) to SGOOD\A and then to the complete version SGOOD, the performance gradually increases on all datasets, validating the effectiveness of all proposed techniques. Second, SGOOD\A already surpasses the best baseline performance on most datasets, which demonstrates the effect of the techniques in Section [3.1,](#page-2-6) without the augmentation techniques in Section [3.2.](#page-3-1) With the help of the substructure-preserving graph augmentations, SGOOD pushes the performance further higher. In Figure [3,](#page-6-3) we visualize the ID and OOD score distributions of SGOOD (base), SGOOD\A and SGOOD on DrugOOD, with their mean scores shown in dotted lines. Clearly, we are obtaining more separable OOD scores against ID data from left to right in Figure [3,](#page-6-3) which demonstrates that our techniques in SGOOD can learn distinguishable representations for ID and OOD graphs.

Effect of Task-agnostic Substructure Detection Methods. As mentioned, SGOOD is orthogonal to specific substructure extraction methods. Here in SGOOD, we evaluate several commonly-used methods to extract substructures, including Graclus [\[6\]](#page-9-20), label propagation (LP) [\[4\]](#page-9-19), and BRICS [\[5\]](#page-9-35). BRICS uses chemistry knowledge for extraction. In Table [6,](#page-6-0) SGOOD with different substructure detection methods are all better than SGOOD w.o. substructures, and SGOOD

Table 7: Comparing with subgraph-aware models AUROC (%). Bold: best. Underline: runner-up.

Method	ENZYMES IMDB-M IMDB-B BACE BBBP DrugOOD					
SAG	70.40	76.50	77.30	76.90	58.90	65.80
TopK	70.20	76.80	77.20	74 20	54 90	58.50
DiffPool	73.30	75.90	78.00	76.50	57 50	70.60
NGNN	70.30	71 20	76.60	71 20	52.60	75.60
$GNN-AK$ ⁺	68.50	73.50	77 20	70.90	54 30	63.00
SGOOD	74.41	78.84	80.42	84.40	61.25	73.16

with Modularity is the best. The results validate the effectiveness of SGOOD that leverages substructures for OOD detection.

Comparison with Task-specific Subgraph Models. We then compare SGOOD directly with subgraph GNN models, including three hierarchical pooling methods (SAG [\[18\]](#page-9-14), TopK [\[9\]](#page-9-13), DiffPool [\[39\]](#page-9-15)) and two subgraph GNNs (NGNN $[42]$ and GNN-AK⁺ $[46]$). Note that these methods are not specifically designed for graphlevel OOD detection. At test time, we extract the graph representations generated by these methods and use Mahalanobis distance as OOD score. Table [7](#page-7-1) reports the AUROC results. SGOOD performs best on 5 out of 6 datasets and is the top-2 on DrugOOD. This validates the effectiveness of our substructure-related techniques in Section [3](#page-1-2) for graph-level OOD detection.

Effect of Augmentations. We evaluate the augmentations (SD, SG, and SS) in Section [3.2,](#page-3-1) with conventional graph augmentations that are not substructure-preserving, including edge perturbation (EP), attribute masking (AM), node dropping (ND), and subgraph sampling (SA). Table [8](#page-7-2) reports the results, AM is not applicable on IMDB-M and IMDB-B since they do not have node attributes. Observe that our SD, SG, and SS are the top-3 ranked techniques for graph-level OOD detection, validating the effectiveness of the proposed substructure-preserving graph augmentations. In Appendix Figure [7,](#page-8-0) we also visualize the improvements of all pairwise combinations of our augmentation techniques.

Performance under Different Backbones. We evaluate SGOOD and competitors when changing the GIN backbone to GCN [\[17\]](#page-9-12) and GraphSage [\[12\]](#page-9-11). Table [9](#page-7-3) reports the results. With GCN backbone, compared with the baselines, SGOOD consistently achieves the best scores; with GraphSage backbone, SGOOD is the best on BACE, BBP, DrugOOD, and the second best on other datasets. The results validate the robustness of SGOOD to different backbones.

Model efficiency. We compare the training time per epoch in seconds of all methods, with results in Table [10.](#page-7-4) Compared with other graph-level OOD detection competitors, including GraphDE, GOOD-D, and AAGOD, SGOOD requires less time to train. Compared with all methods, including the methods originally designed for image data, SGOOD requires moderate time for training. Considering together the time cost in Table [10](#page-7-4) and the effectiveness in Table [3,](#page-5-0) we can conclude that SGOOD is effective and efficient for graph-level OOD detection,

4.4 Parameter Sensitivity

In this section, we evaluate the performance of SGOOD under varying hyperparameters to test its robustness and sensitivity to parameter settings.

Table 8: Comparing with different augmentations by AUROC.

						ENZYMES IMDB-M IMDB-B BACE BBBP DrugOOD Avg. Rank
EP	74.28	76.50	78.44	78.75 58.24	71.32	4.67
AM	72.44			77.28 59.68	71.27	5.25
ND.	73.11	77.09	78.40	78.79 58.59	69.48	4.83
SA	72.12	76.76	79.25	77.13 57.84	72.66	4.83
SD.	74.77	78.15	79.54	82.00 59.76	72.65	1.83
SG	72.74	77.98	78.97	82.24 59.58	71.97	3.33
SS	74.27	76.20	80.50	83.53 63.53	7194	2.67

Table 9: Performance with different backbones by AUROC (%). Bold: best. Underline: runner-up.

Backbone		Method ENZYMES IMDB-M IMDB-B BACE BBBP DrugOOD					
	MAH	70.04	71.27	53.46	72.68	54.97	66.01
	GraphDE	61.40	68.44	29.13	53.24	52.50	56.61
GCN	GOOD-D	41.96	61.71	59.53	72.52	58.91	61.79
	OCGIN	64.35	57.46	64.08	67.54	51.23	59.30
	SGOOD	71.26	73.52	65.91	83.42 62.76		72.52
	MAH	68.07	48.06	43.63	73.60	53.88	64.55
	GraphDE	61.37	69.65	28.28	53.24	52.50	56.66
GraphSage GOOD-D		45.55	57.02	23.90	73.15	56.85	61.57
	OCGIN	71.75	36.86	71.44	57.47	46.65	63.82
	SGOOD	70.21	68.63	61.59	82.22 59.50		68.60

Table 10: Training time per epoch of all methods on all datasets by seconds (s).

Figure 4: OOD detection performance of SGOOD by AUROC (%) when the number of pretraining epochs T_{PT} varies from 0 to 200, with colored area representing standard deviation.

Varying pretraining epochs T_{PT} . We conduct experiments to study the effect of pretraining epochs T_{PT} from 0 to 200. As shown in Figure [4,](#page-7-0) compared to SGOOD without first-stage pretraining $(TPT = 0)$, pretraining improves SGOOD's performance. We also found that excessive pretraining can sometimes have negative effects. For example, when $T_{PT} = 200$, SGOOD's performance decrease on all datasets except ENZYMES. We speculate the reason is

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Figure 5: OOD detection results of SGOOD by AUROC (%) when the weight of the contrastive loss α varies from 0 to 1, with the colored area representing standard deviation.

Figure 6: OOD detection results of SGOOD by AUROC (%) when the batch size B varies from 16 to 256.

Figure 7: AUROC gain (%) of SGOOD compared with SGOOD\A without graph augmentations.

that excessive pretraining makes task-agnostic information dominate, with a negative impact on the SGOOD's ability to learn from class labels. As $T_{PT} = 100$ generally leads to competitive performance across all datasets, we set the default value of T_{PT} to 100.

Varying the weight of contrastive loss α . We vary α from 0 to 1 to study the effect. As shown in Figure [5,](#page-8-1) compared to SGOOD fine-tuned solely by \mathcal{L}_{CE} (i.e., $\alpha = 0$), fine-tuning SGOOD with both \mathcal{L}_{CE} and \mathcal{L}_{CL} generally leads to better performance. As $\alpha = 0.1$ usually leads to competitive performance across all datasets, we set the default value of α to 0.1 in SGOOD.

Varying number of negative samples in \mathcal{L}_{CL} . We conduct experiments to study the effect of the number of negative samples used in contrastive loss \mathcal{L}_{CL} (Eq.[\(6\)](#page-3-4)). Following the established convention in graph contrastive learning [\[40\]](#page-9-22), pairs of augmented graphs originating from the same graph are treated as positive pairs,

Table 11: Varying L_1 and L_2 in SGOOD (AUROC).

		L_1 L_2 ENZYMES IMDB-M IMDB-B BBBP BACE DrugOOD					
	$4 \quad 1$	74.00	77.13	81.00		80.43 62.00	71.17
3	2	74.41	78.84	80.42	84.40 61.25		73.16
2°	$\mathbf{3}$	73.63	76.03	79.05		80.34 62.26	69.12
1	$\overline{4}$	74 22	77.83	76.79		76.62 61.08	68.01

while pairs generated from different graphs within the batch are considered negative pairs. In such a way, in a B -size batch, for every G_i , it will have 2B-2 negative samples, as shown in the denominator of Eq.[\(6\)](#page-3-4). Apparently the number of negative samples is related to batch size B . We vary B from 16 to 256 to evaluate sensitivity of SGOOD w.r.t. the number of negative samples, and report the results in Figure [6](#page-8-2) . Observe that as increasing from 16 to 128, the overall performance increases and then becomes relatively stable, which proves the effectiveness of the augmentation techniques developed in SGOOD and also validates the superior performance of SGOOD when varying batch size and the number of negative samples.

Varying different combinations of augmentations. In Figure [7,](#page-8-0) we exhaust the pairwise combinations of all options in $A =$ {I, SD, SG, SS} and visualize the AUROC gain on graph-level OOD detection over SGOOD\A without graph augmentations. As shown in Figure [7,](#page-8-0) most combinations achieve positive gains for effective OOD detection.

Varying L_1 and L_2 . In the experiments above, we fix the layers of the two GINs in the two-level graph encoding in Section [3.1](#page-2-6) to be $L_1 = 3$ and $L_2 = 2$ as default. If we search L_1 and L_2 , it is possible to get even better OOD detection results, as shown in Table [11](#page-8-3) where L_1 and L_2 are varied with their sum fixed to be 5. For example, on BACE with L_1 =2 and L_2 =3, AUROC is 62.26%, about 1% higher than the default setting.

5 RELATED WORK

Graph-level Representation Learning. Graph-level representation learning aims to learn representations of entire graphs [\[34\]](#page-9-36). GNNs [\[12,](#page-9-11) [17,](#page-9-12) [31,](#page-9-37) [36\]](#page-9-21) are often adopted [\[11,](#page-9-38) [38\]](#page-9-6) to first learn node representations by message passing on graphs, and then node representations are aggregated by flat pooling functions to get graphlevel representations [\[36\]](#page-9-21). However, these traditional methods have limitations in capturing high-order structures with crucial semantics for graph-level tasks, e.g., functional groups in molecules [\[39\]](#page-9-15). Hence, there exist methods to leverage subgraphs, e.g., hierarchical pooling [\[9,](#page-9-13) [18,](#page-9-14) [39\]](#page-9-15) and subgraph GNNs [\[42,](#page-10-2) [46\]](#page-10-3). Hierarchical pooling methods learn to assign nodes into different clusters and coarsen graphs hierarchically. Subgraph GNNs apply message passing on extracted rooted-subgraphs of nodes in a graph, and then aggregate subgraph representations [\[8\]](#page-9-39). These methods are not designed for graph OOD detection, and they assume that graphs are i.i.d in training and testing and learn task-specific substructures. In this paper, we explore leveraging task-agnostic substructures to learn expressive graph representations for OOD detection.

Graph Out-of-distribution Detection. Out-of-Distribution (OOD) detection has recently received considerable research attention on

graph data. [\[33\]](#page-9-32) explore node-level OOD detection by using energy function to detect OOD nodes in a graph, which is a different problem from this paper. For graph-level OOD detection, [\[21\]](#page-9-5) design a generative model that has the ability to identify outliers in training graph samples, as well as OOD samples during the testing stage. [\[24\]](#page-9-10) develop a self-supervised learning approach to train their model to estimate OOD scores at test time. Recently, [\[41\]](#page-9-40) proposes to learn anomalous substructures using deep random walk kernel, which depends on labeled anomalous graphs, while OOD graphs are unseen during the training stage and only available during the testing stage. Instead of training GNNs for OOD detection, AAGOD [\[10\]](#page-9-9) develops an adaptive amplifier that modifies the graph structure to enlarge the gap between OOD and ID graphs. Observe that existing graph-level OOD detection methods mainly leverage node representations output by GNNs [\[17,](#page-9-12) [31,](#page-9-37) [36,](#page-9-21) [47\]](#page-10-6) to get graph-level representations, while the rich substructure patterns hidden in graphs are under-investigated for graph-level OOD detection. On the other hand, our method SGOOD explicitly uses substructures in graphs to learn high-quality representations for effective graph-level OOD detection.

6 CONCLUSION

We study the problem of graph-level OOD detection, and present a novel SGOOD method with superior performance. The design of SGOOD is motivated by the exciting finding that substructure differences commonly exist between ID and OOD graphs, and SGOOD aims to preserve more distinguishable graph-level representations between ID and OOD graphs. Specifically, we build a super graph of substructures for every graph, and develop a two-level graph encoding pipeline to obtain high-quality structure-enhanced graph representations. We further develop a set of substructure-preserving graph augmentations. Extensive experiments on real-world graph datasets with various OOD types validate the superior performance of SGOOD over existing methods for graph-level OOD detection.

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