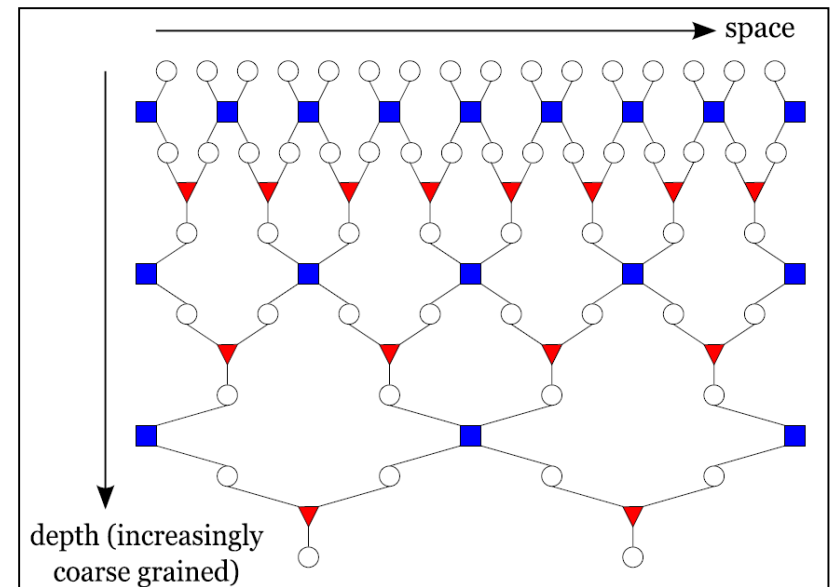
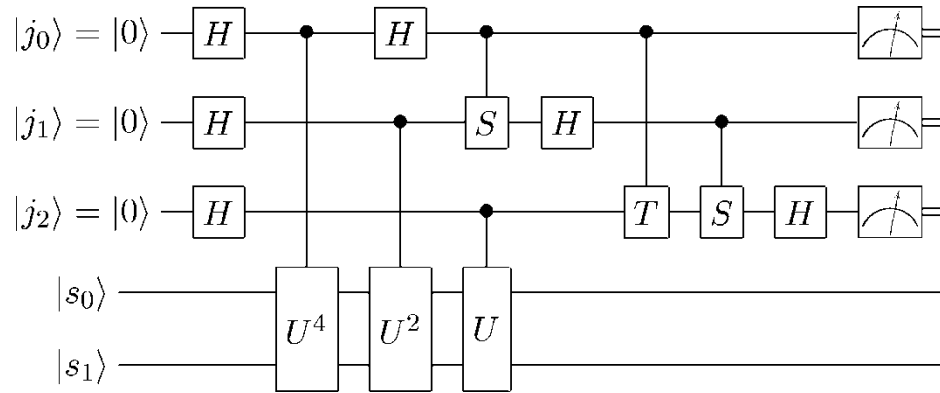
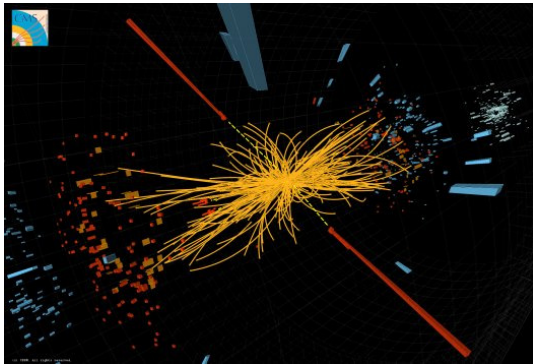


Quantum computing and the entanglement frontier



Frontiers of Physics

short distance



Higgs boson

Neutrino masses

Supersymmetry

Quantum gravity

String theory

long distance



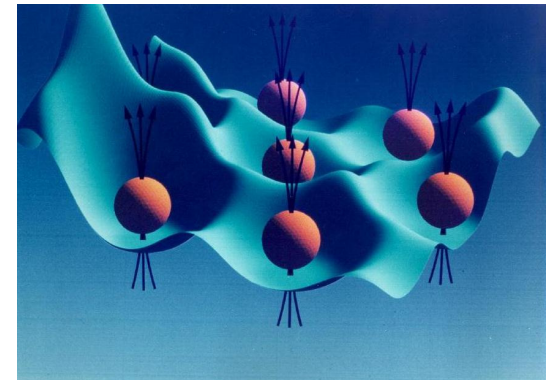
Large scale structure

Cosmic microwave background

Dark matter

Dark energy

complexity



“More is different”

Many-body entanglement

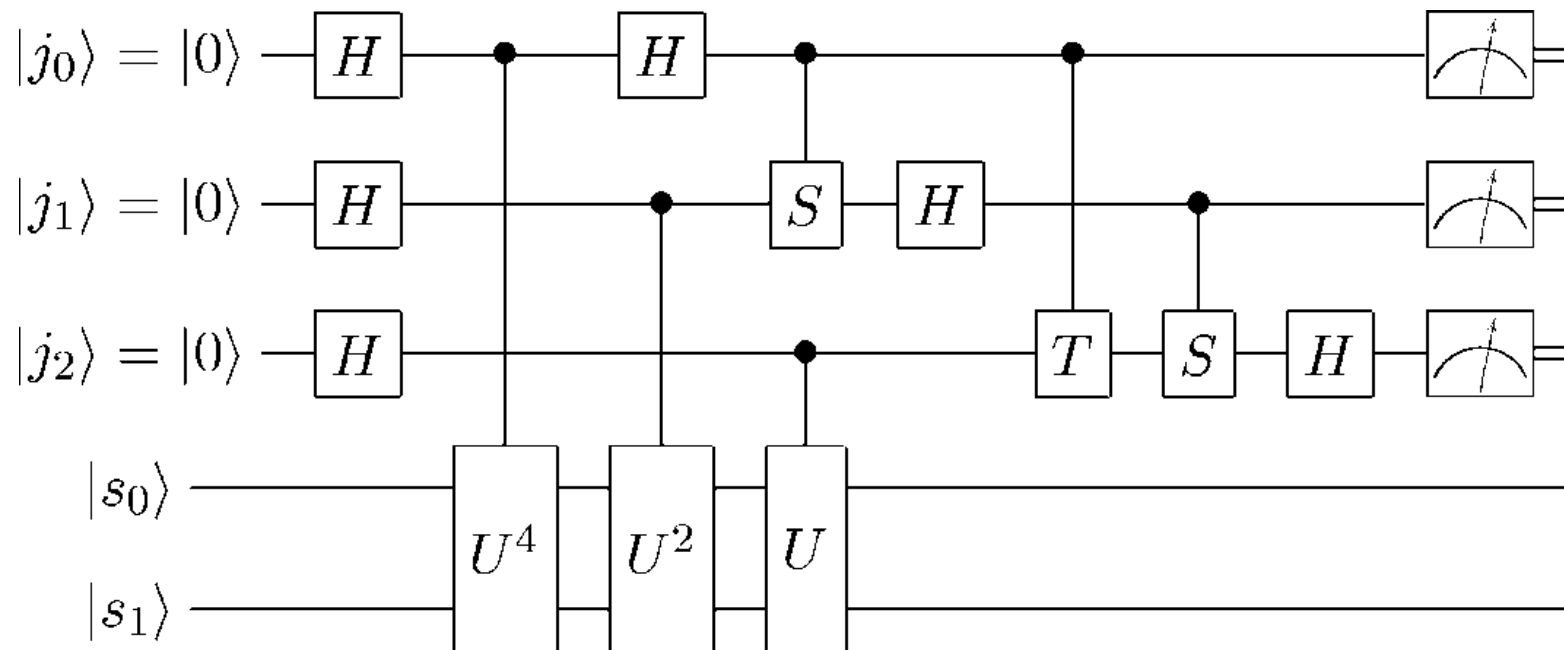
Phases of quantum matter

Quantum computing

Quantum Information Science:

Can we control complex quantum systems and if so what are the scientific and technological implications?

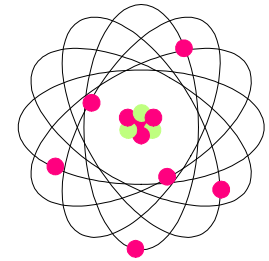
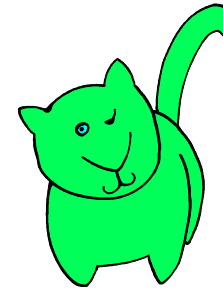
Not the frontier of short (subnuclear) distances or long (cosmological) distances, but rather the frontier of highly complex quantum states: *The entanglement frontier*



Truism:

the macroscopic world is classical.

the microscopic world is quantum.



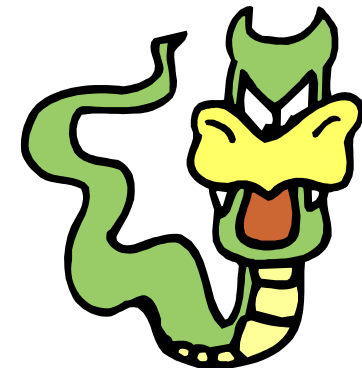
Goal of Quantum Information Science:
controllable quantum behavior in scalable systems

Why?

Classical systems cannot simulate quantum systems
efficiently (a widely believed but unproven conjecture).

But to control quantum systems we must slay the dragon of
decoherence ...

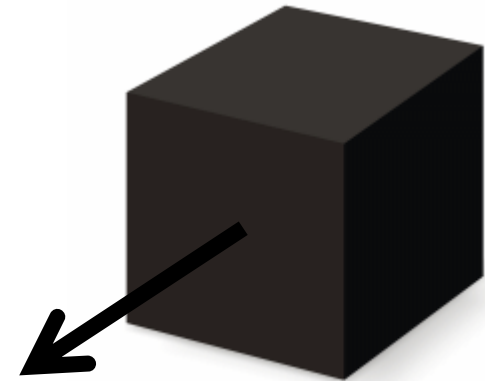
Is this merely *really, really hard*?
Or is it *ridiculously hard*?



Toward quantum supremacy

Sufficiently complex quantum systems will behave in ways that cannot be predicted using digital computers --- these systems will “surpass understanding” and surprise us.

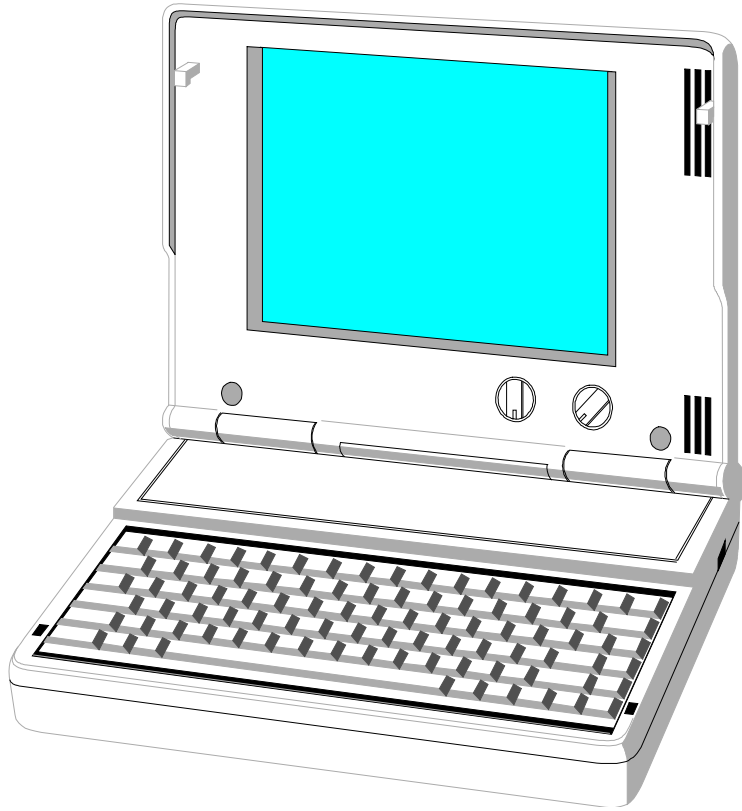
???!!



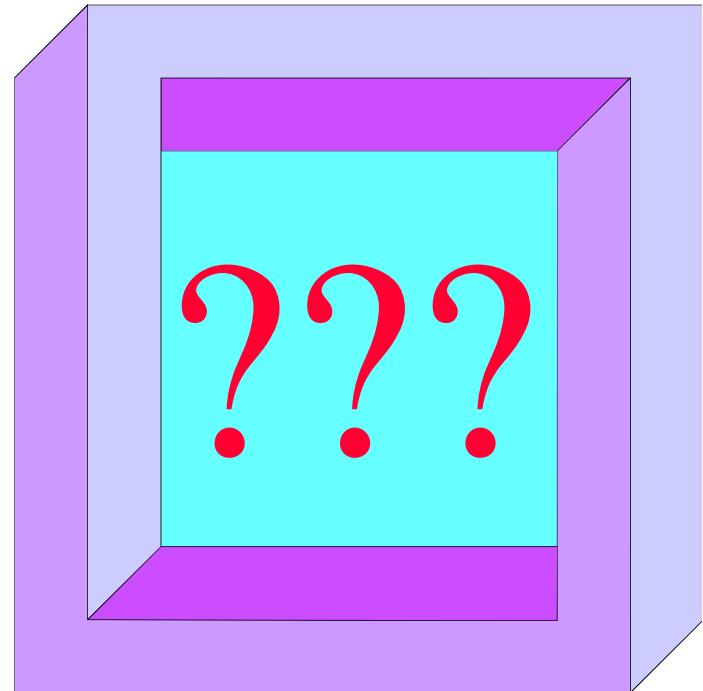
What quantum tasks are feasible?

What quantum tasks are hard to simulate classically?

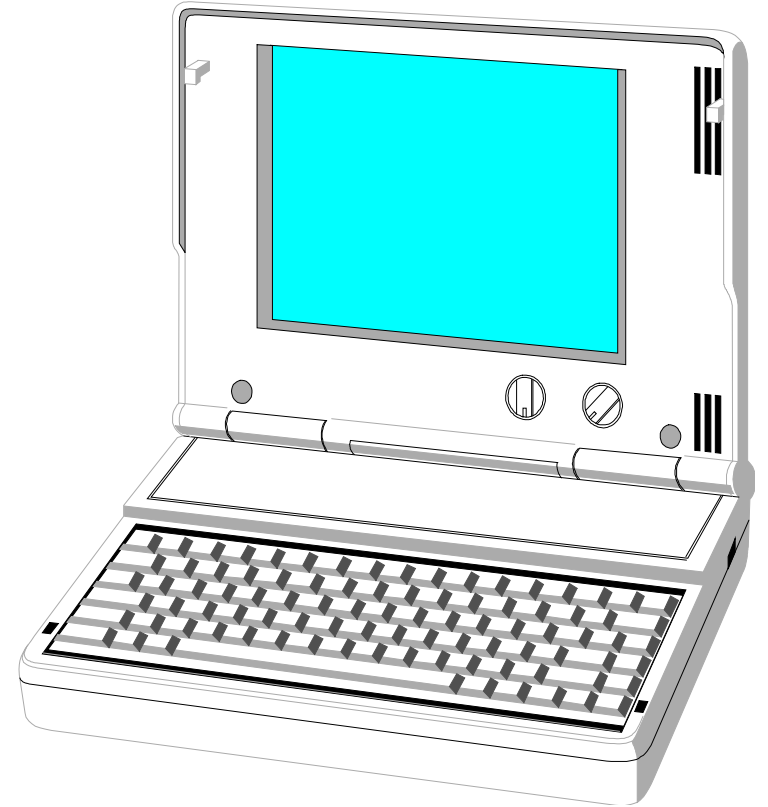
Or ... might it be that the extravagant “exponential” classical resources required for classical description and simulation of generic quantum states are illusory, because quantum states in Nature have succinct descriptions?



2013



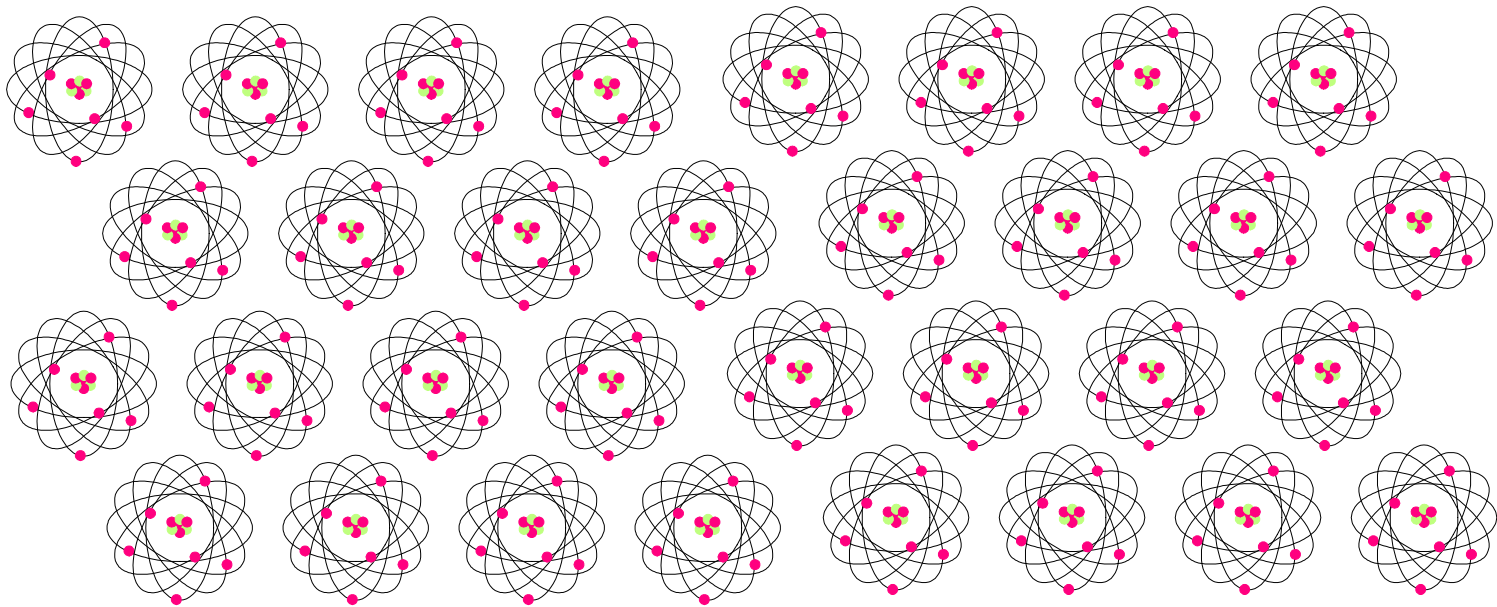
2100



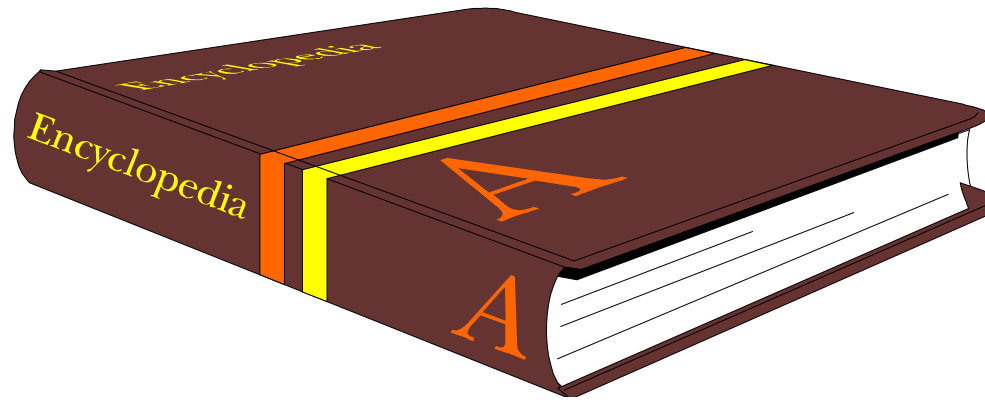
2013

Quantum Theory



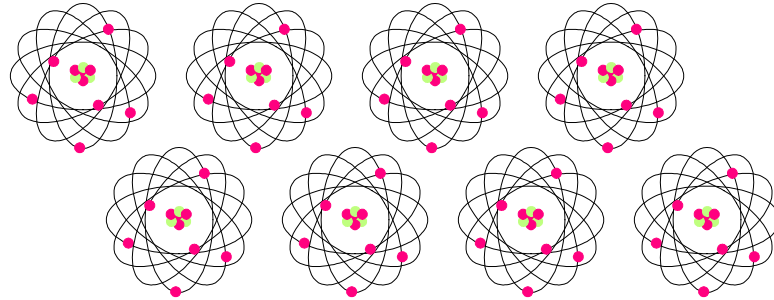


Though quantum theory is over 100 years old, quantum and classical systems differ in profound ways we are just beginning to understand ...



Information

is encoded in the state of a *physical* system.



Information

is encoded in the state of a *quantum* system.



Put
Weirdness

to work!

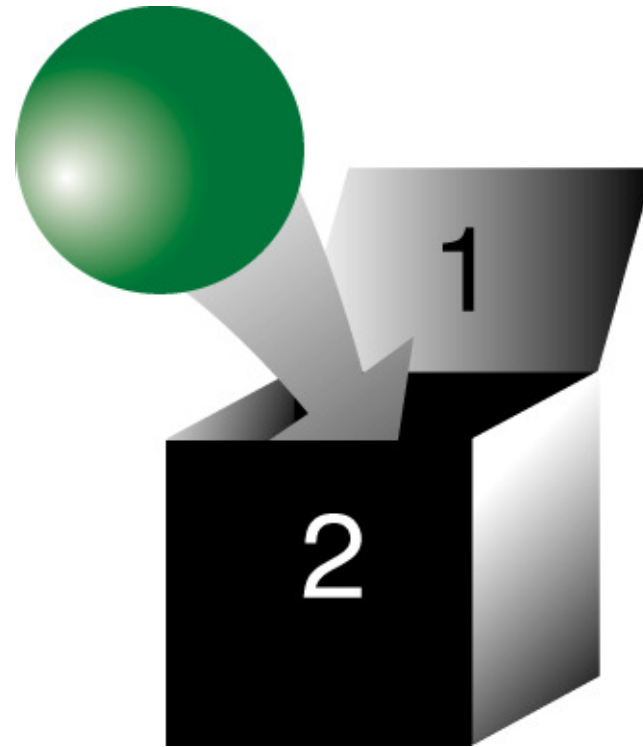
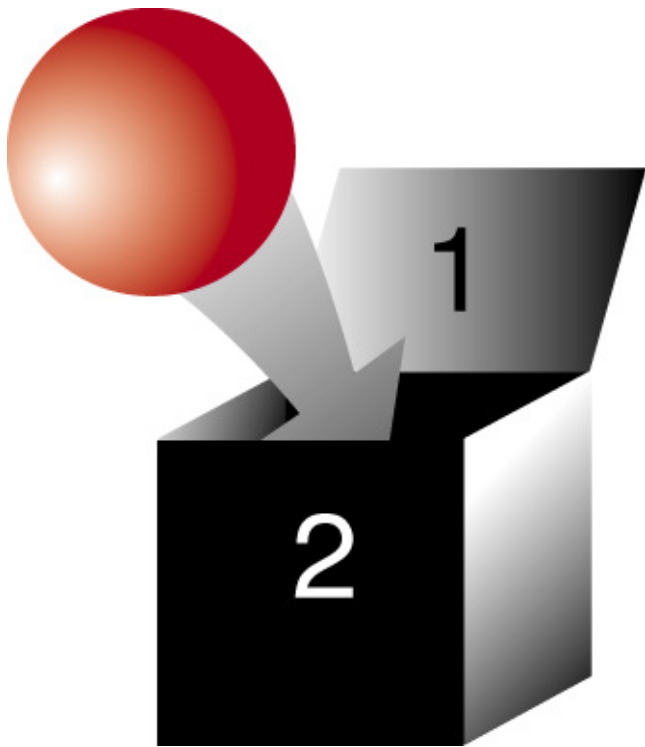
Theoretical Quantum Information Science

is driven by ...

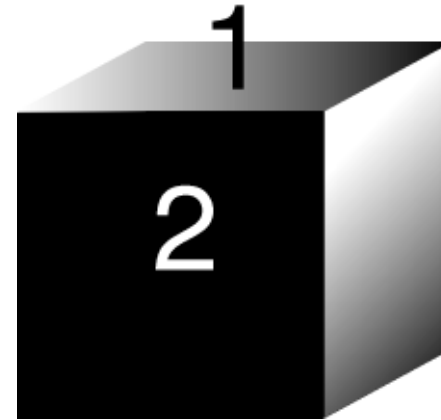
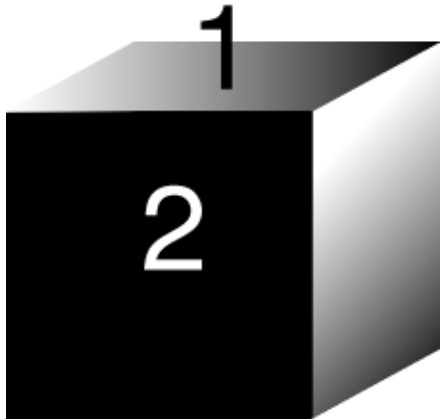
Three *Great* Ideas:

- 1) Quantum Entanglement
- 2) Quantum Computation
- 3) Quantum Error Correction

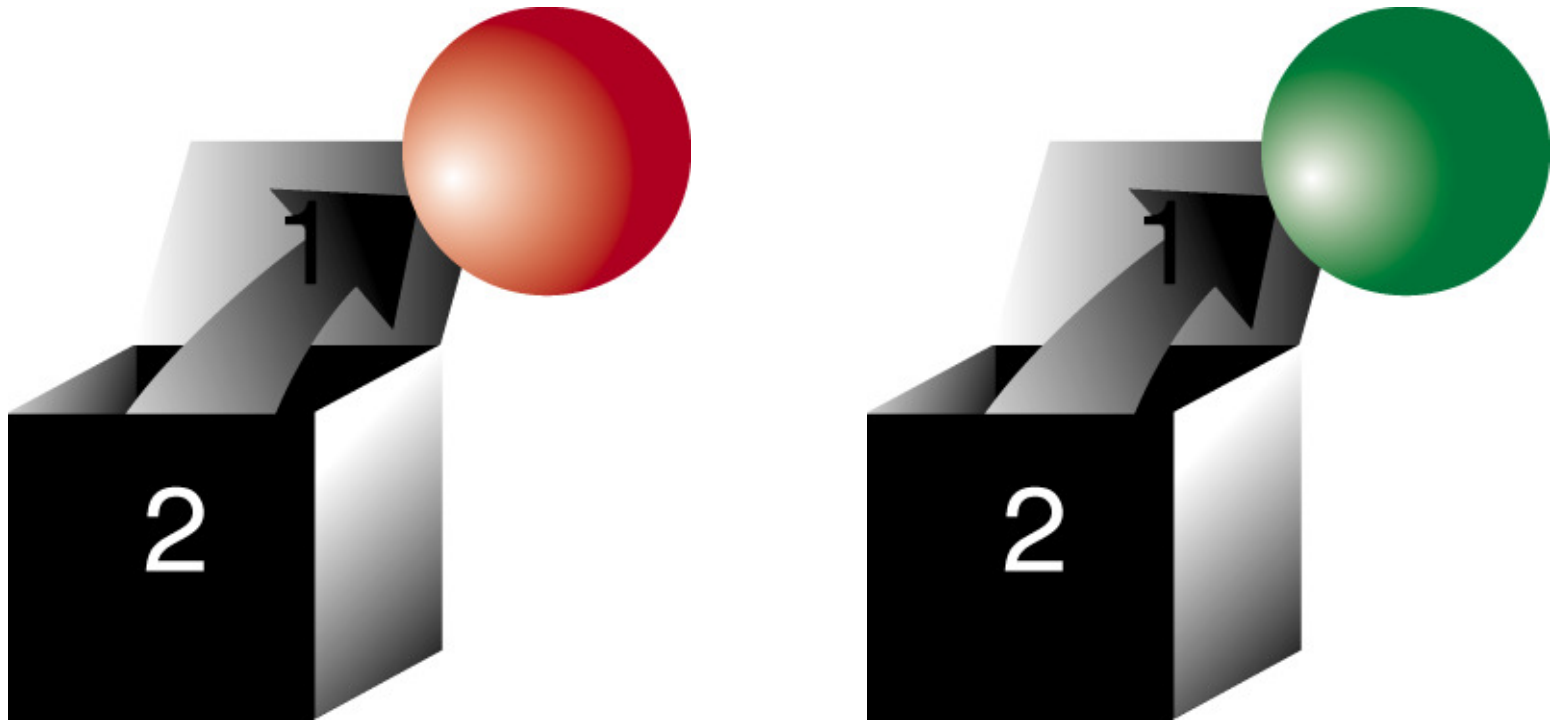
Classical Bit



Classical Bit

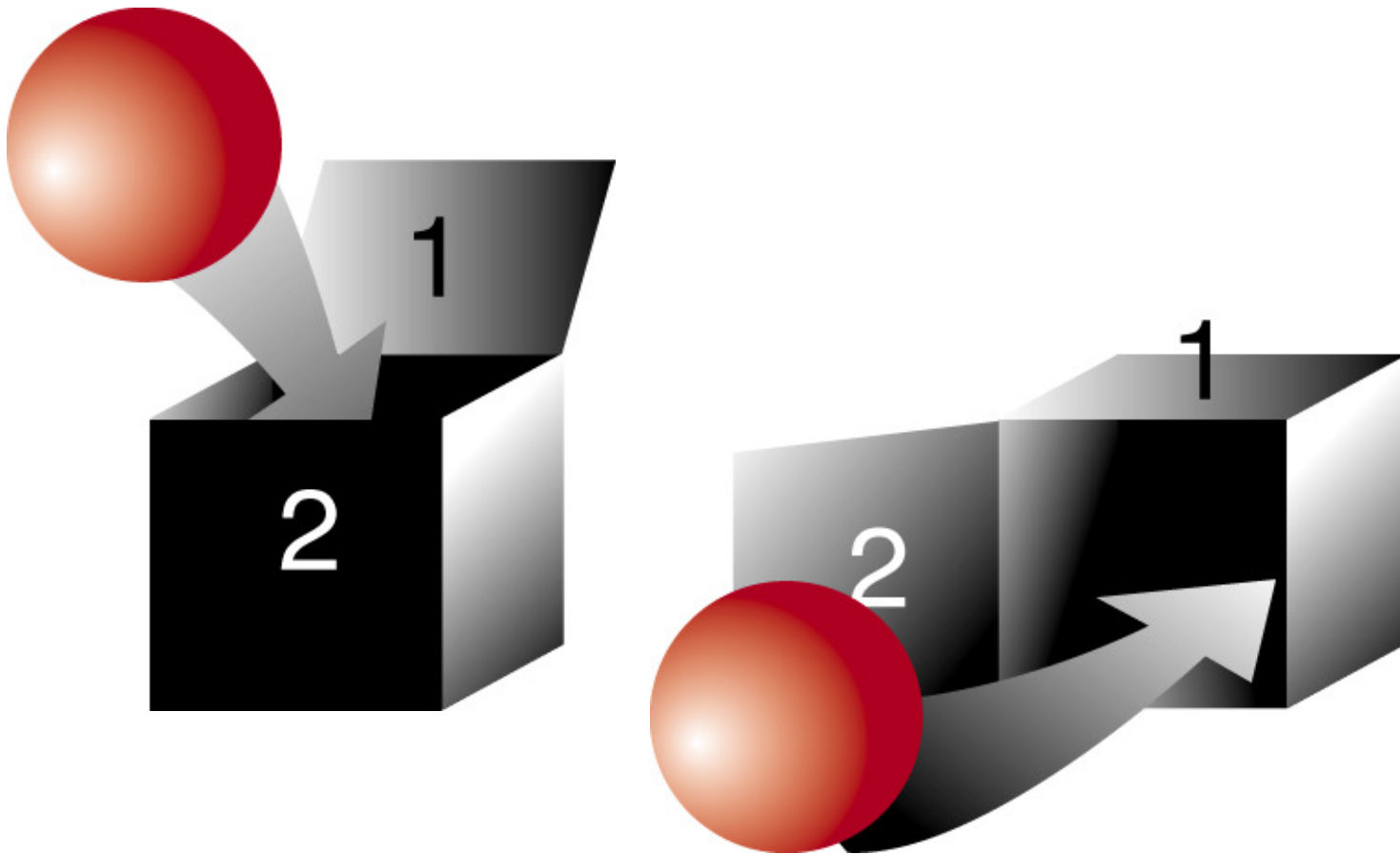


Classical Bit



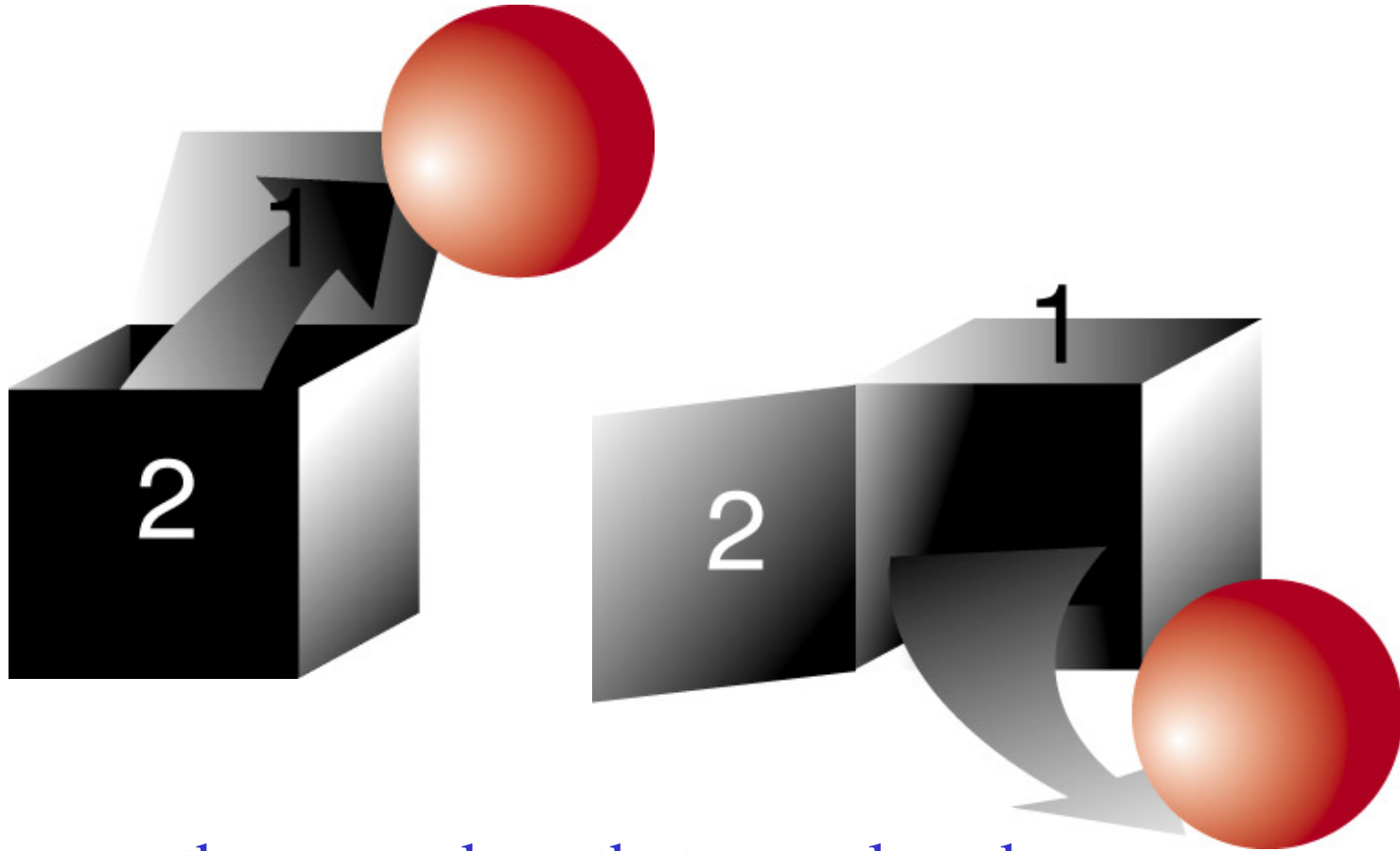
What went in, comes out.

Quantum Bit (“Qubit”)



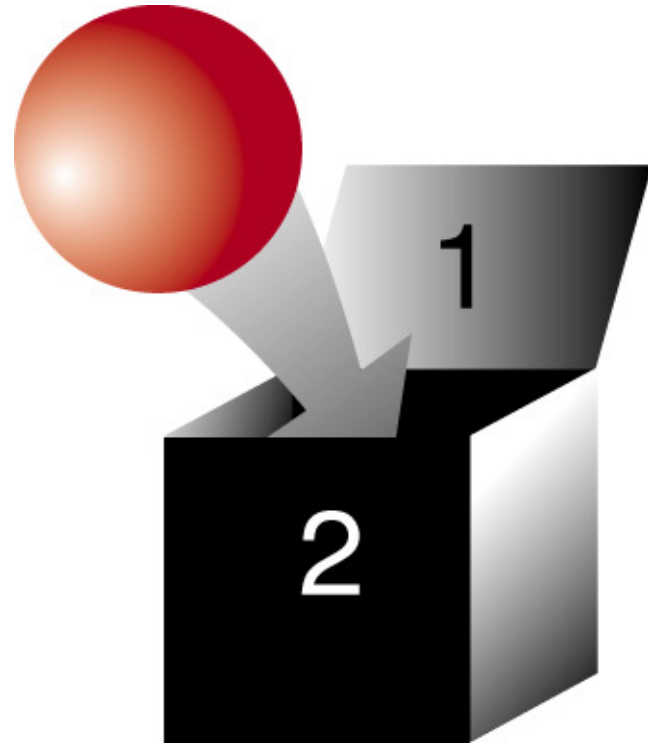
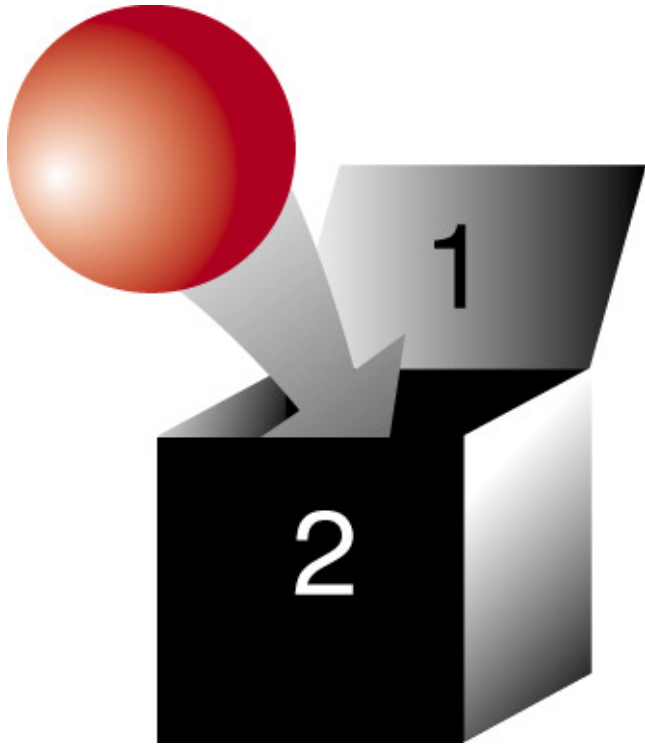
The two doors are two complementary observables, such as two ways to measure the polarization state of a photon.

Quantum Bit (“Qubit”)

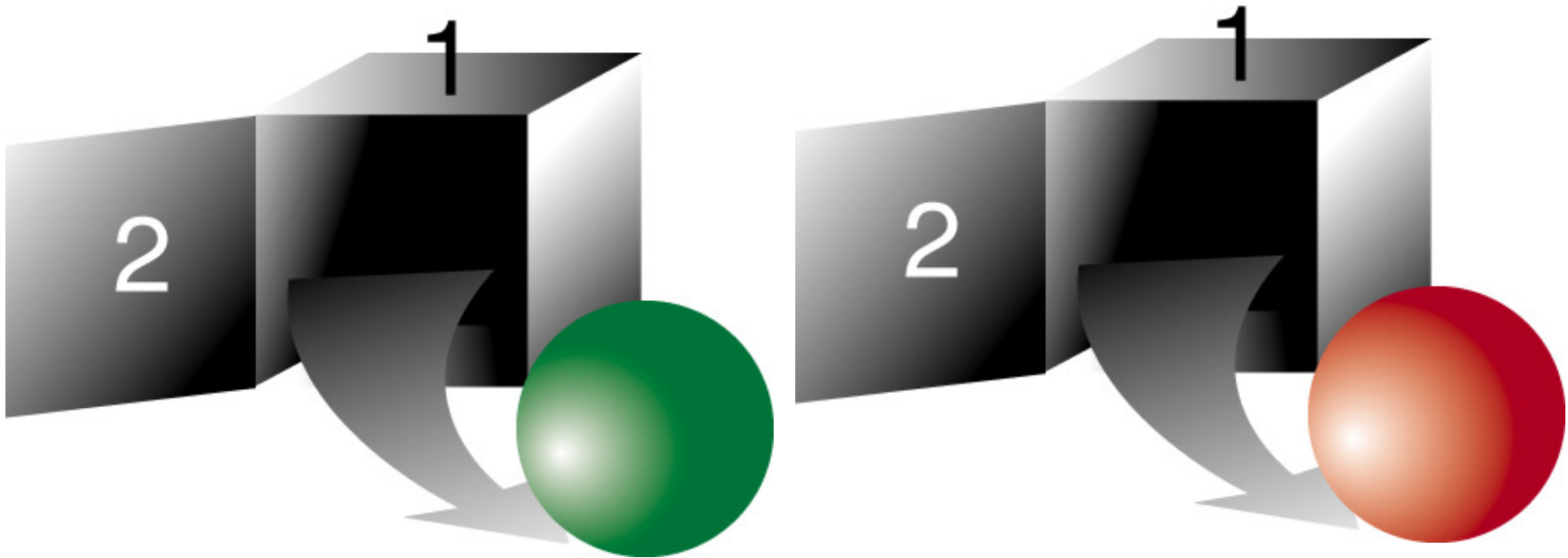


If you open the *same* door that you closed, you can recover the bit from the box.

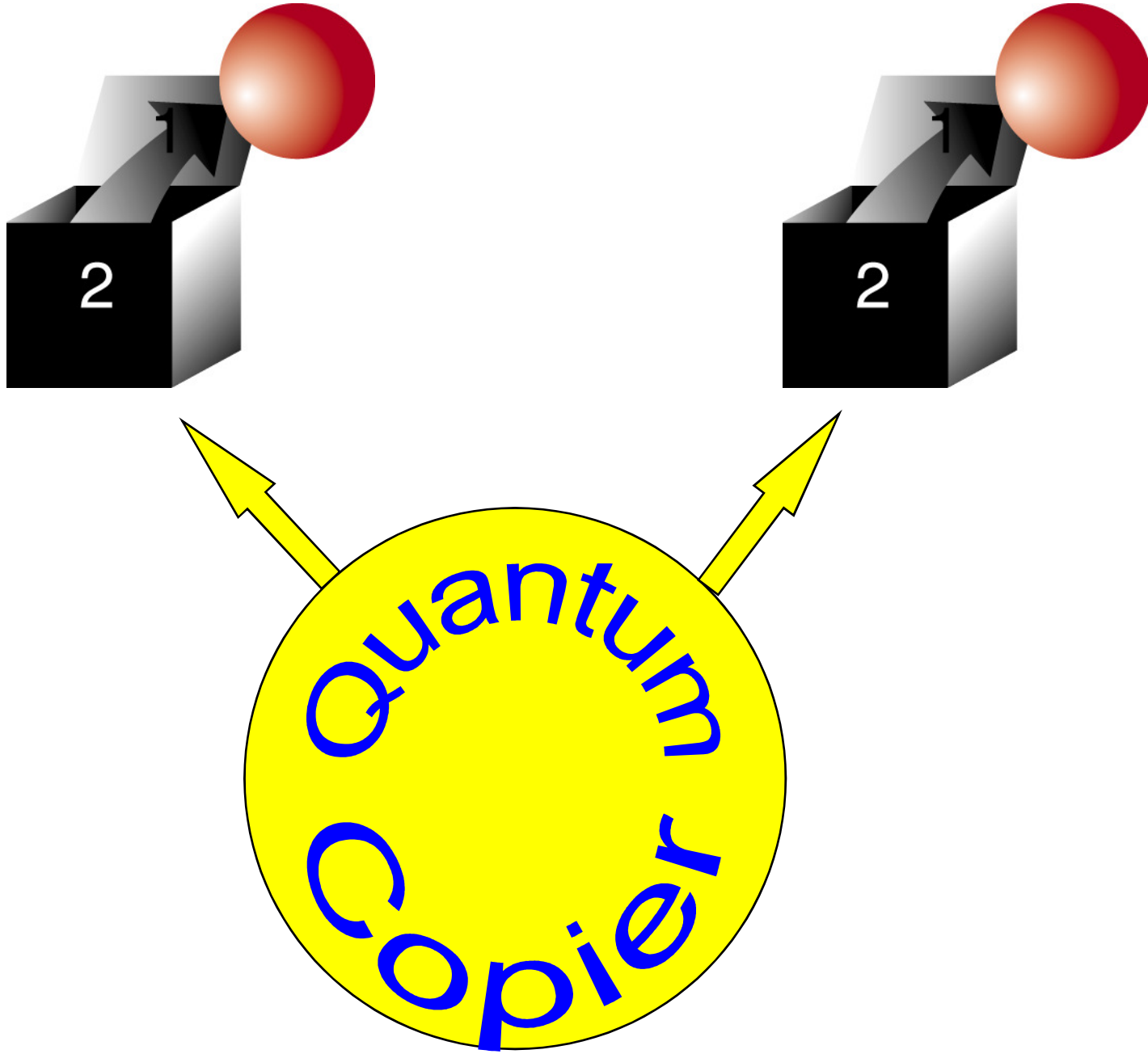
Quantum Bit (“Qubit”)

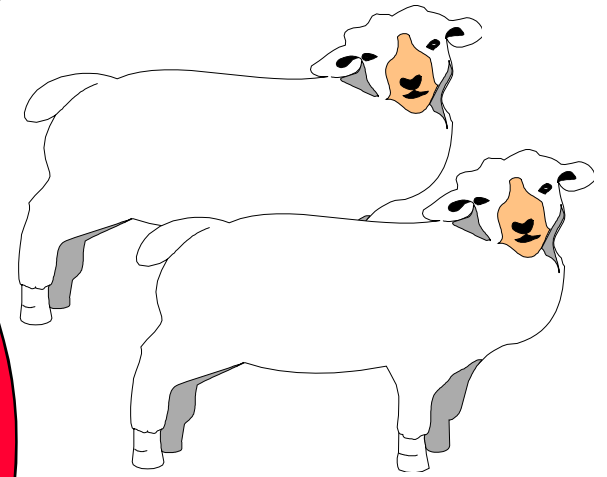
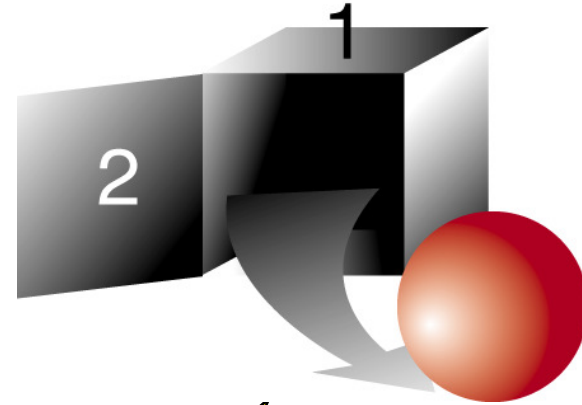
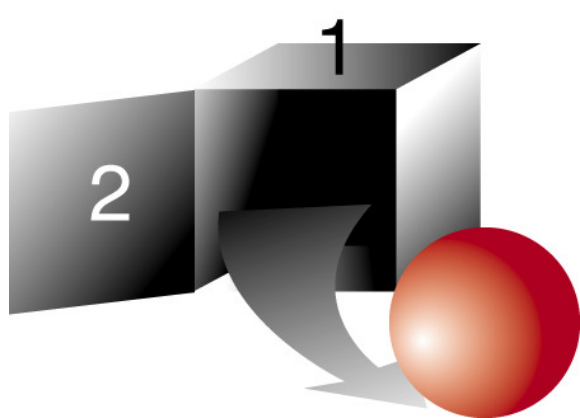


Quantum Bit (“Qubit”)



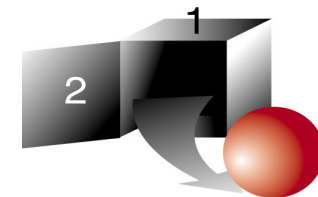
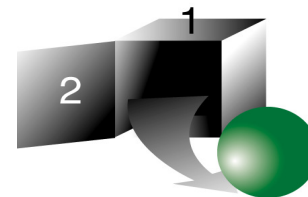
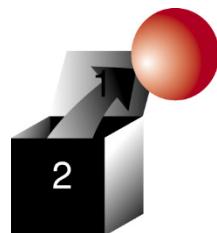
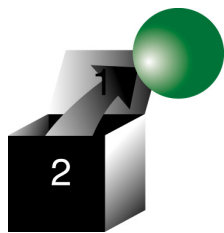
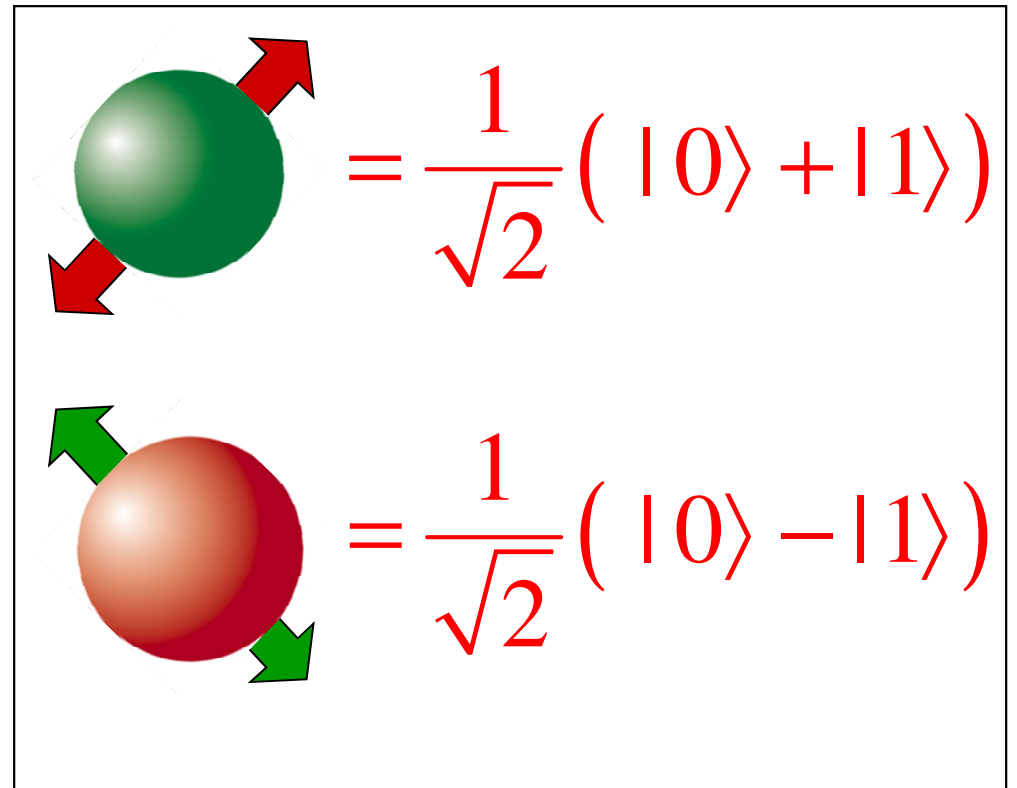
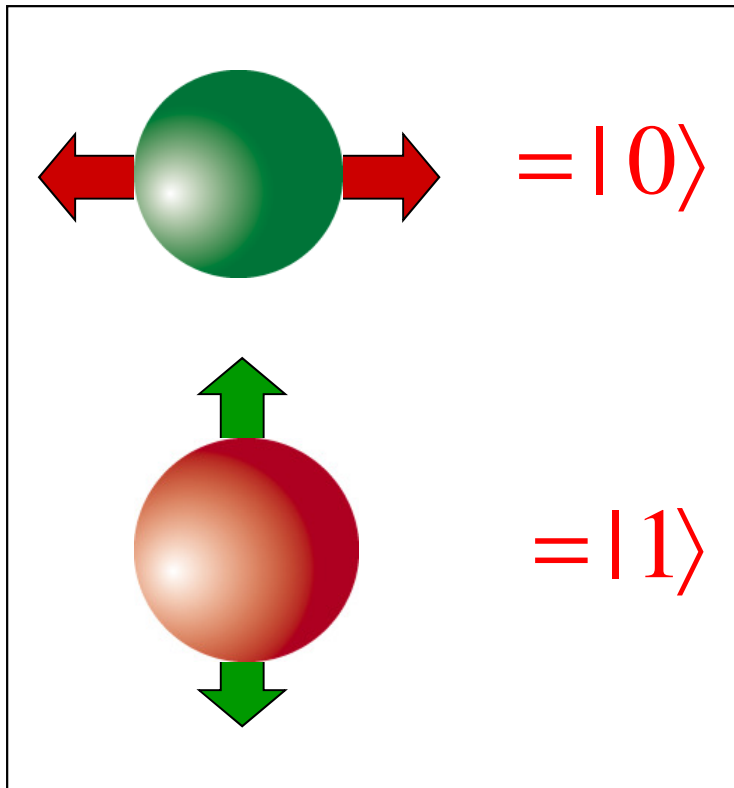
If you open a *different* door than you closed, the color is *random* (red 50% of the time and green 50% of the time).





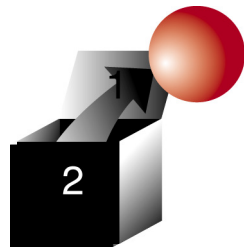
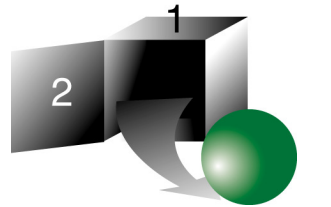
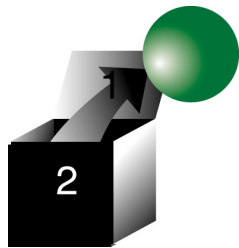
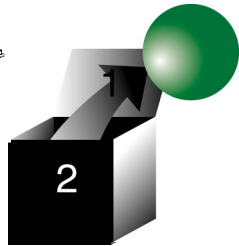
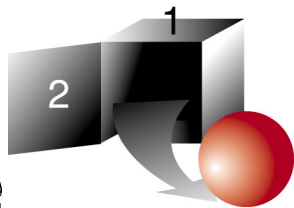
No cloning!

Photon polarization as a qubit

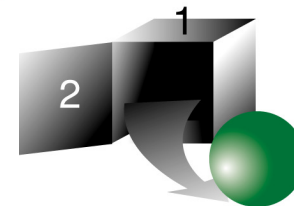
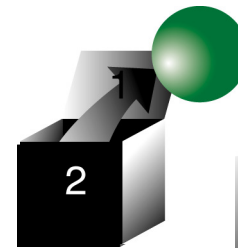
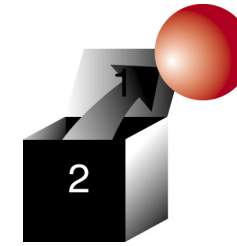
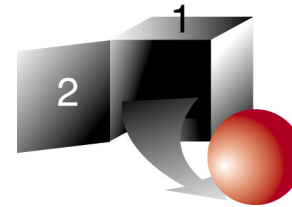
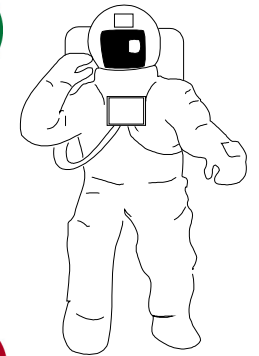
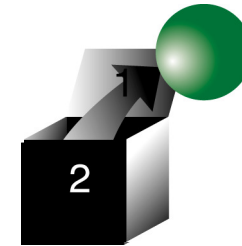


Quantum Correlations

Pasadena



Andromeda

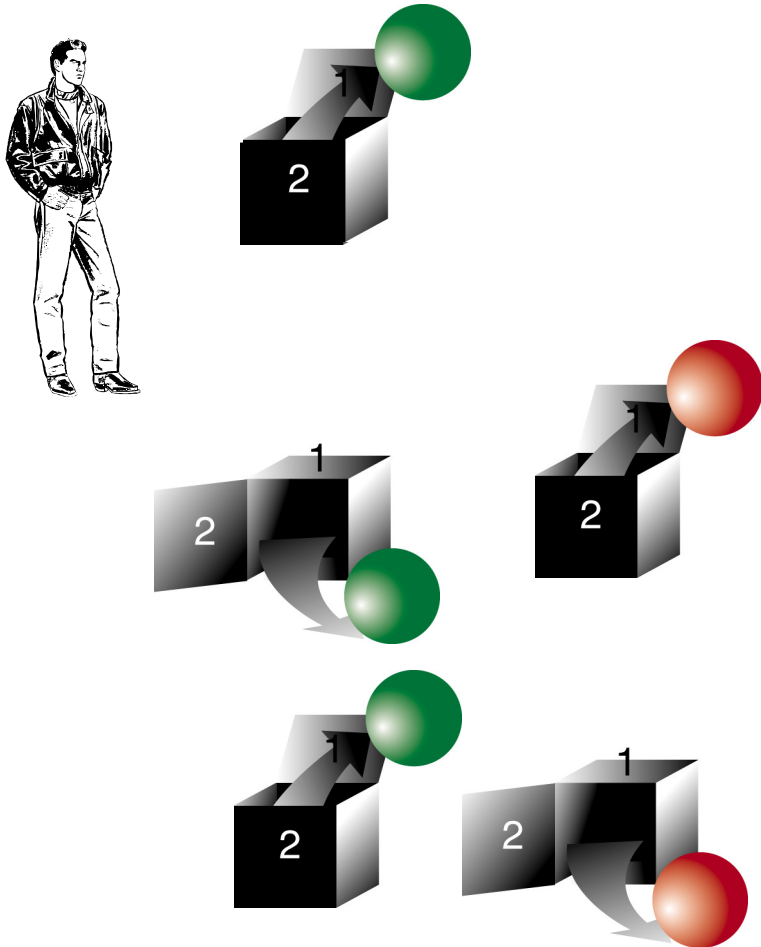


Open either door in Pasadena, and the color of the ball is *random*.

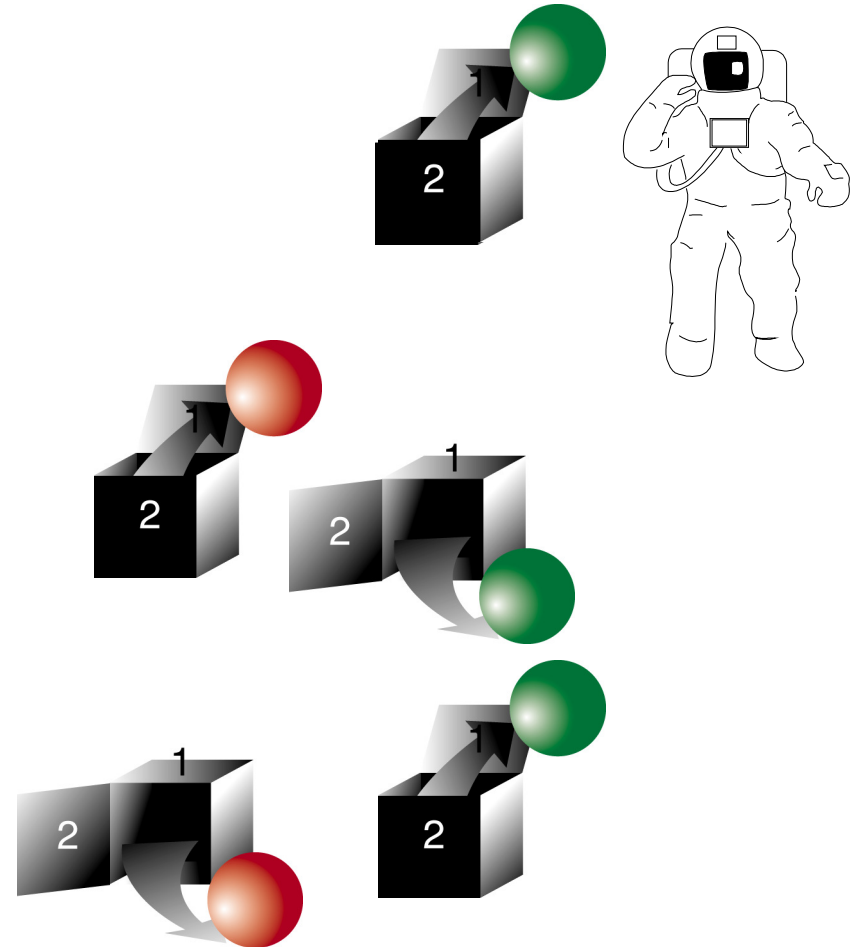
Same thing in Andromeda.

Quantum Correlations

Pasadena



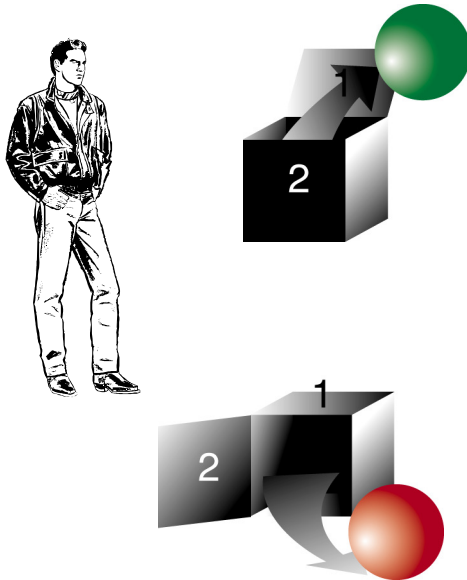
Andromeda



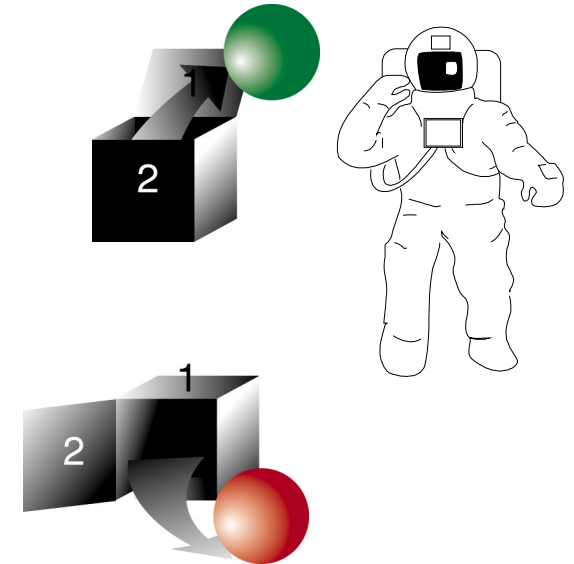
But if we both open the same door, we always find the same color.

Quantum Correlations

Pasadena

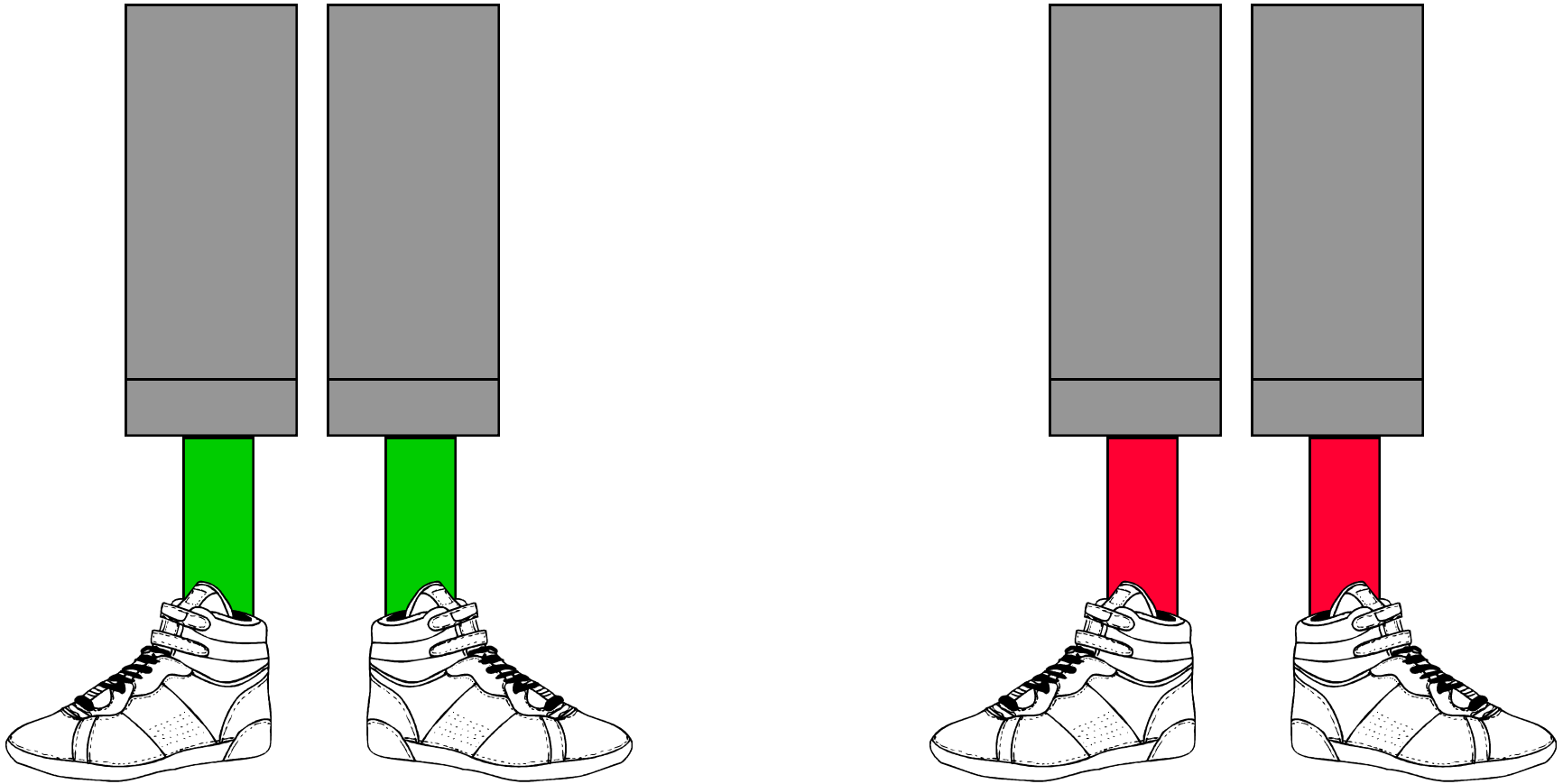


Andromeda

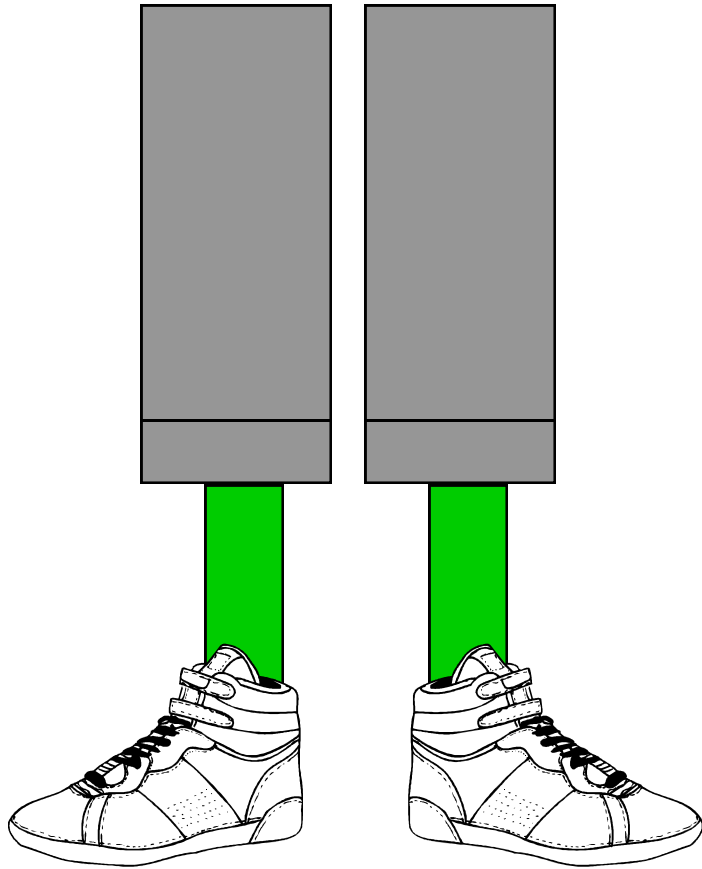


Quantum information can be *nonlocal*, shared equally by a box in Pasadena and a box in Andromeda.

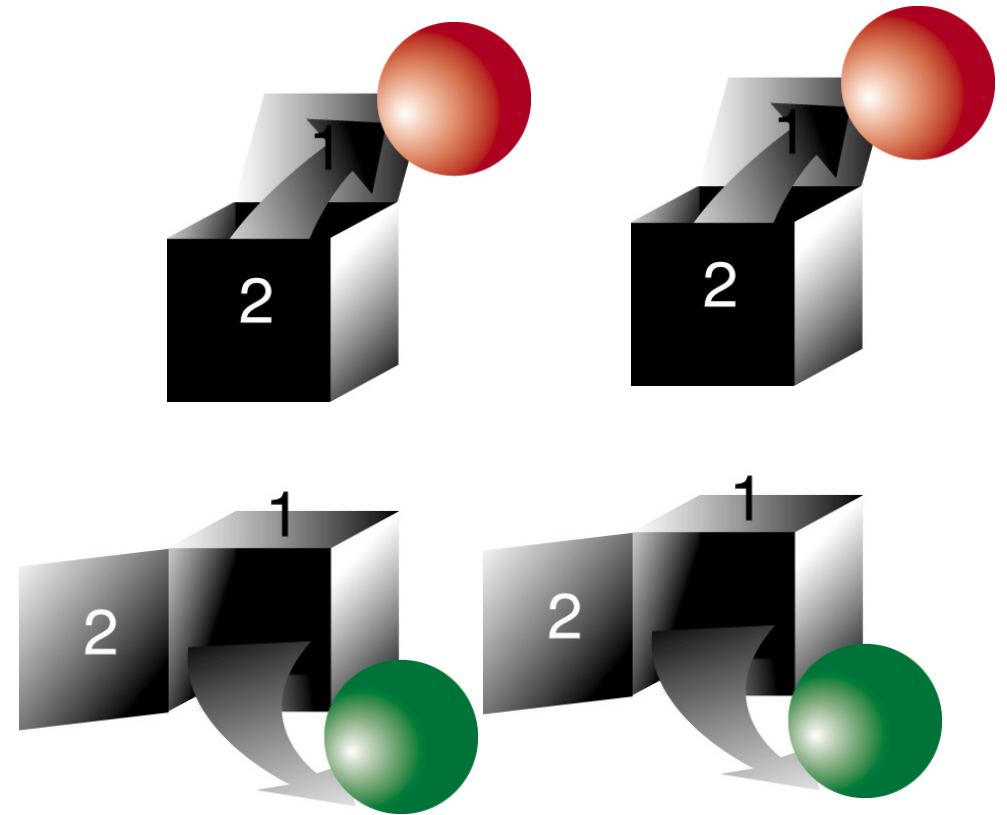
This phenomenon, called *quantum entanglement*, is a crucial feature that distinguishes quantum information from classical information.



Classical Correlations



Classical Correlations



Quantum Correlations

Aren't boxes like soxes?

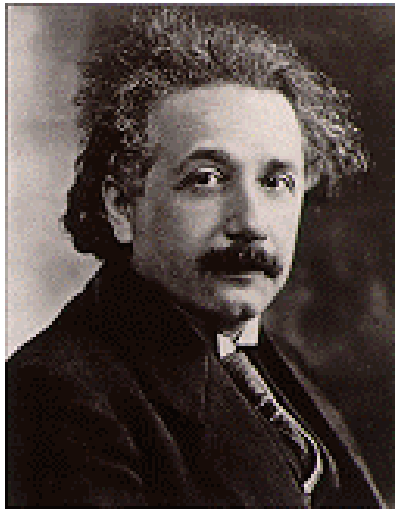
Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)

In a complete theory there is an element corresponding to each element of reality. A sufficient condition for the reality of a physical quantity is the possibility of predicting it with certainty, without disturbing the system. In quantum mechanics in the case of two physical quantities described by non-commuting operators, the knowledge of one precludes the knowledge of the other. Then either (1) the description of reality given by the wave function in

quantum mechanics is not complete or (2) these two quantities cannot have simultaneous reality. Consideration of the problem of making predictions concerning a system on the basis of measurements made on another system that had previously interacted with it leads to the result that if (1) is false then (2) is also false. One is thus led to conclude that the description of reality as given by a wave function is not complete.



Einstein's 1935 paper, with Podolsky and Rosen (EPR), launched the theory of quantum entanglement. To Einstein, quantum entanglement was so unsettling as to indicate that something is missing from our current understanding of the quantum description of Nature.

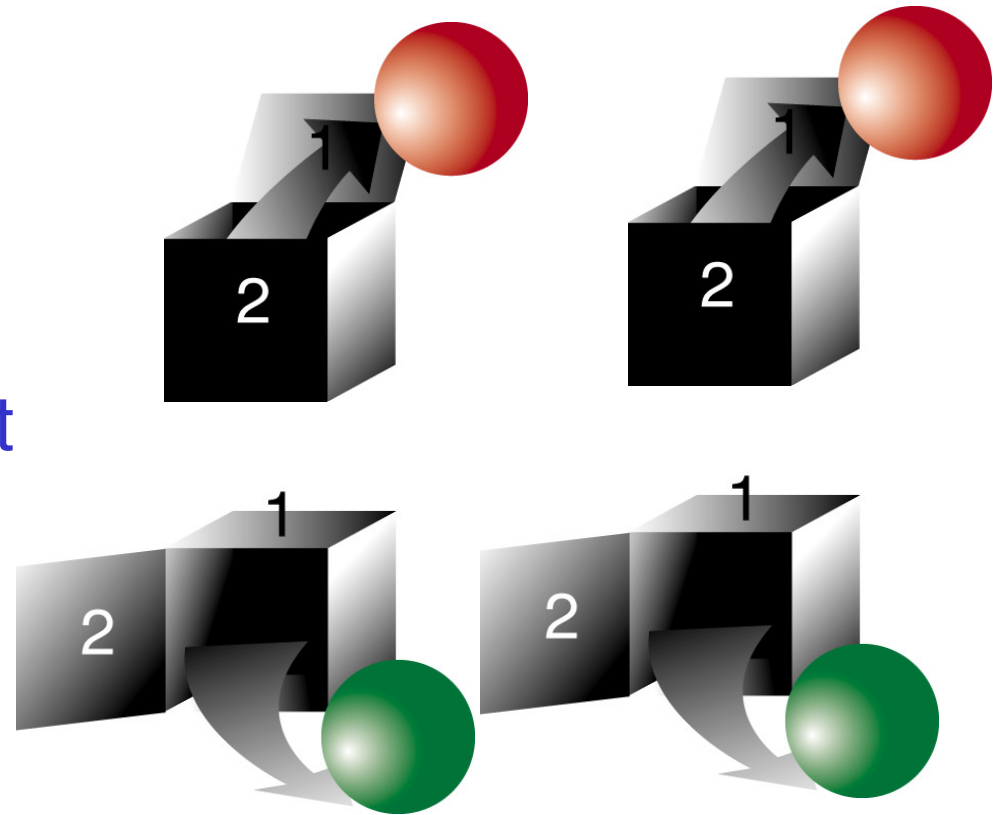
“Another way of expressing the peculiar situation is: **the best possible knowledge of a *whole* does not necessarily include the best possible knowledge of its *parts*** ... I would not call that *one* but rather *the* characteristic trait of quantum mechanics, the one that enforces its entire departure from classical lines of thought...

By the interaction the two representatives [quantum states] have become ***entangled***.”



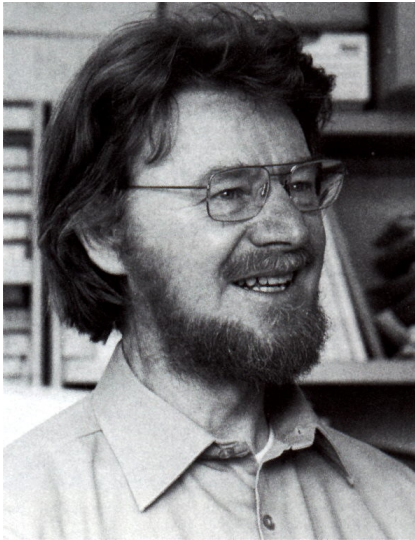
Erwin Schrödinger, *Proceedings of the Cambridge Philosophical Society*, submitted 14 August 1935

“It is rather discomfoting that the theory should allow a system to be steered or piloted into one or the other type of state at the experimenter’s mercy in spite of his having no access to it.”

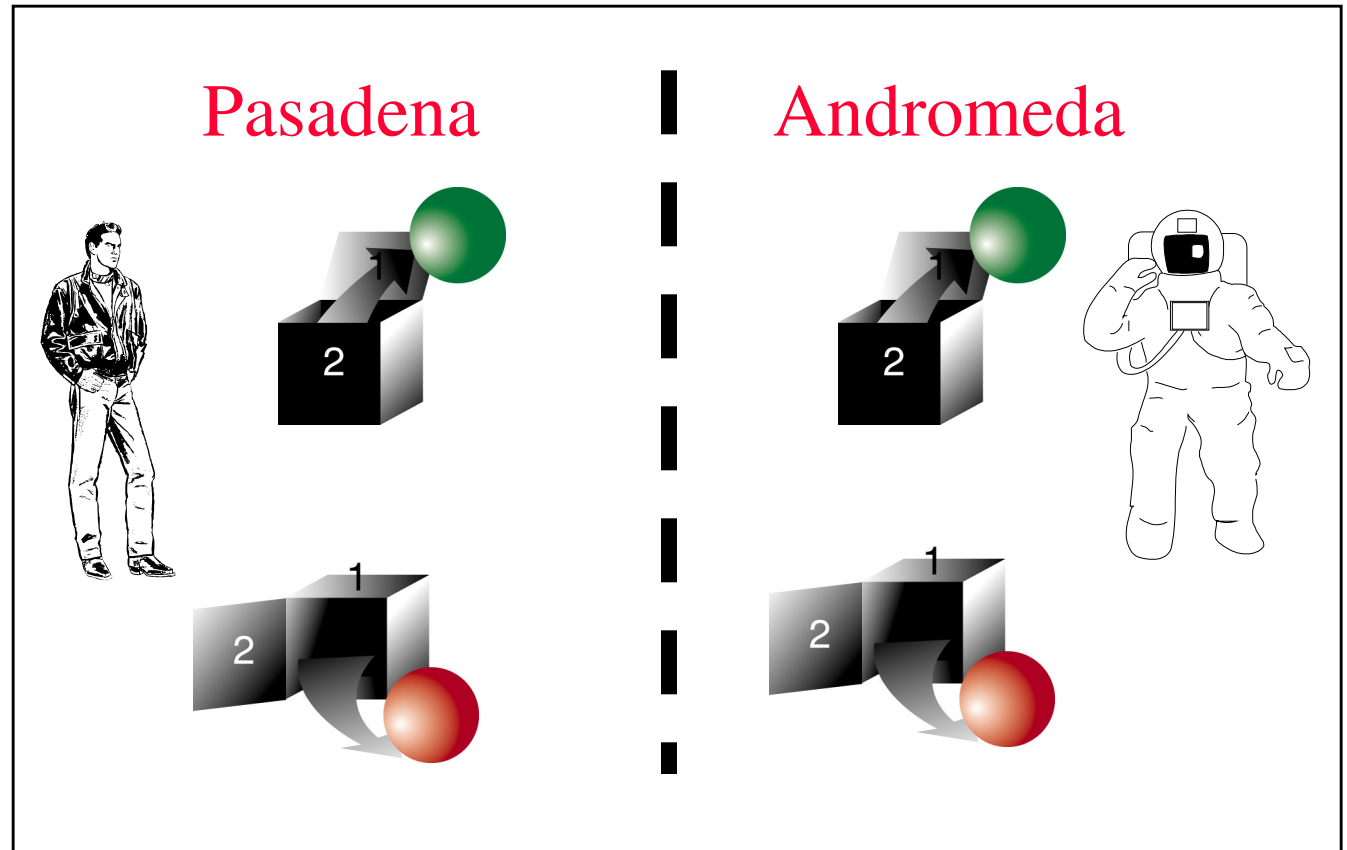


Erwin Schrödinger, *Proceedings of the Cambridge Philosophical Society*, submitted 14 August 1935

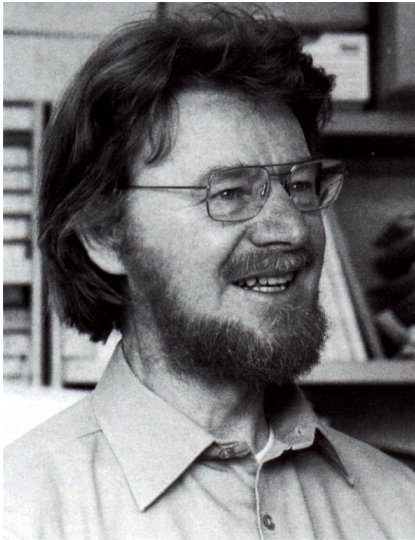
Quantum Entanglement



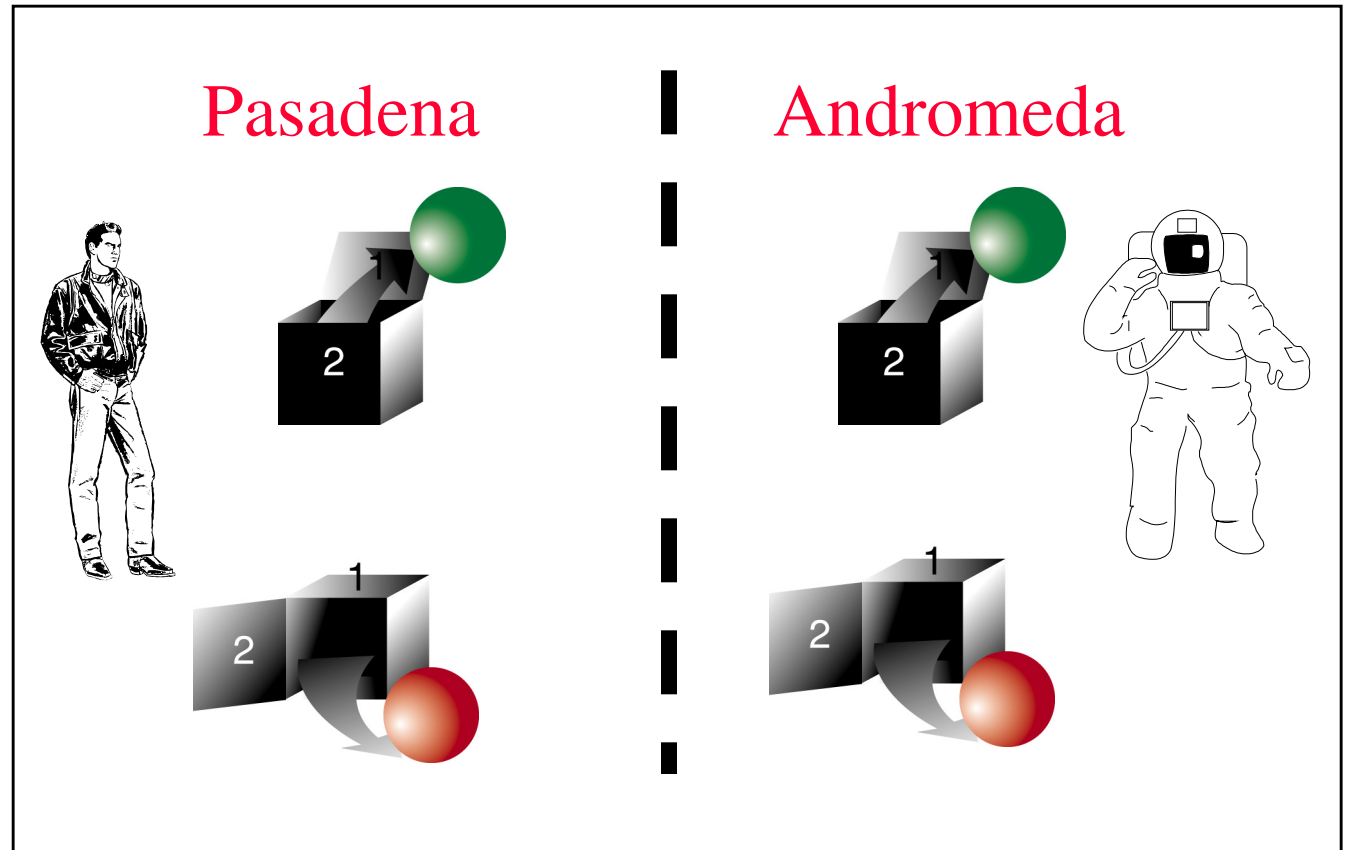
Bell '64



Quantum information can be *nonlocal*;
quantum correlations are a stronger
resource than classical correlations.



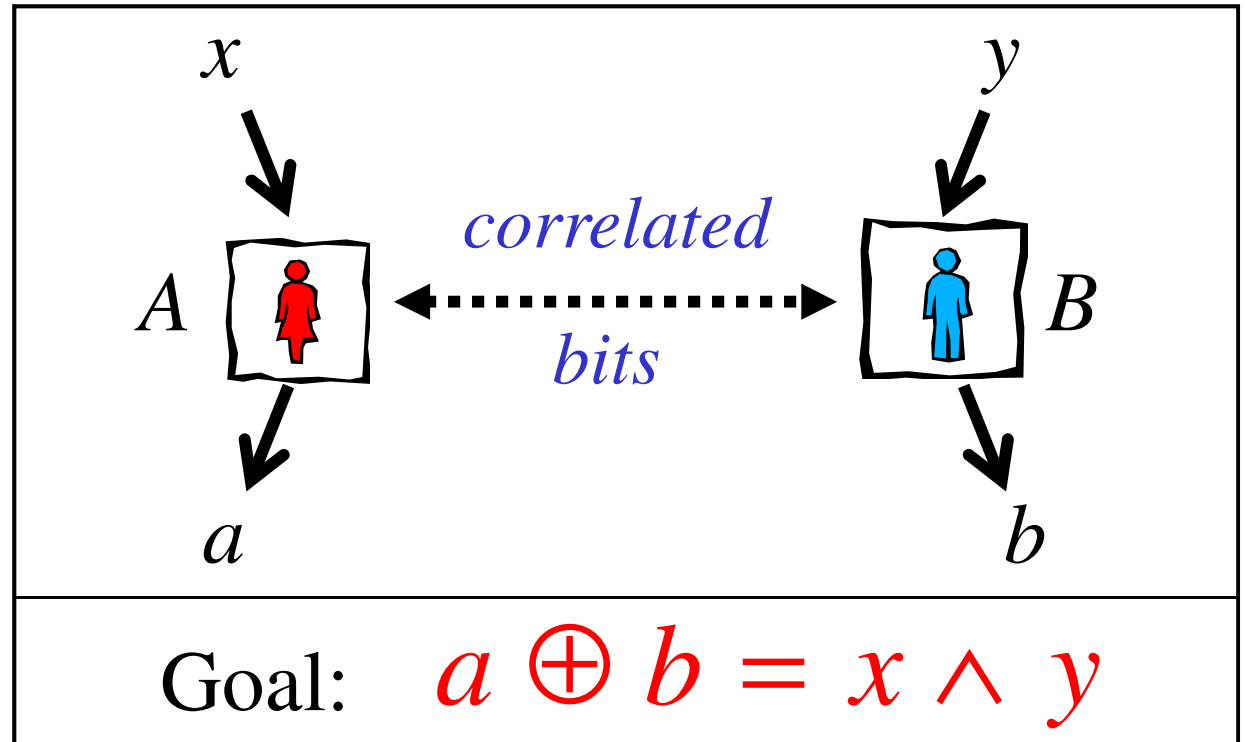
Bell '64



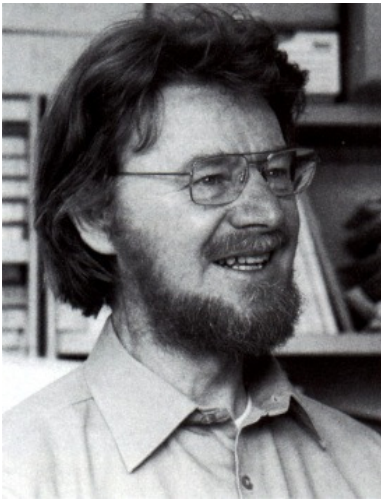
Quantum entanglement



Alice and Bob play a cooperative two-player game.

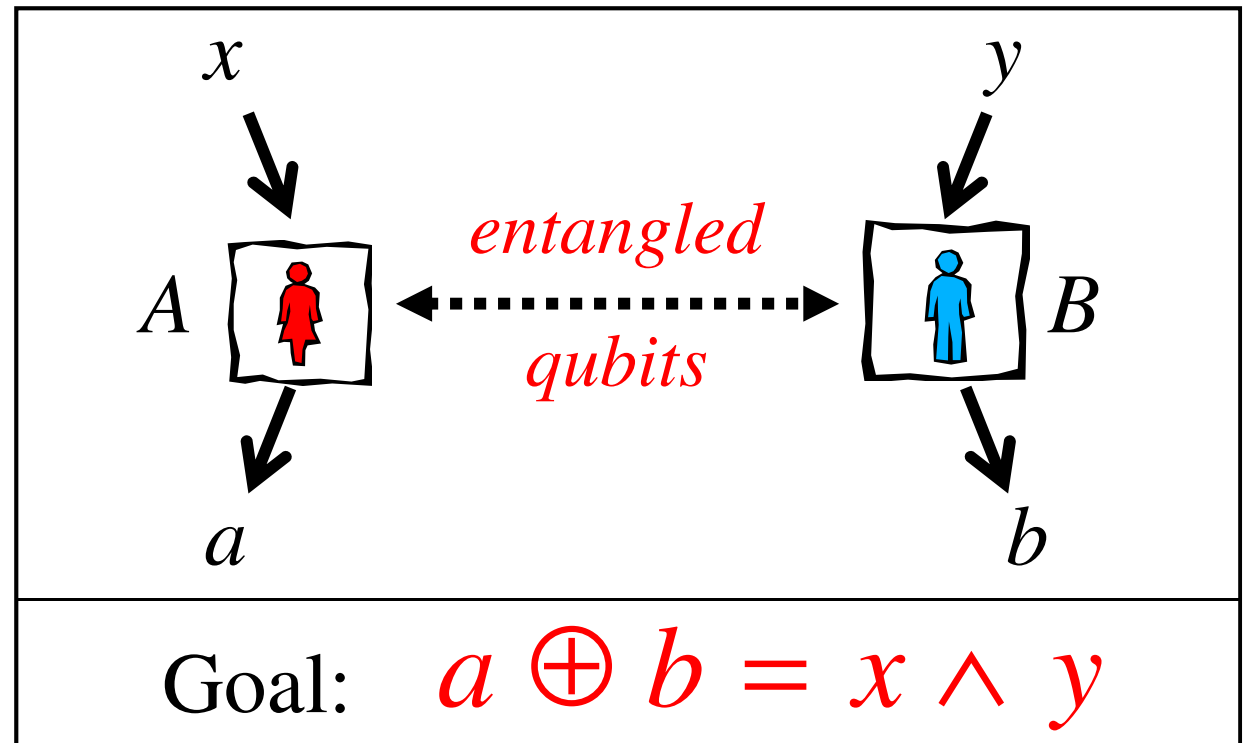


If they share correlated classical bits and play their best strategy, they win with probability 75% (averaged over the inputs they receive).



Quantum entanglement

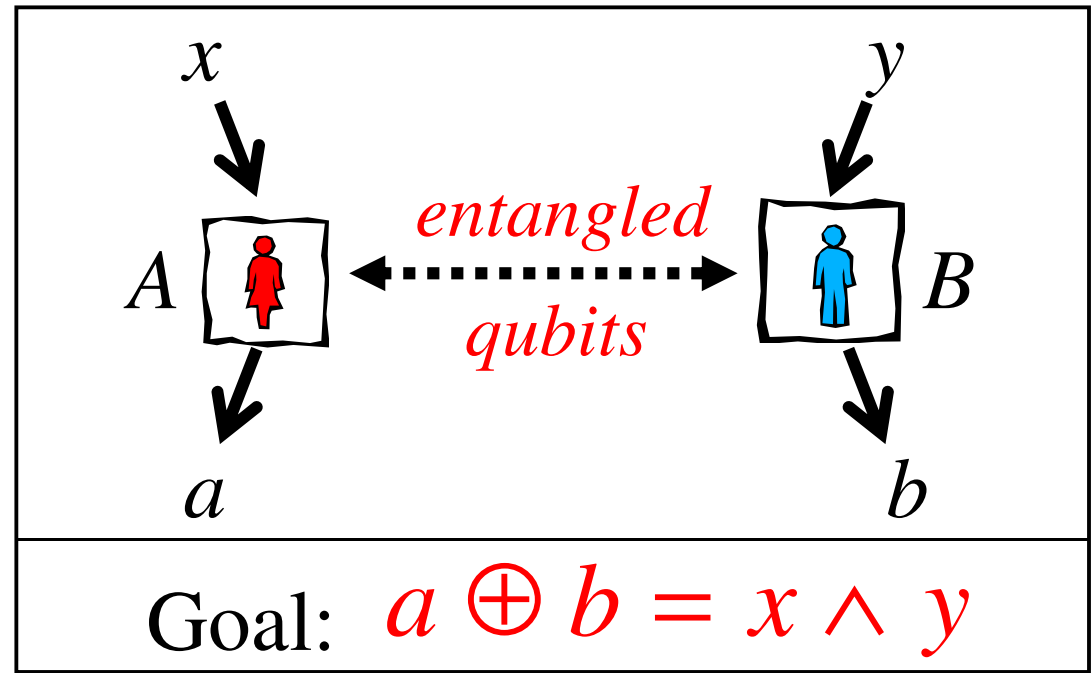
Alice and Bob play a cooperative two-player game.



If they share entangled qubits and play their best strategy, they win with probability 85.4% (averaged over the inputs they receive).

Quantum entanglement

In experimental tests, physicists have played the game and have won with probability above 75%.



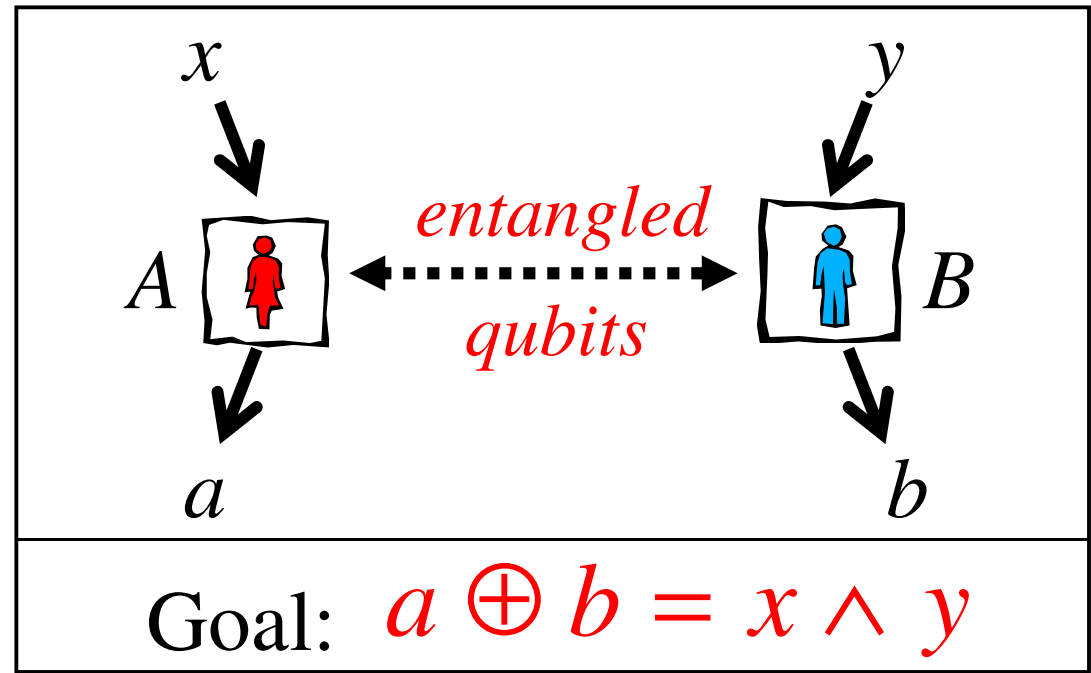
Quantum correlations are a stronger resource than classical correlations.



Aspect

Quantum entanglement

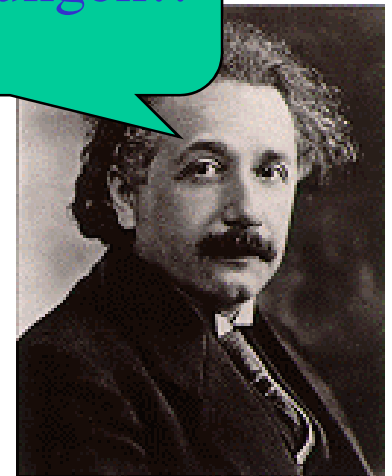
In experimental tests, physicists have played the game and have won with probability above 75%.



Quantum correlations are a stronger resource than classical correlations.

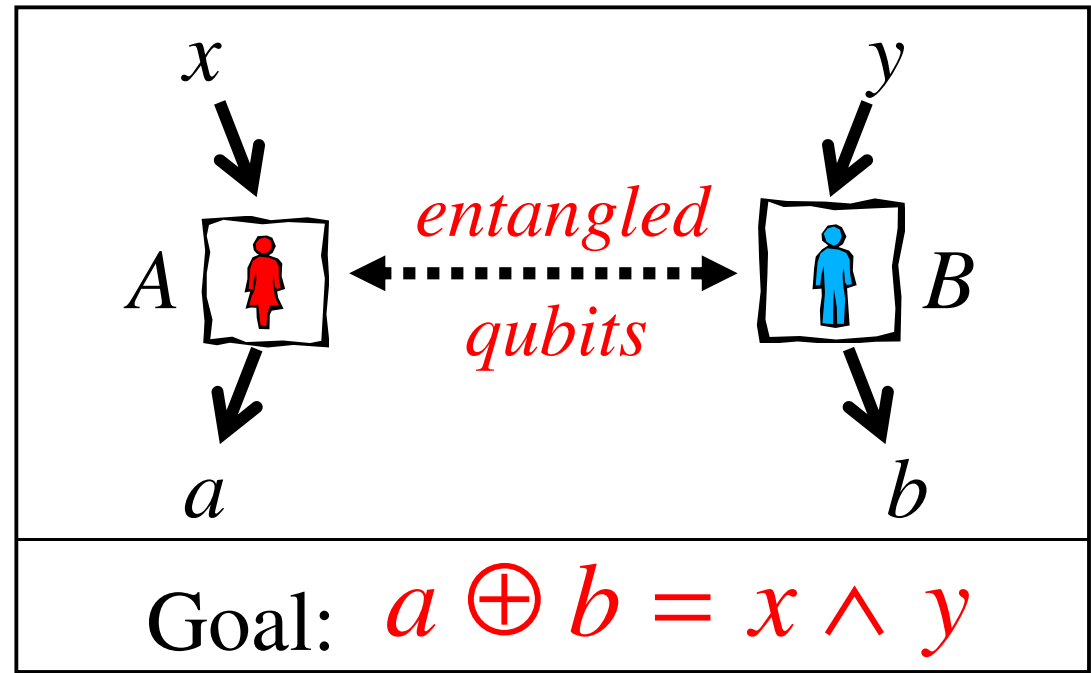
Spukhafte Fernwirkungen!!*

* Spooky action at a distance!!

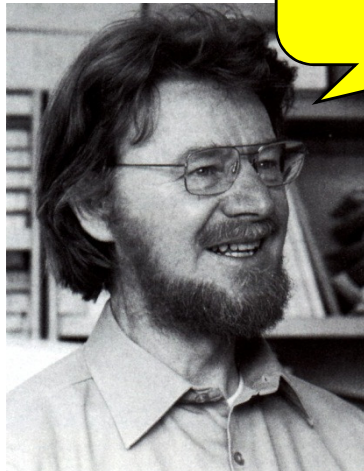


Quantum entanglement

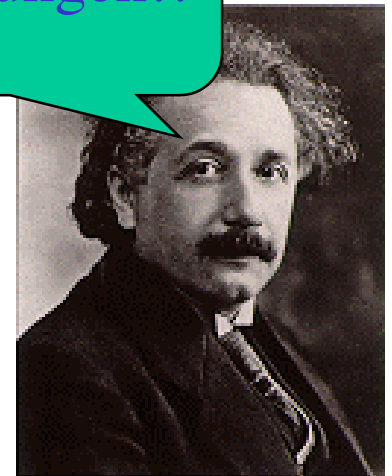
In experimental tests, physicists have played the game and have won with probability above 75%.



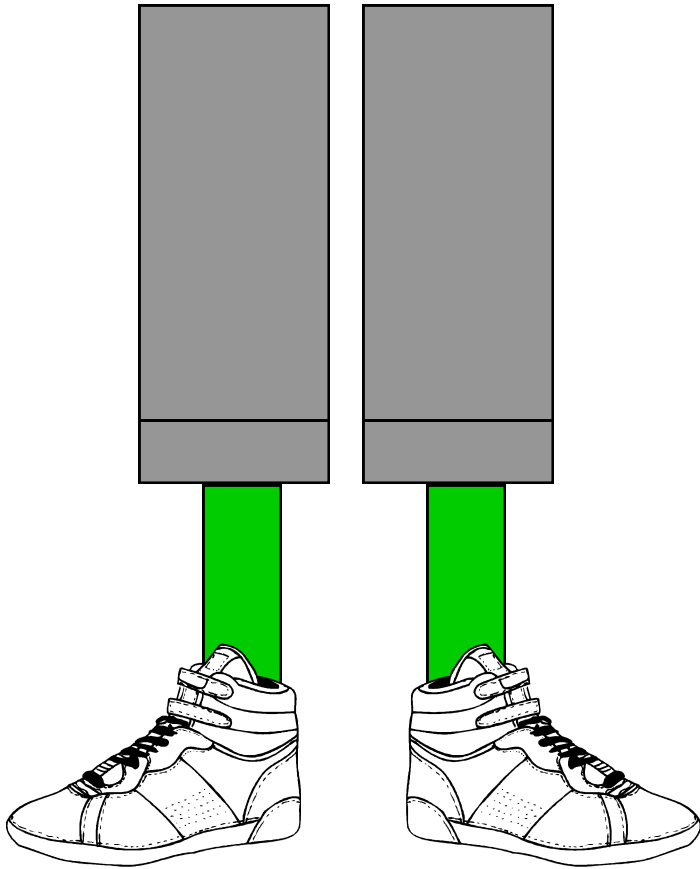
Sorry, Al . . .



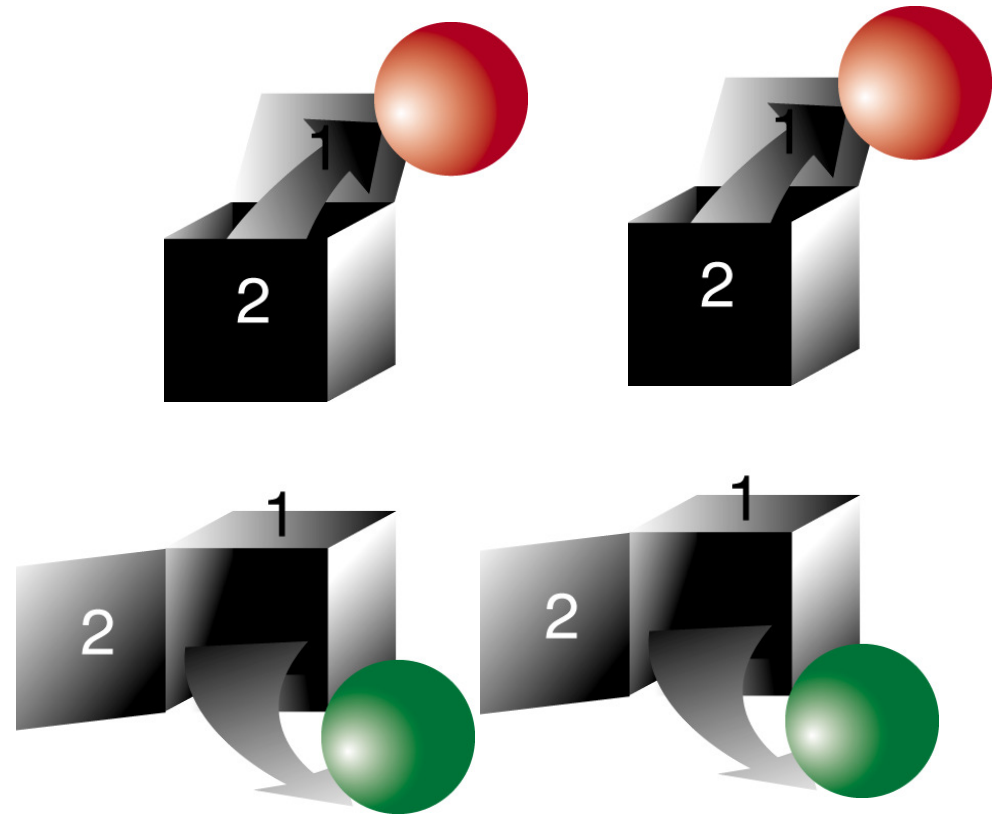
Spukhafte Fernwirkungen!!*



* Spooky action at a distance!!



Classical Correlations



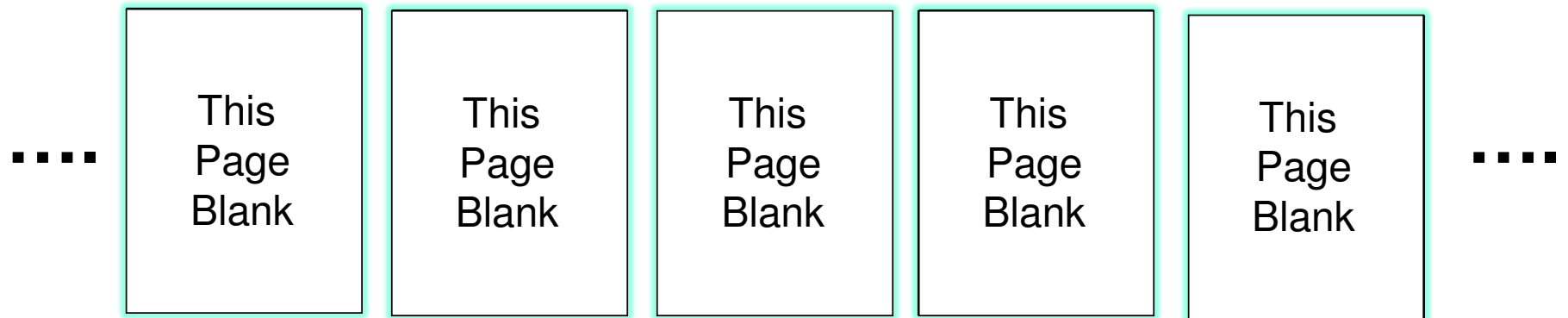
Quantum Correlations

Boxes are not like soxes!

Quantum information vs. Classical information

- 1) **Randomness.** Clicks in a Geiger counter are intrinsically random, not pseudorandom. Can't predict outcome even with the most complete possible knowledge of the state.
- 2) **Uncertainty.** Operators A and B do not commute means that measuring A influences the outcome of a subsequent measurement of B .
- 3) **Entanglement.** The whole is more definite than the parts. Even if we have the complete possible knowledge of the (pure) state of joint system AB , the (mixed) state of A may be highly uncertain.

Quantum entanglement



Nearly all the information in a typical entangled “quantum book” is encoded in the correlations among the “pages”.

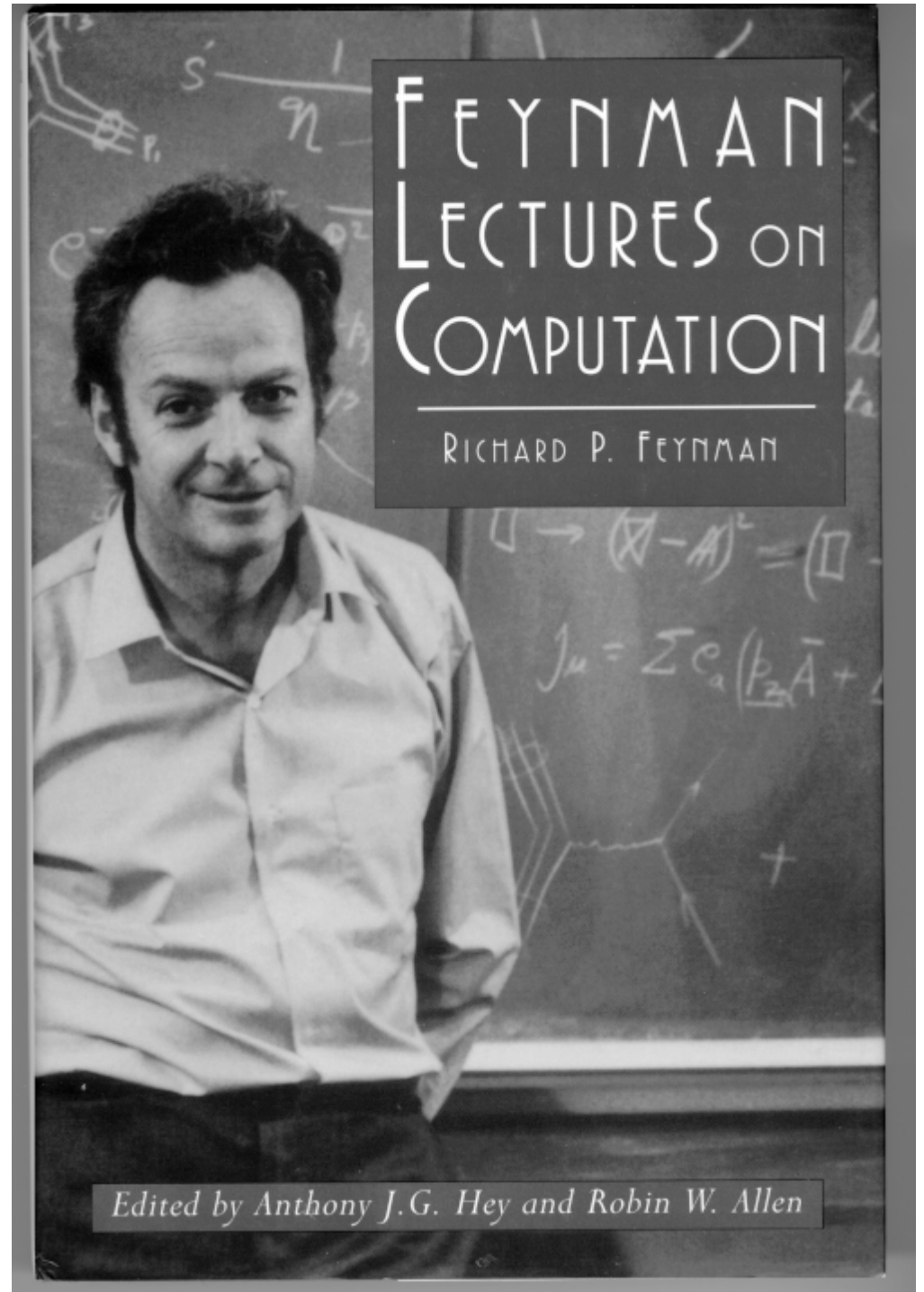
You can't access the information if you read the book one page at a time.



To describe **300** qubits, we would need more numbers than the number of atoms in the visible universe!

We can't even hope to *describe* the state of a few hundred qubits in terms of classical bits.

Might a computer that operates on qubits rather than bits (a *quantum computer*) be able to perform tasks that are beyond the capability of any conceivable classical computer?





Peter
Shor

Finding Prime Factors

1807082088687
4048059516561
6440590556627
8102516769401
3491701270214
5005666254024
4048387341127
5908123033717
8188796656318
2013214880557

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Finding Prime Factors

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3968599945959
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4832555157243

×

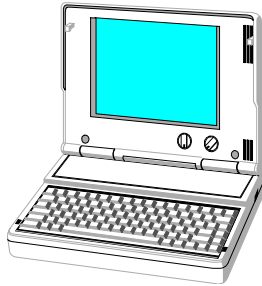
4553449864673
5972188403686
8972744088643
5630126320506
9600999044599

The boundary between
“hard” and “easy” seems to be
different in a quantum world
than in a classical world.

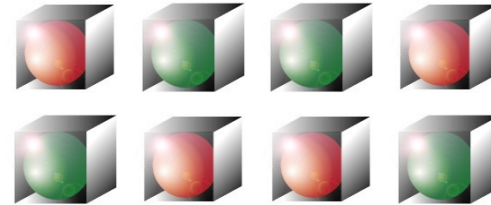


Shor

Classical Computer



Quantum Computer



Factor 193 digits
in 30 CPU years (2.2 GHz).

Factor 193 digits
in 0.1 second.

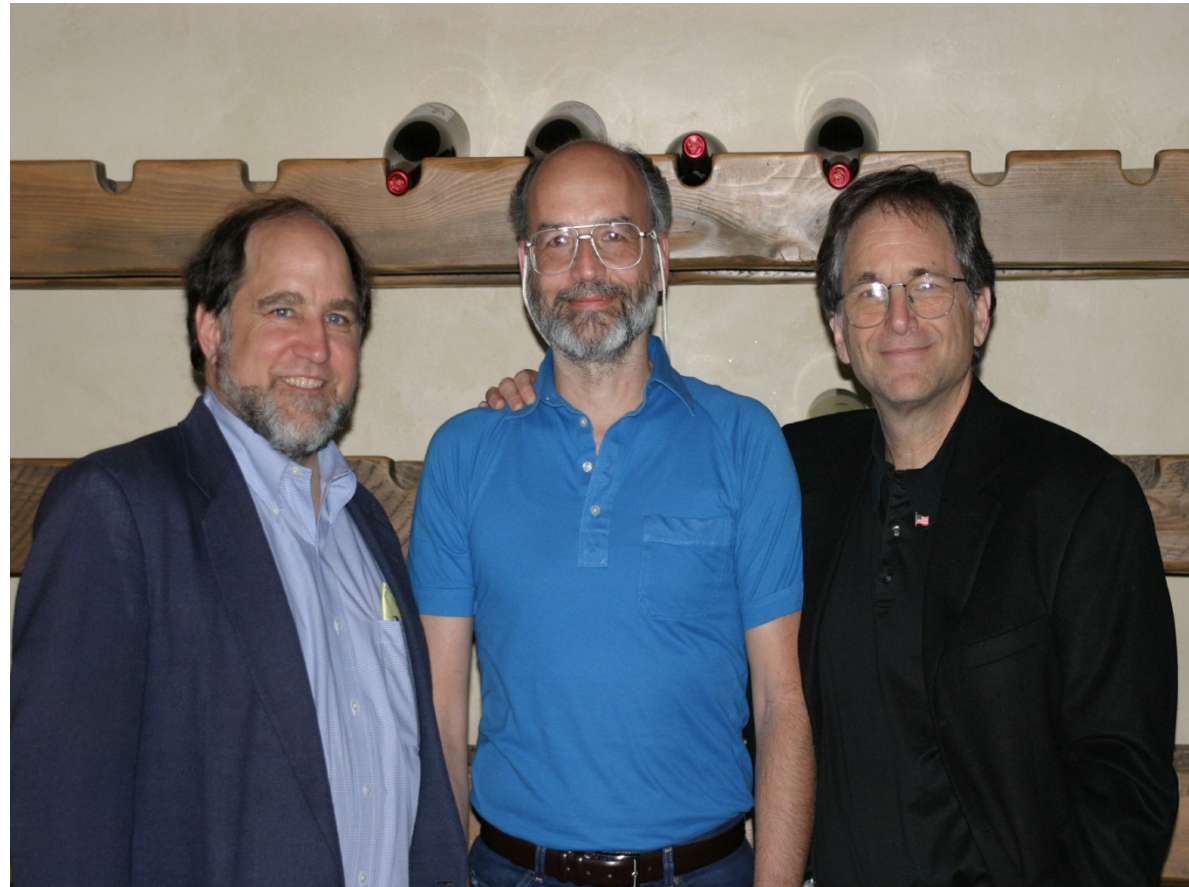
Factor 500 digits
in 10^{12} CPU years.

Factor 500 digits
in 2 seconds.

MITOSION:
IMPOSSIBLE



Peter Shor

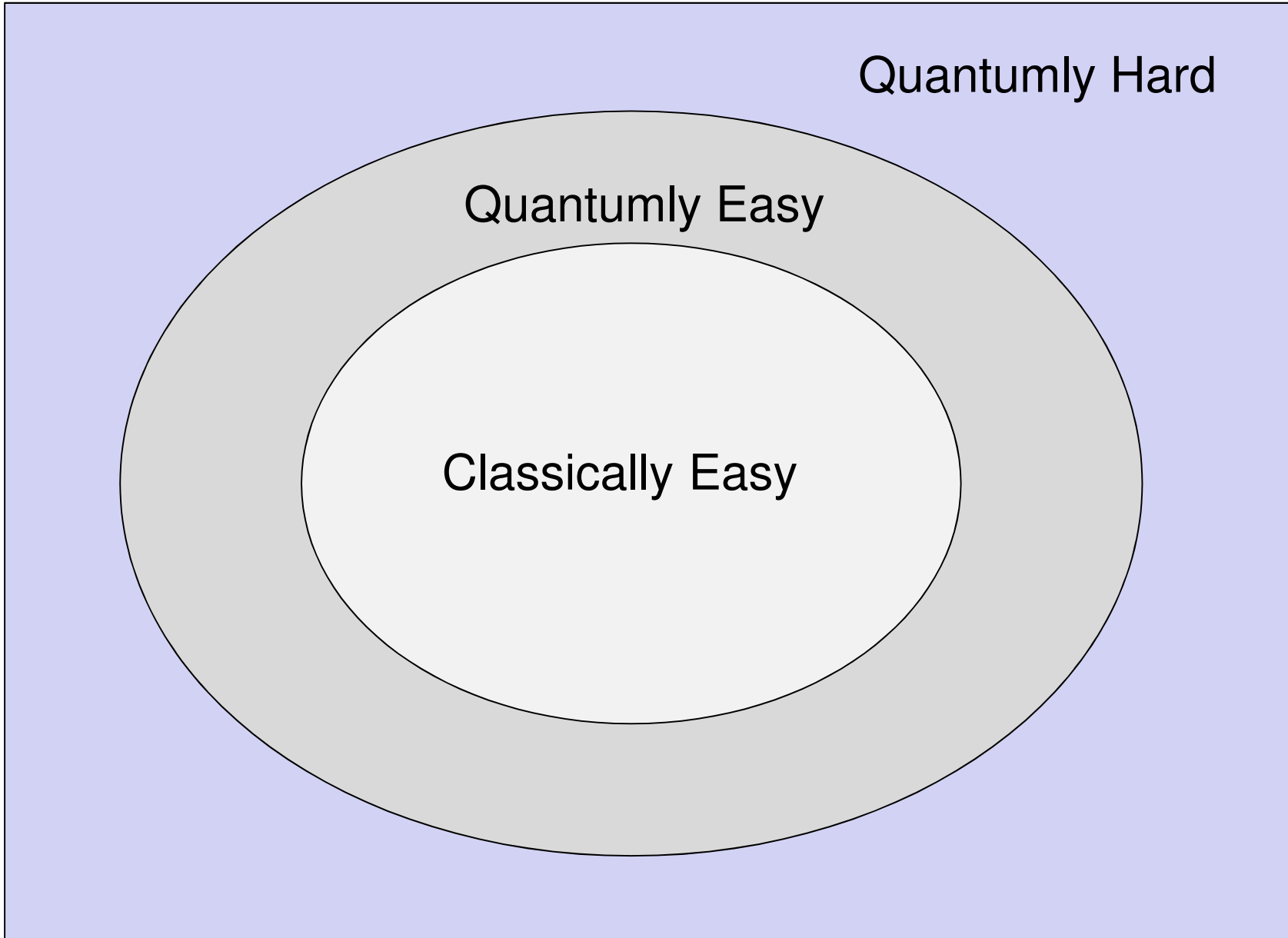


Ron Rivest

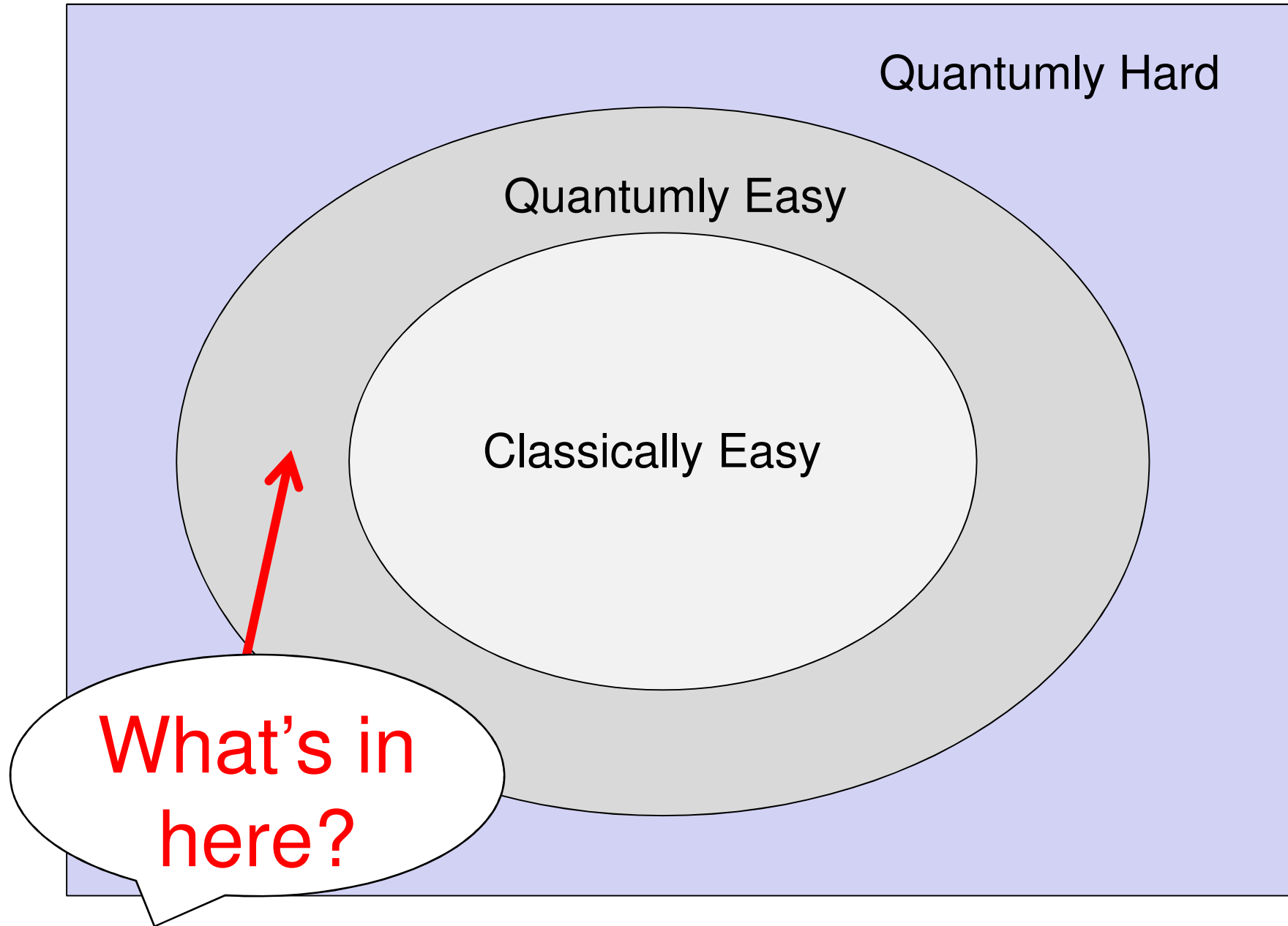
Adi Shamir

Len Adleman

Problems



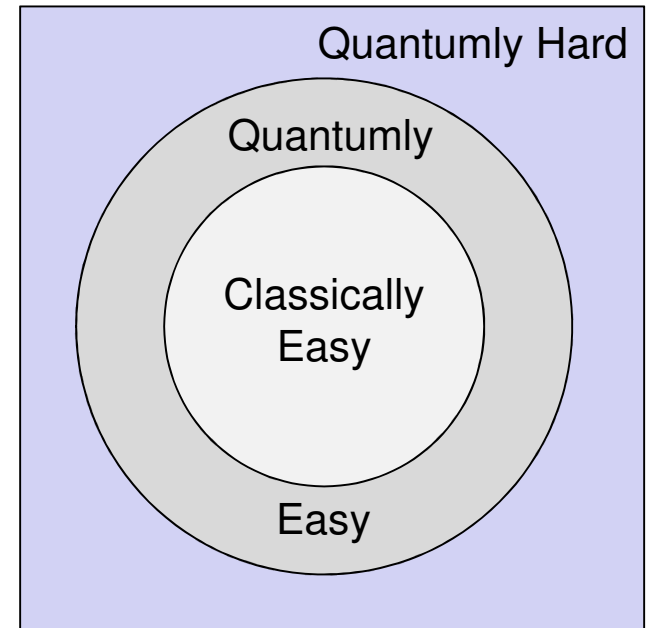
Problems



Quantum algorithms

Quantum computers have limitations:

Spectacular quantum speedups seem to be possible only for problems with special structure, *not* for NP-complete problems like 3-SAT. (Quantum physics speeds up unstructured search quadratically, not exponentially.)



Beyond NP: Speedups for problems *outside* NP are also common and important. Indeed the “natural” application for a quantum computer is simulating time evolution of quantum systems, e.g. collisions in molecular chemistry or quantum field theory.

Many more quantum algorithms at math.nist.gov/quantum/zoo/

Quantum algorithms for quantum field theories



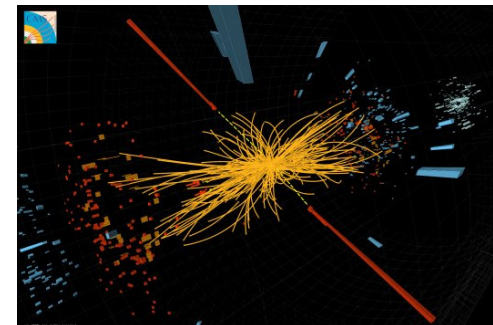
Classical methods have limited precision, particularly at strong coupling.

A quantum computer can simulate particle collisions, even at high energy and strong coupling, using resources (number of qubits and gates) scaling polynomially with precision, energy, and number of particles.

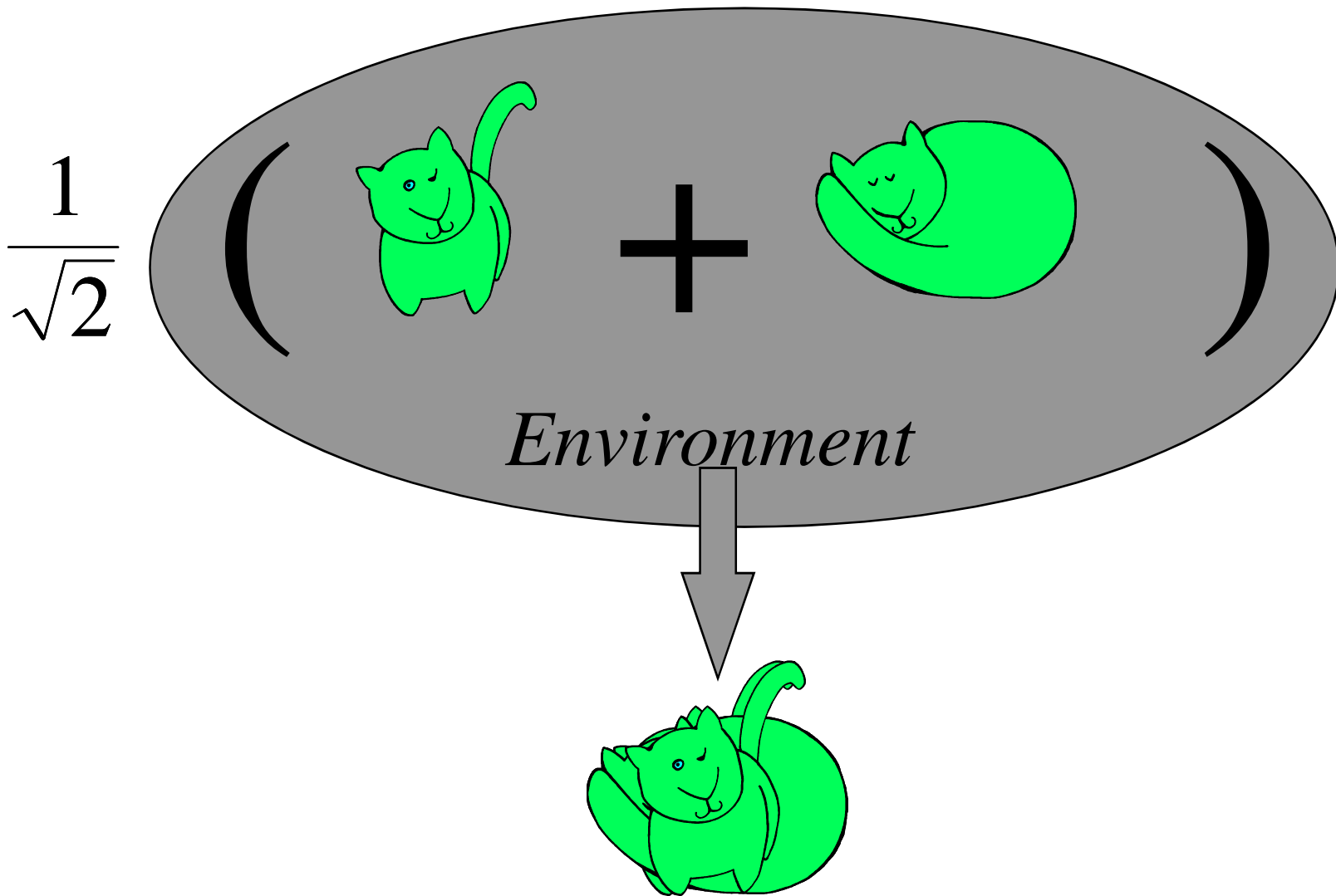
Does the quantum circuit model capture the computational power of Nature?

What about quantum gravity?

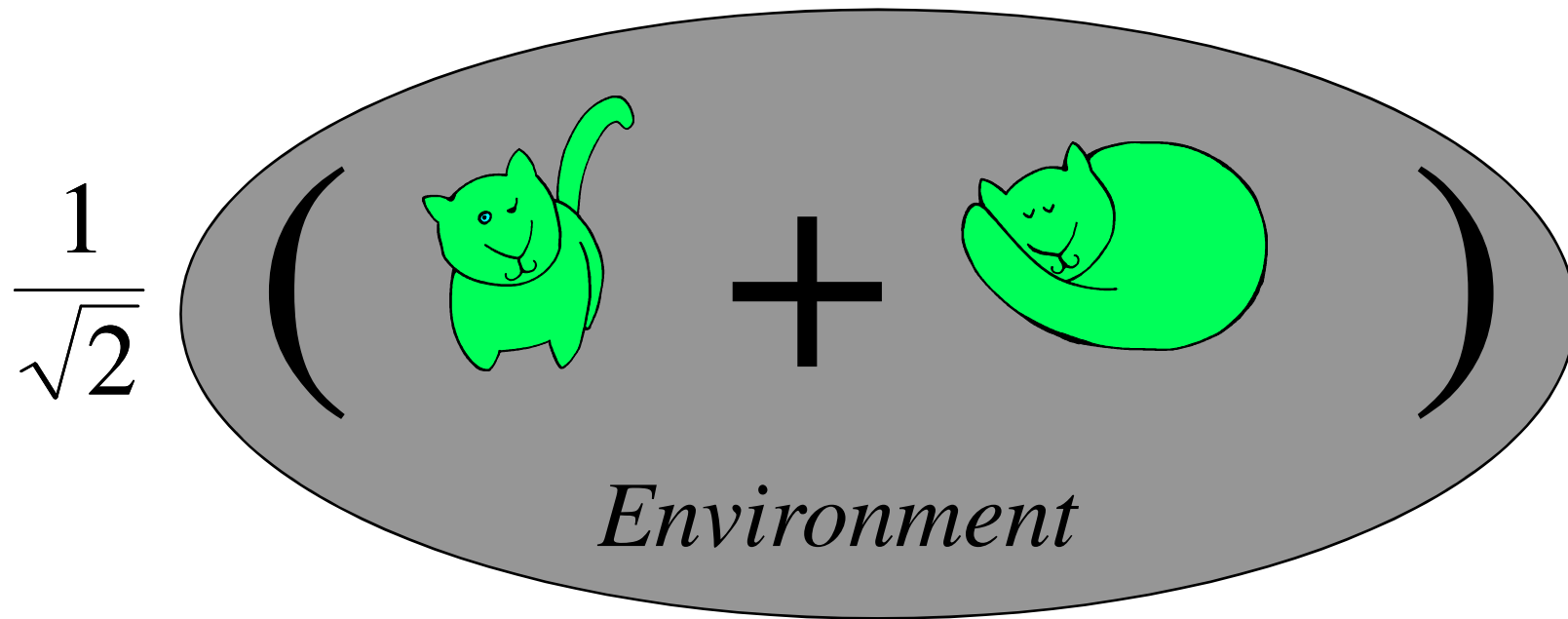
Jordan, Lee, Preskill (2012)



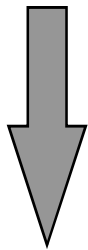
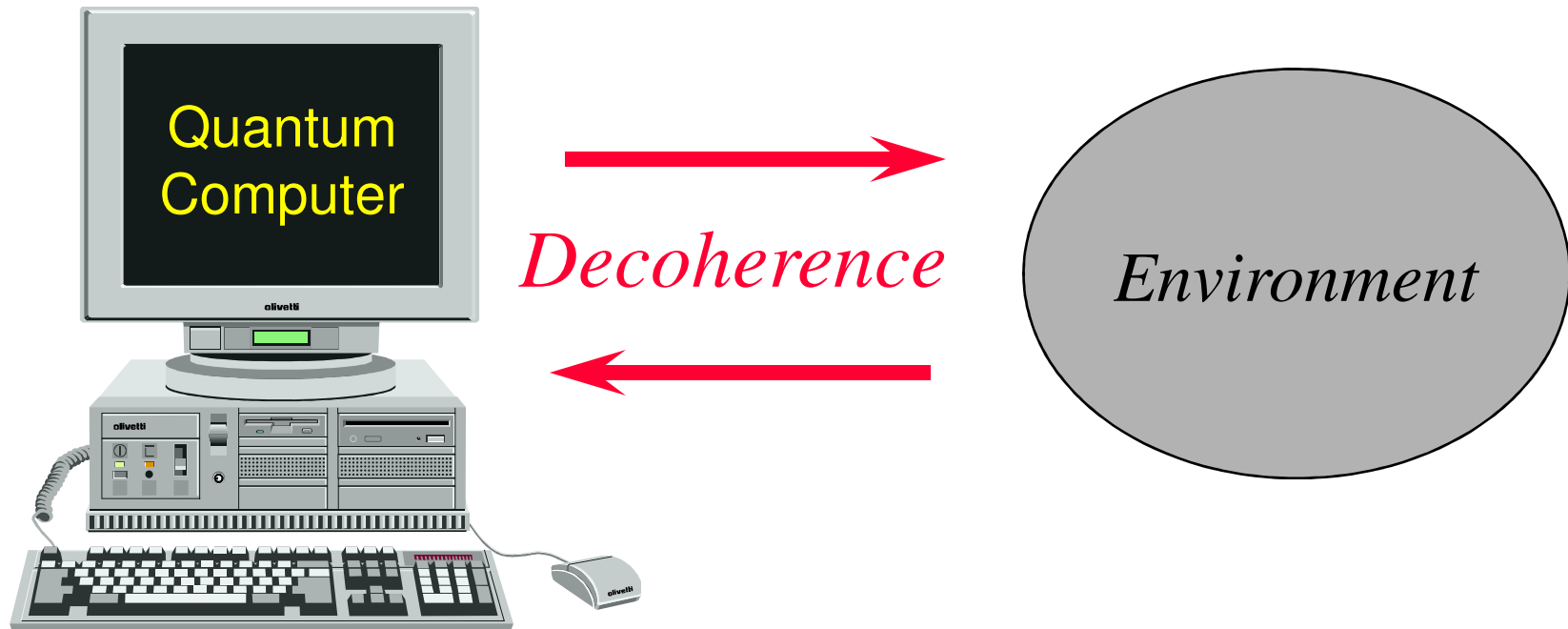
Decoherence



Decoherence



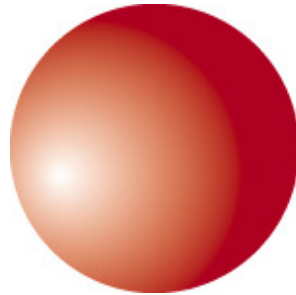
Decoherence explains why quantum phenomena, though observable in the microscopic systems studied in the physics lab, are not manifest in the macroscopic physical systems that we encounter in our ordinary experience.



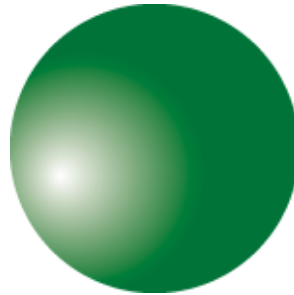
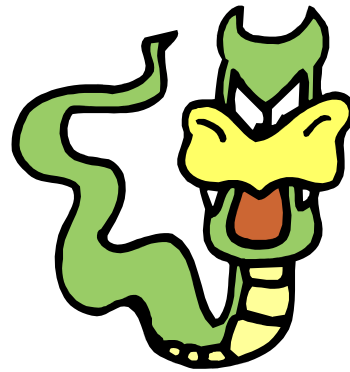
ERROR!

How can we protect a quantum computer from decoherence and other sources of error?

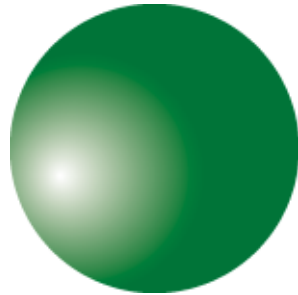
What about errors?



What about errors?

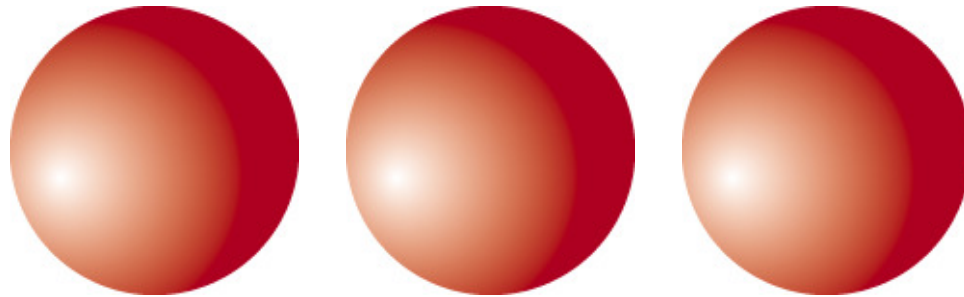
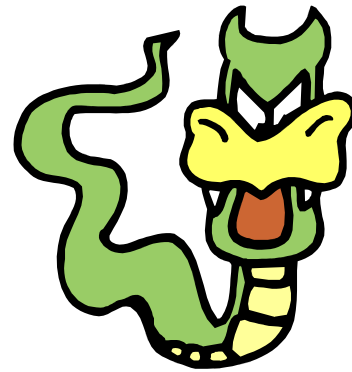


What about errors?

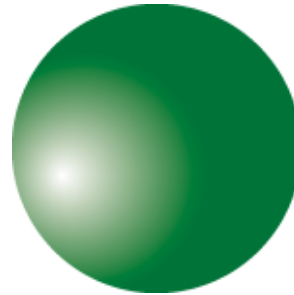
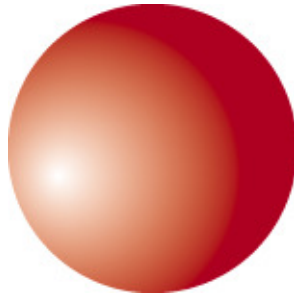
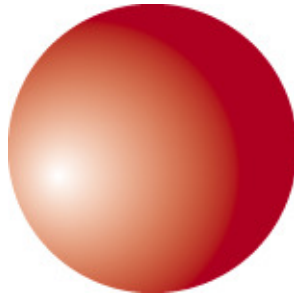
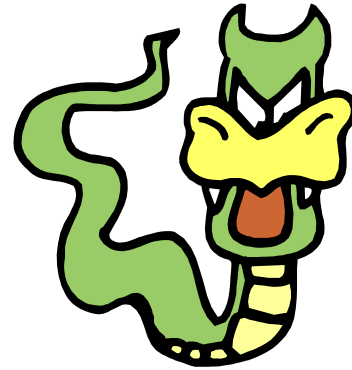


Error!

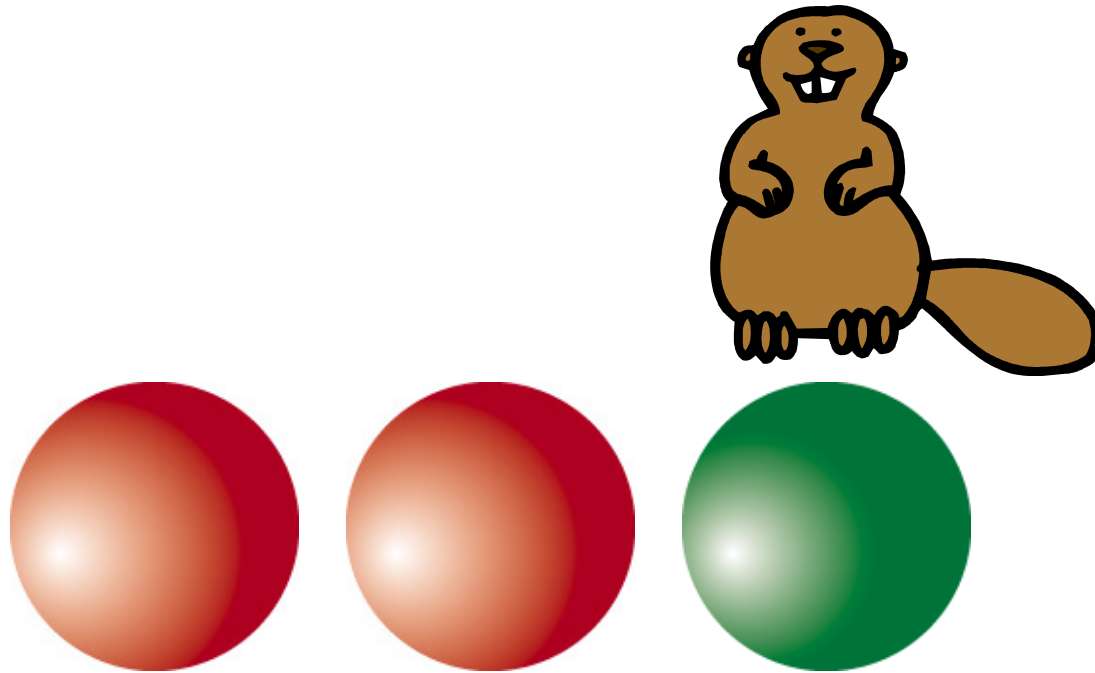
What about errors?



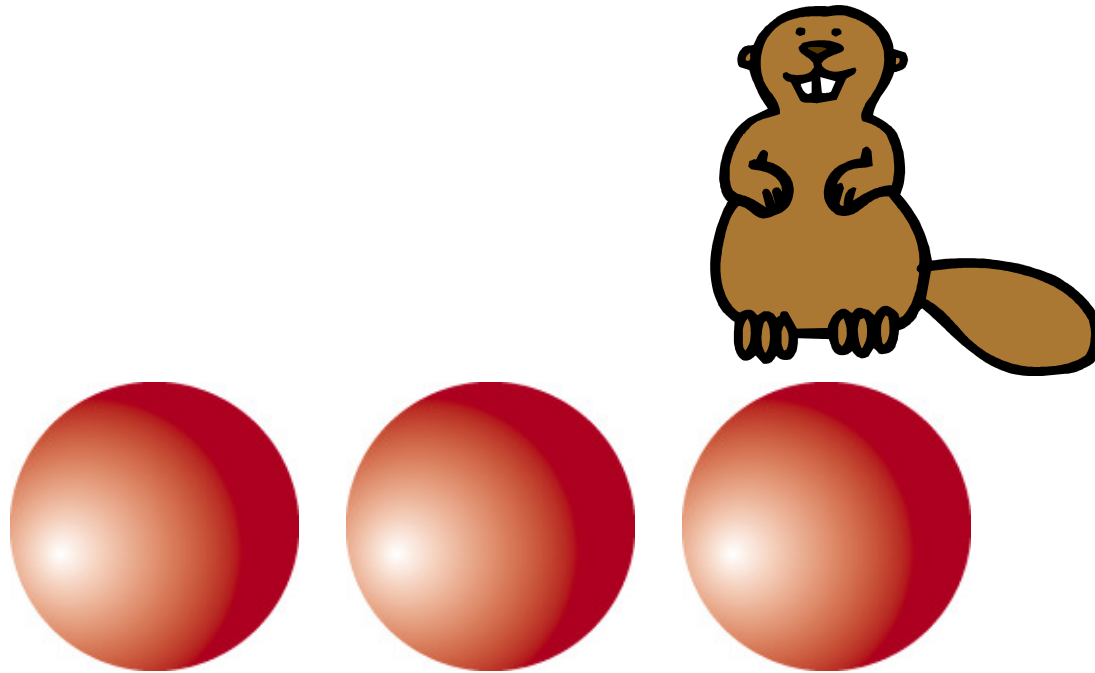
What about errors?



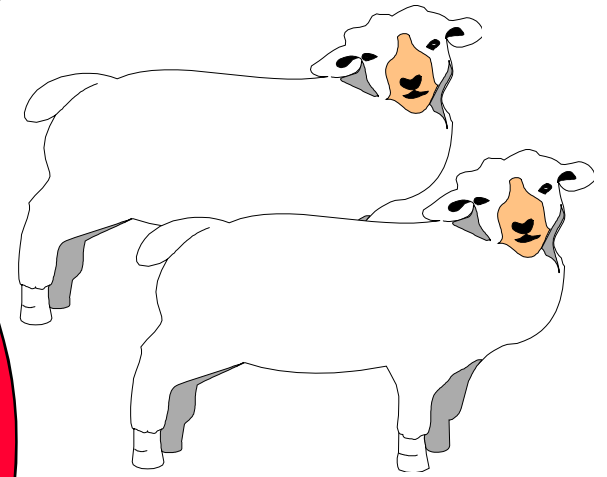
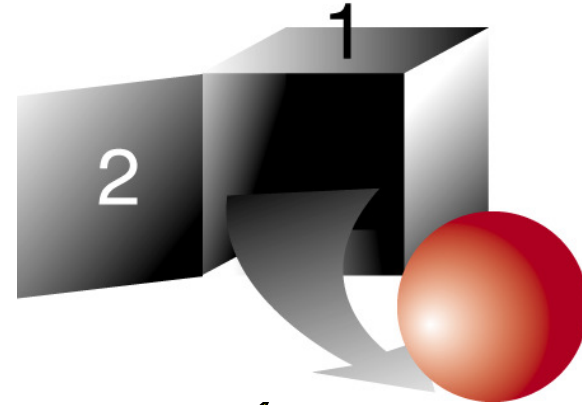
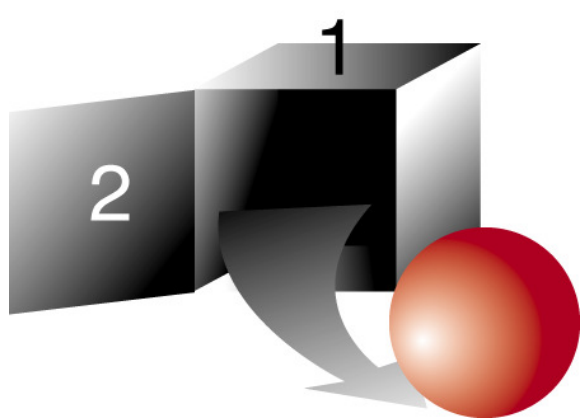
What about errors?



What about errors?

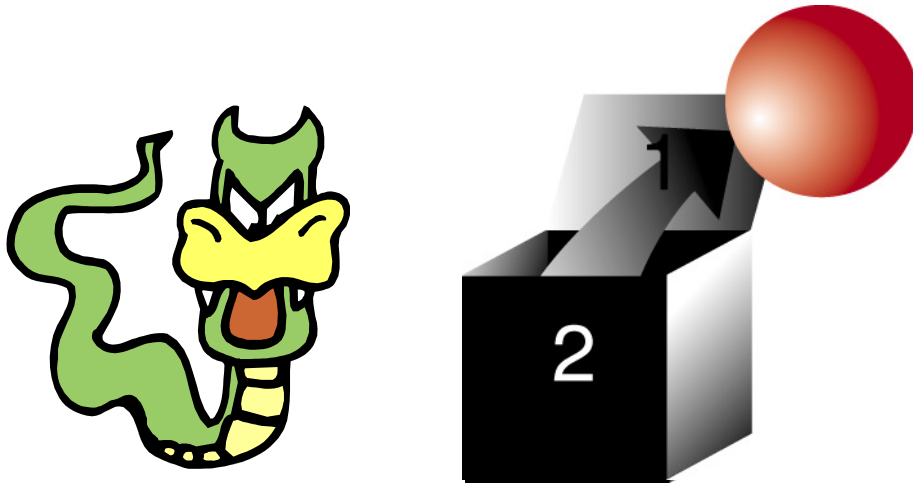


Redundancy protects against errors.

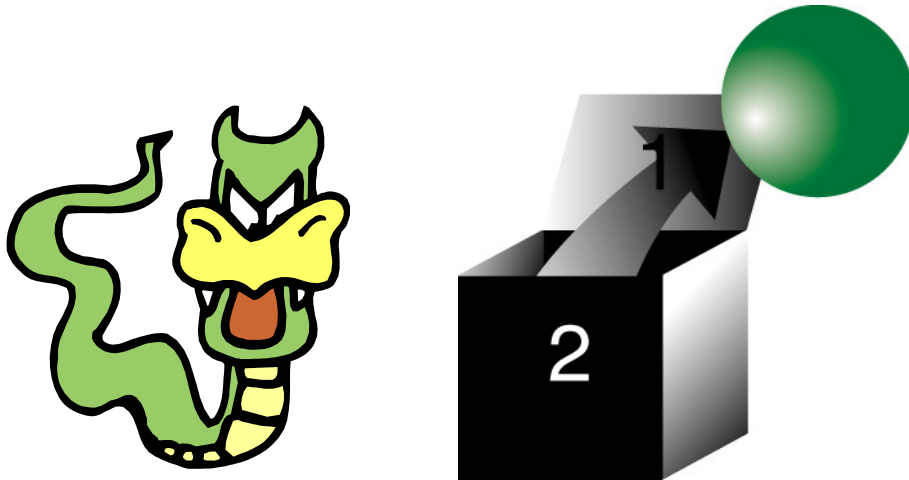


No cloning!

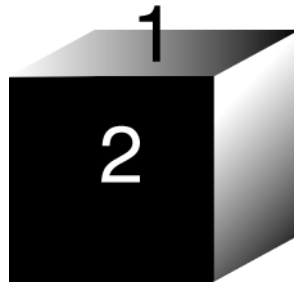
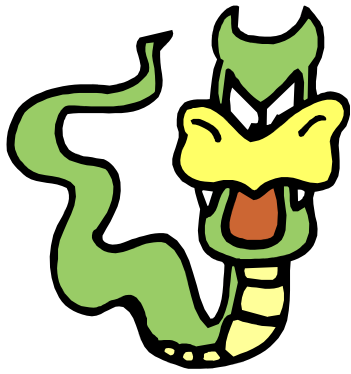
What about *quantum* errors?



What about *quantum* errors?

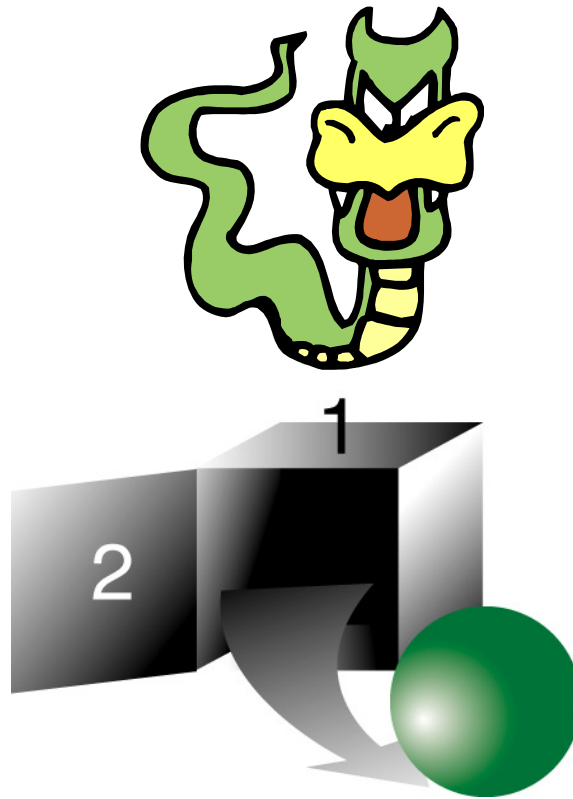


What about *quantum* errors?

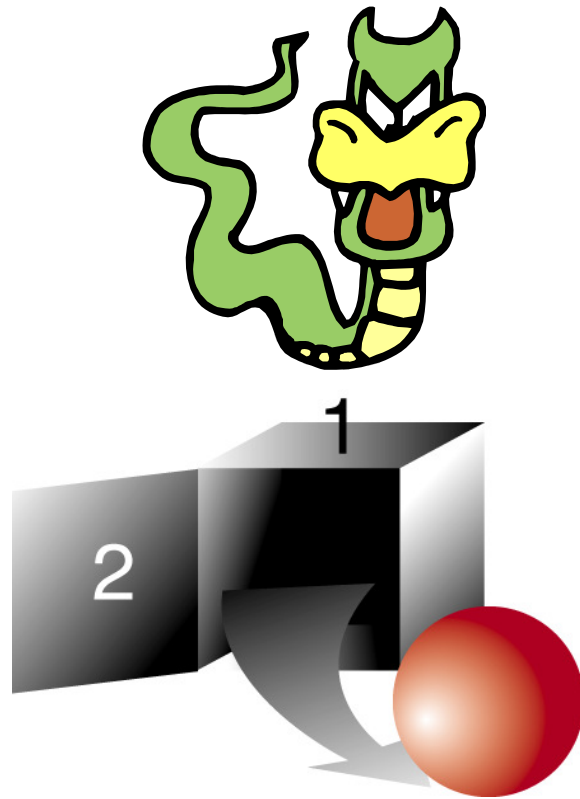


Error!

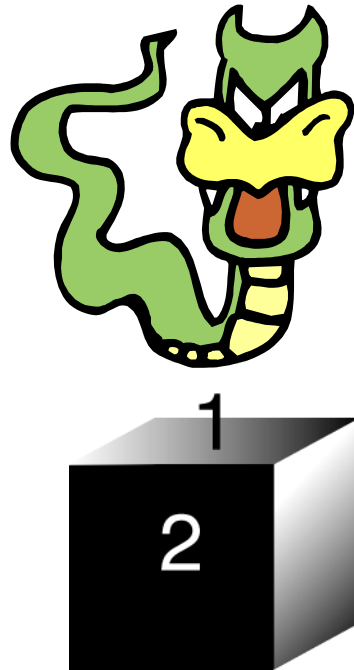
What about *quantum* errors?



What about *quantum* errors?

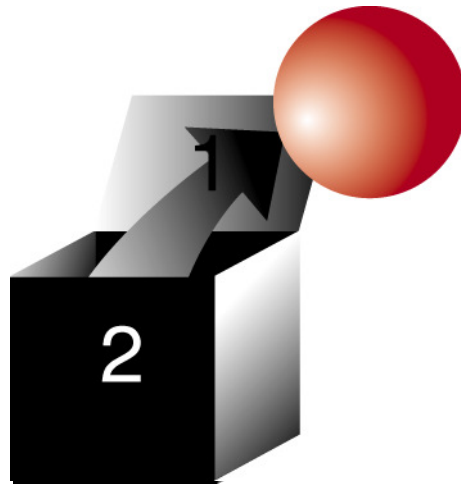
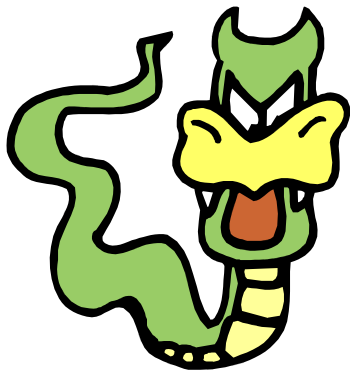


What about *quantum* errors?

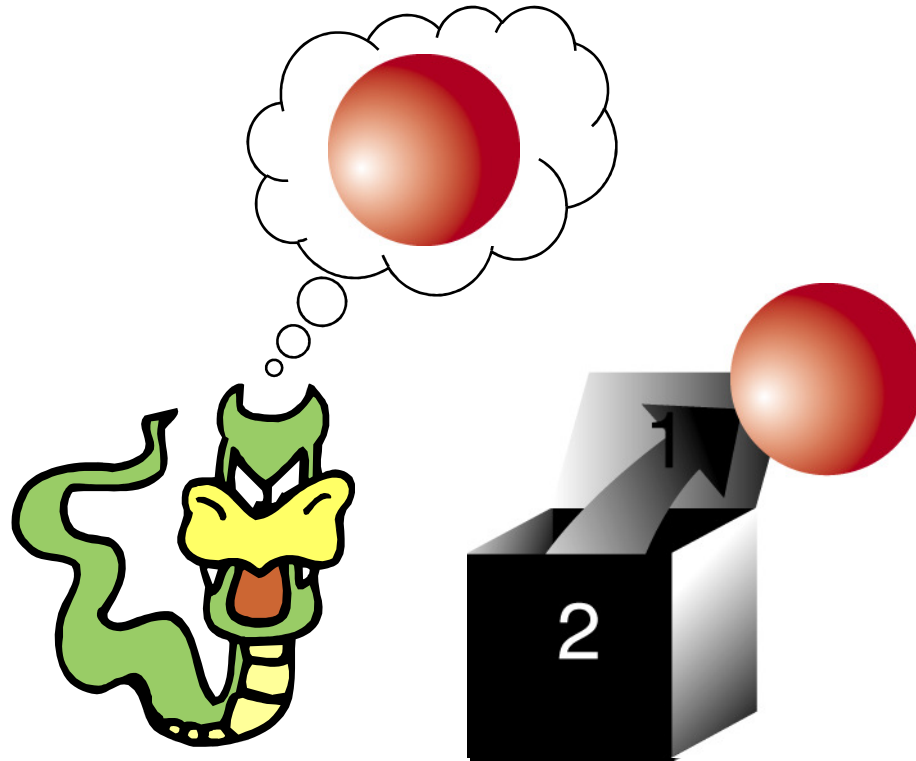


To fix the errors, must we know
what door the dragon opened?
Error!

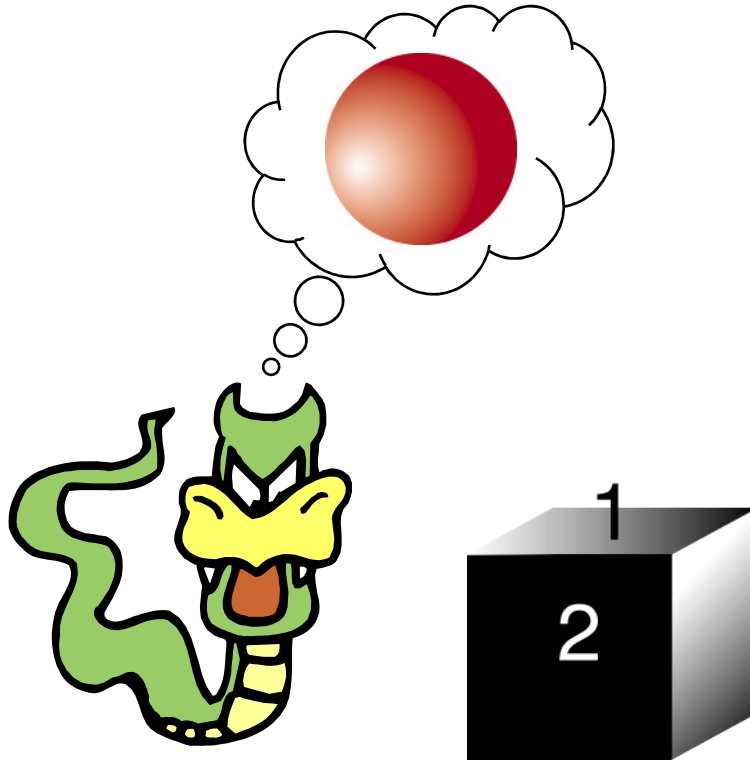
What about *quantum* errors?



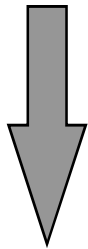
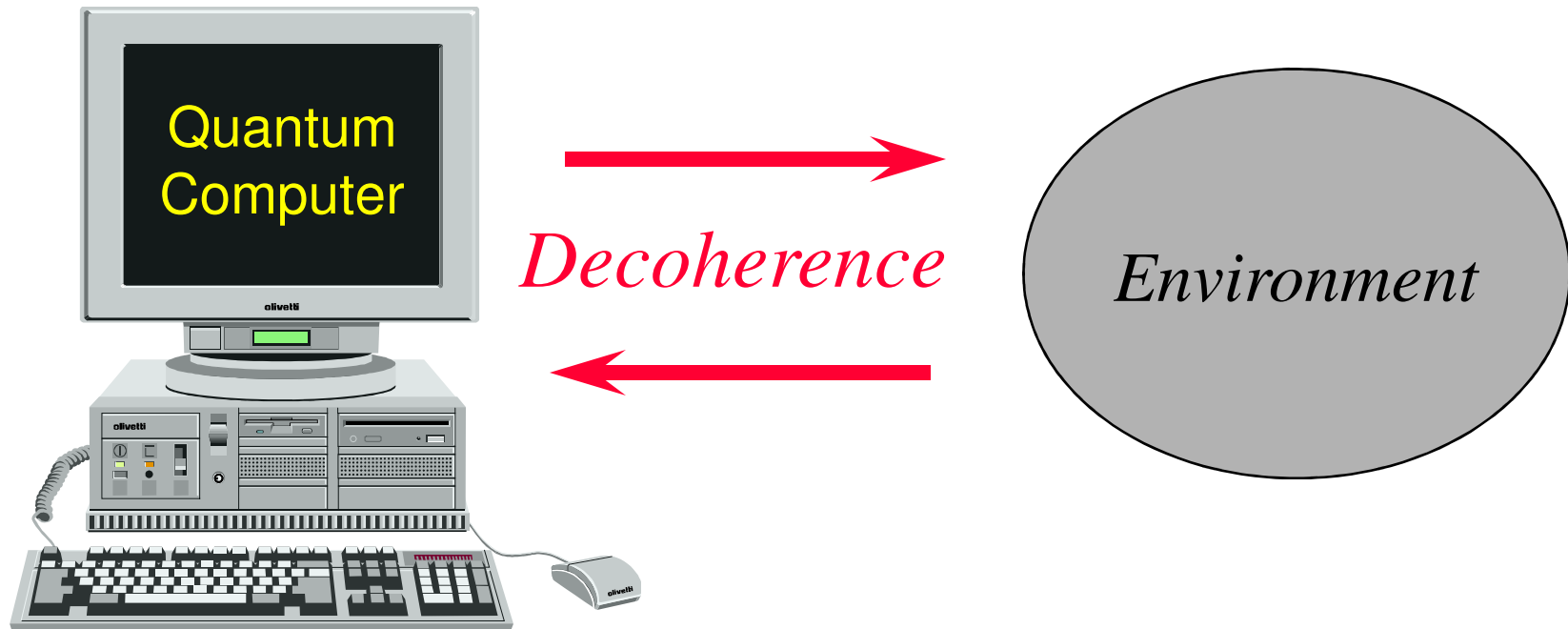
What about *quantum* errors?



What about *quantum* errors?

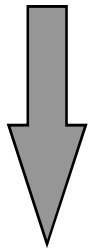
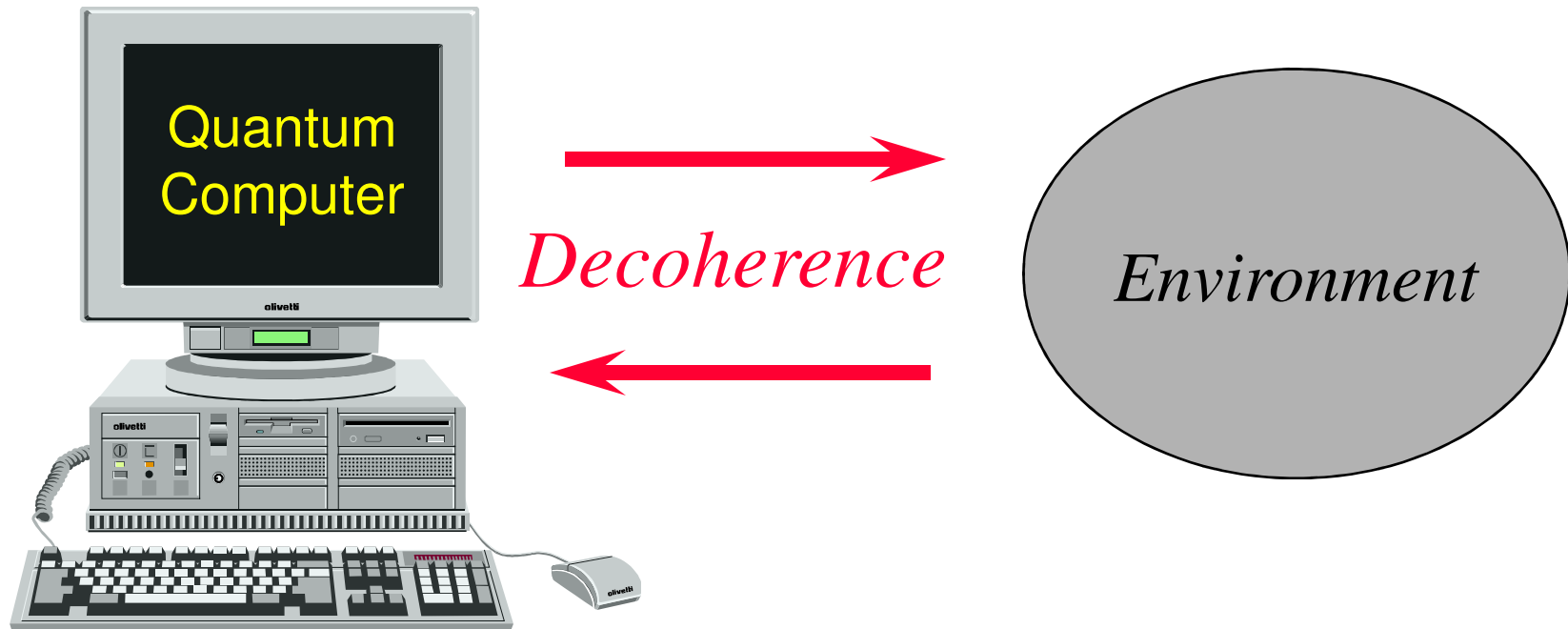


A door-number-2 error (“phase error”) occurs if the dragon remembers (i.e., copies) the color that he sees through door number 1. It is easier to remember a bit than to flip a bit; therefore, phase errors are particularly pervasive.



ERROR!

To resist decoherence, we must prevent the environment from “learning” about the state of the quantum computer during the computation.

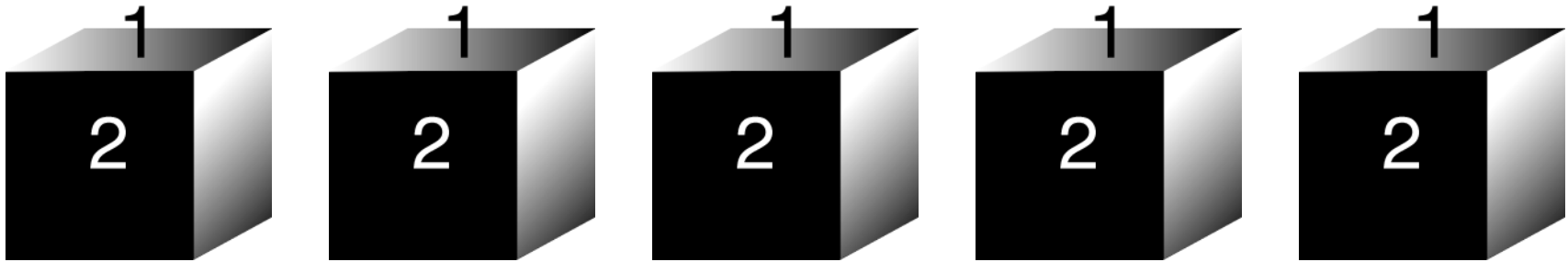


ERROR!

If a quantum computation works, and you ask the quantum computer later what it just did, it should answer:

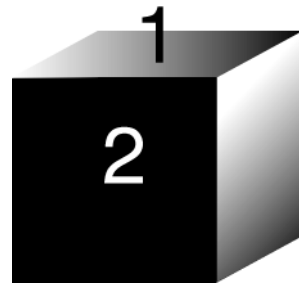
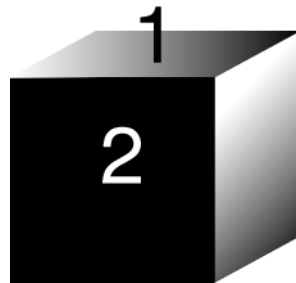
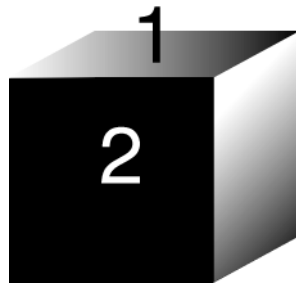
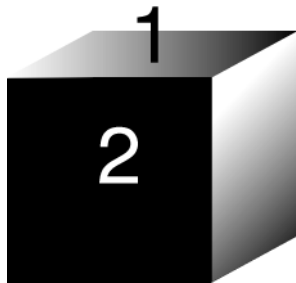
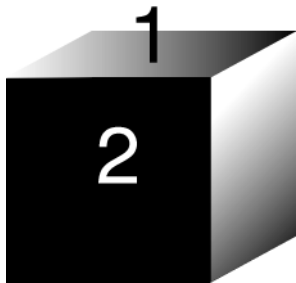
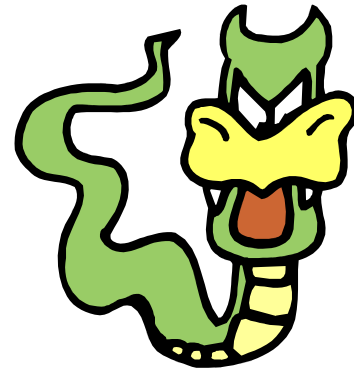
“I forget...”

What about *quantum* errors?

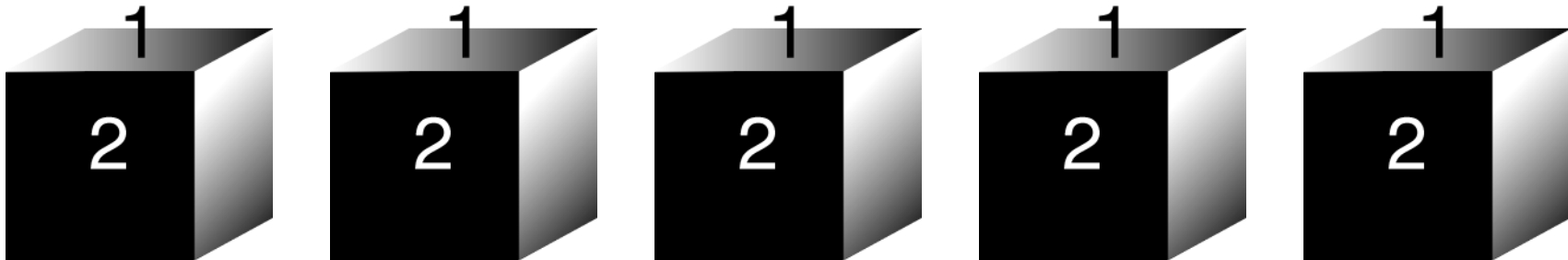
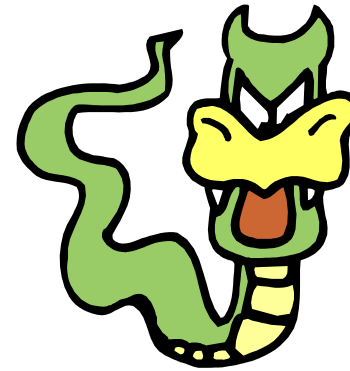


One qubit of quantum information can be encoded in the nonlocal correlations among five qubits.

What about *quantum* errors?



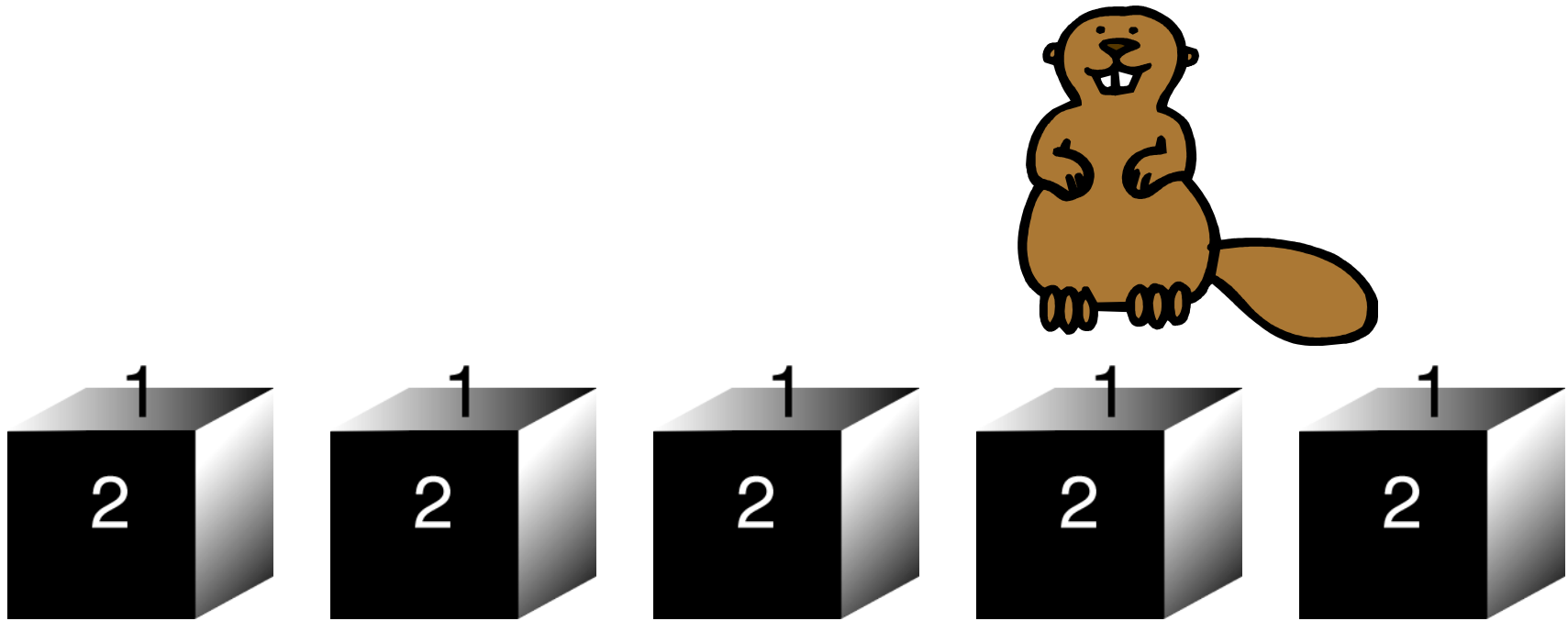
What about *quantum* errors?



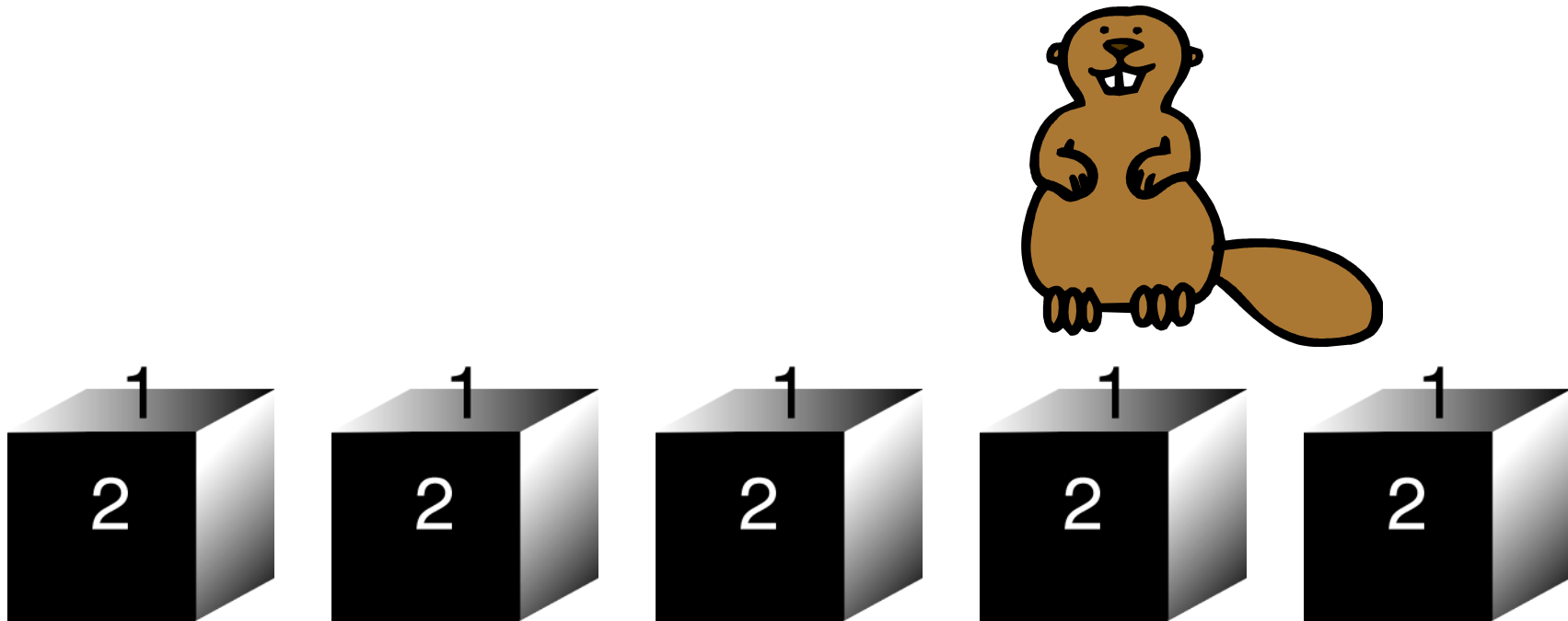
Though the dragon does damage one of the boxes, and he might learn something about the color of the ball in that box, this information does not tell him anything about the *encoded* qubit. Therefore the damage is *reversible*.

Error!

What about *quantum* errors?

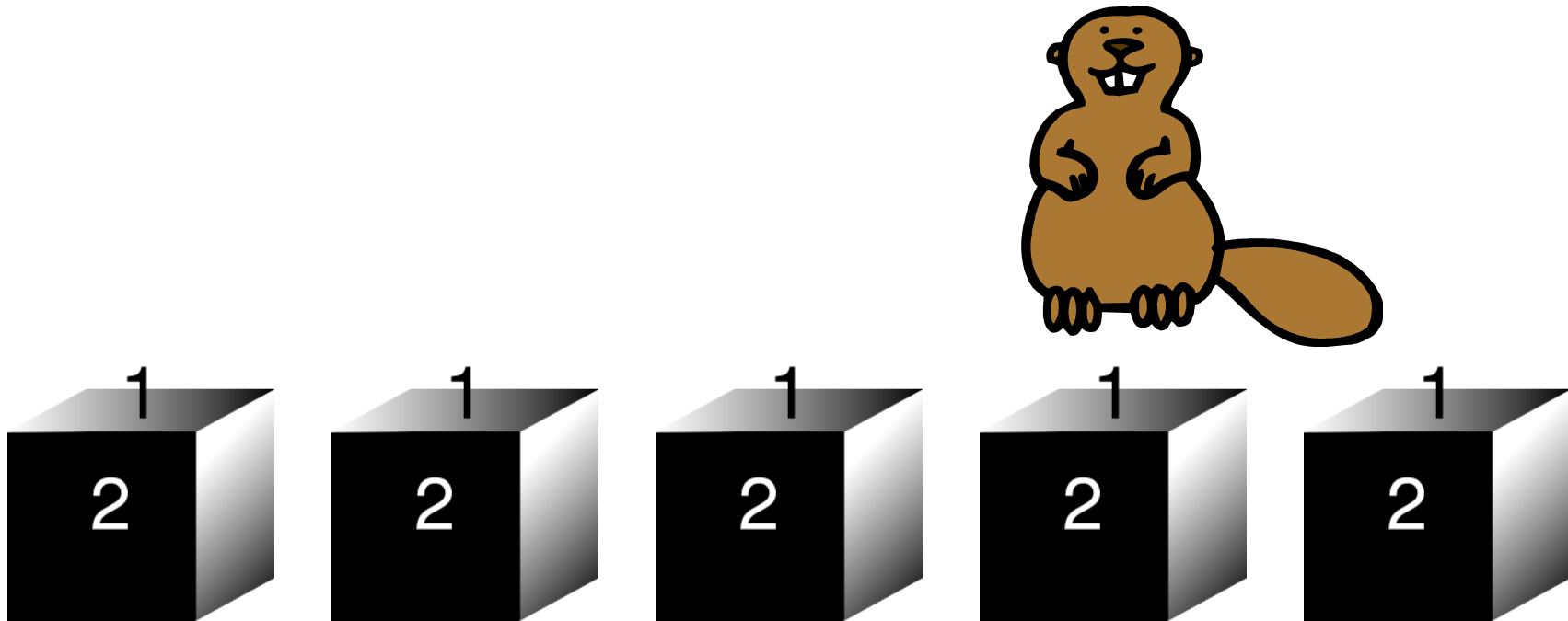


What about *quantum* errors?



By making carefully designed *collective* measurements on the five qubits (using a quantum computer), the beaver learns what damage the dragon inflicted, and how to reverse it. But he, too, learns nothing about the state of the encoded qubit.

What about *quantum* errors?



Redundancy protects against *quantum* errors!



Alexei
Kitaev

A. Kitaev

Anyons + Fault Tolerance

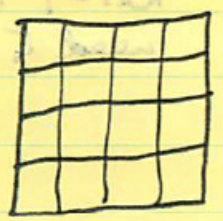
9 April 97

Classical Fault Tolerance

- Not needed! Why?

Magnetic disk: $H = -J \sum \sigma_i^z \sigma_{i+1}^z$ -- A "repetition code"
(spins align) $x_i = x_{i+1}$

Rep. code has no quantum analog
↓ closest thing is "toric code"



Torus --
qubits on
edges of
lattice

Stabilizer generators:

$\square A_r = \prod_{j \in \text{plaquette}} \sigma_j^x$

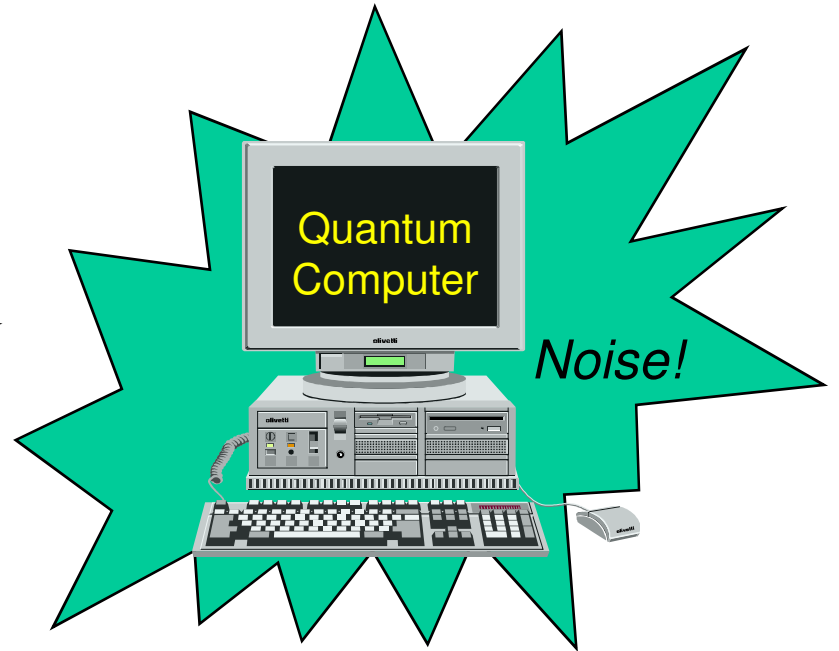
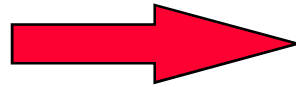
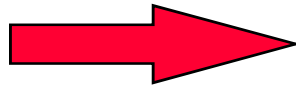
$\star B_l = \prod_{j \in \text{star}} \sigma_j^z$

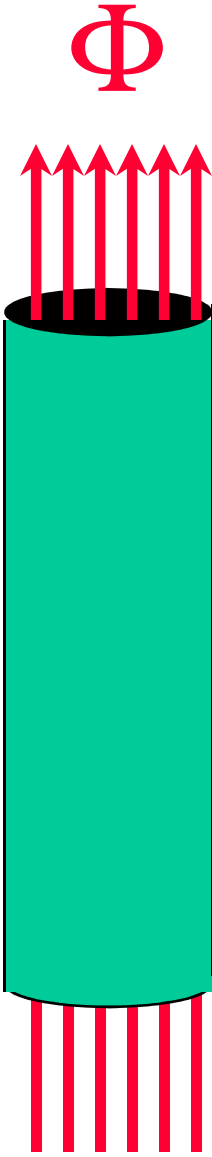
All mutually
commuting

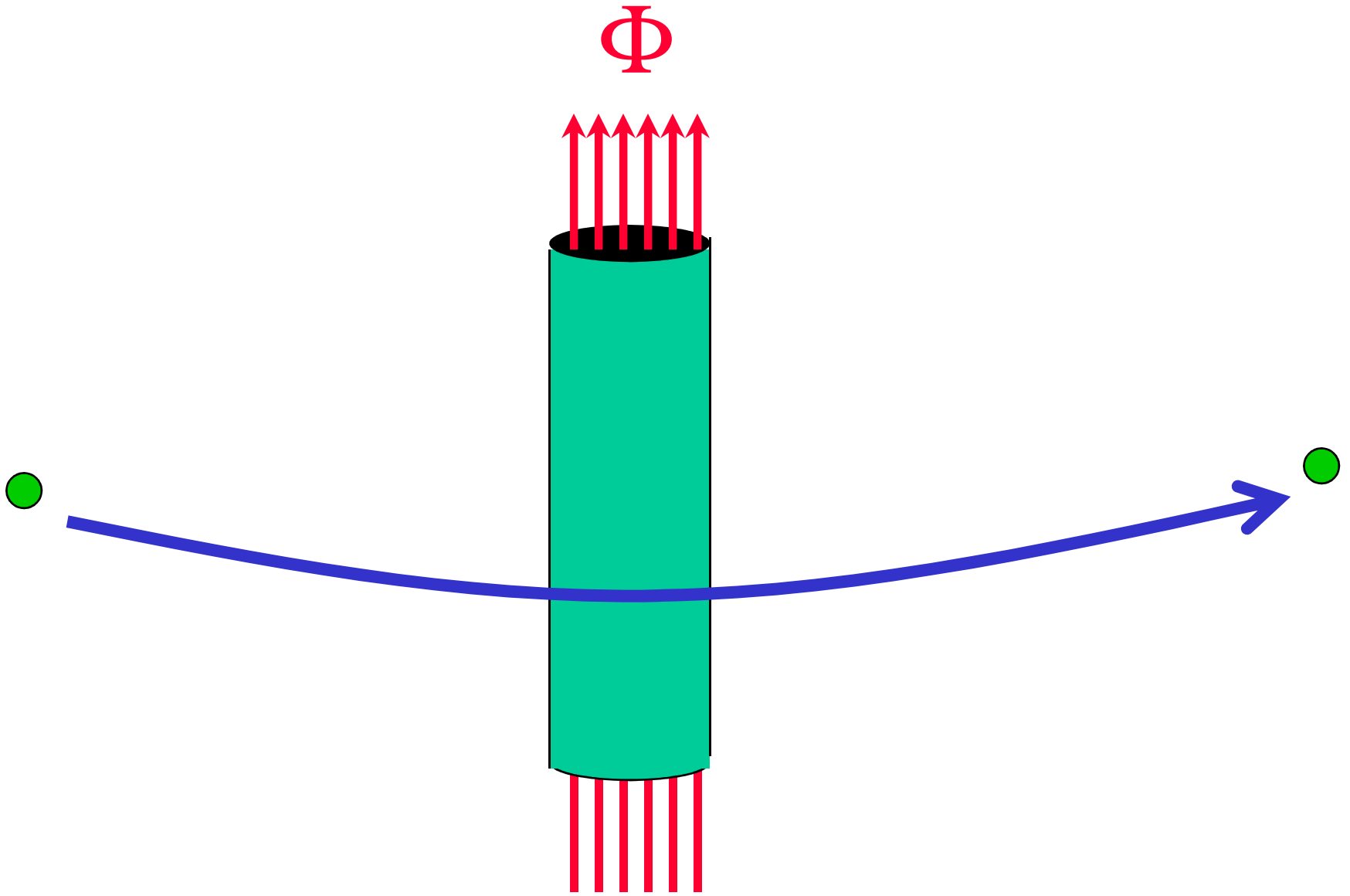


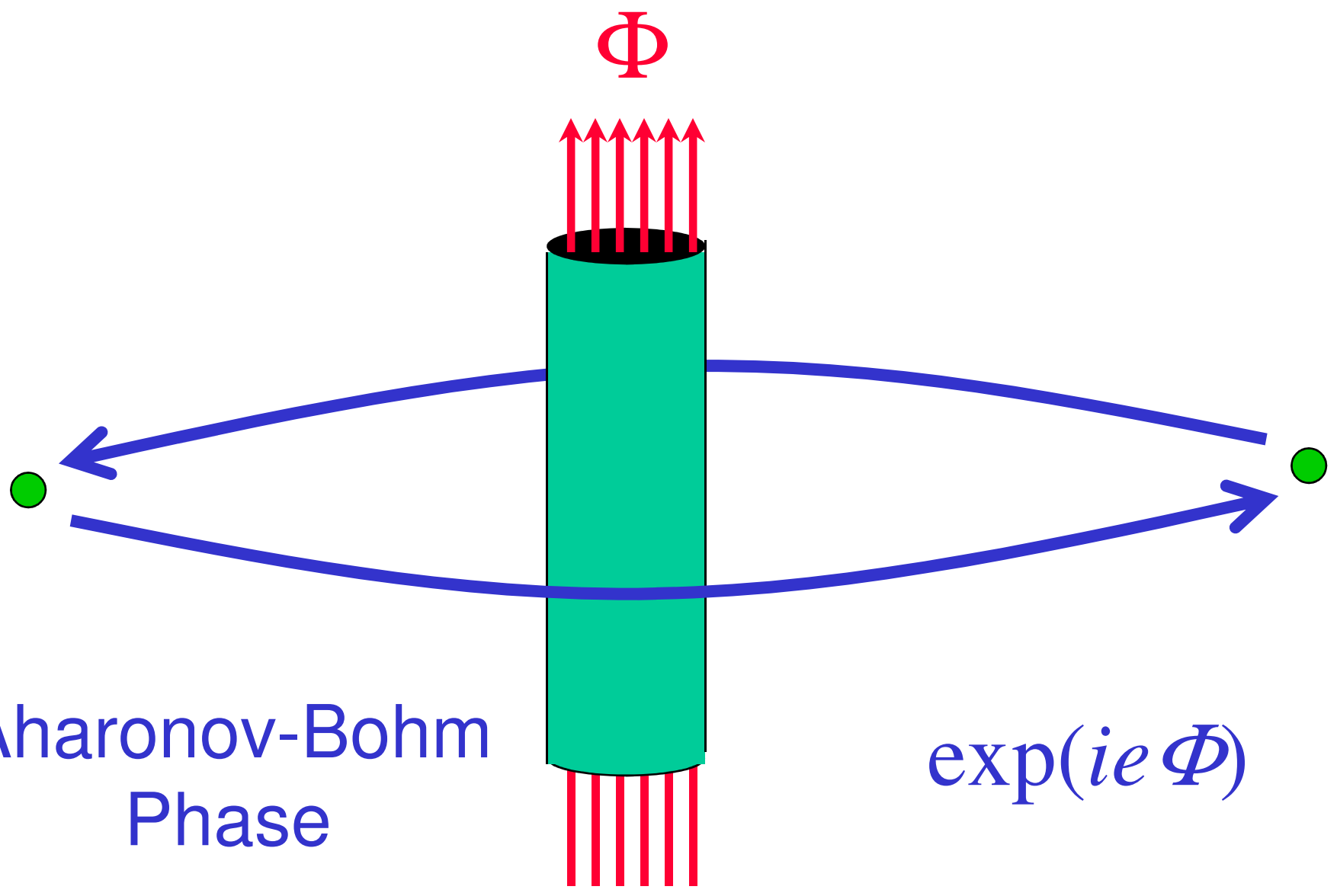
9 April 1997 ... An exciting day!

Topology



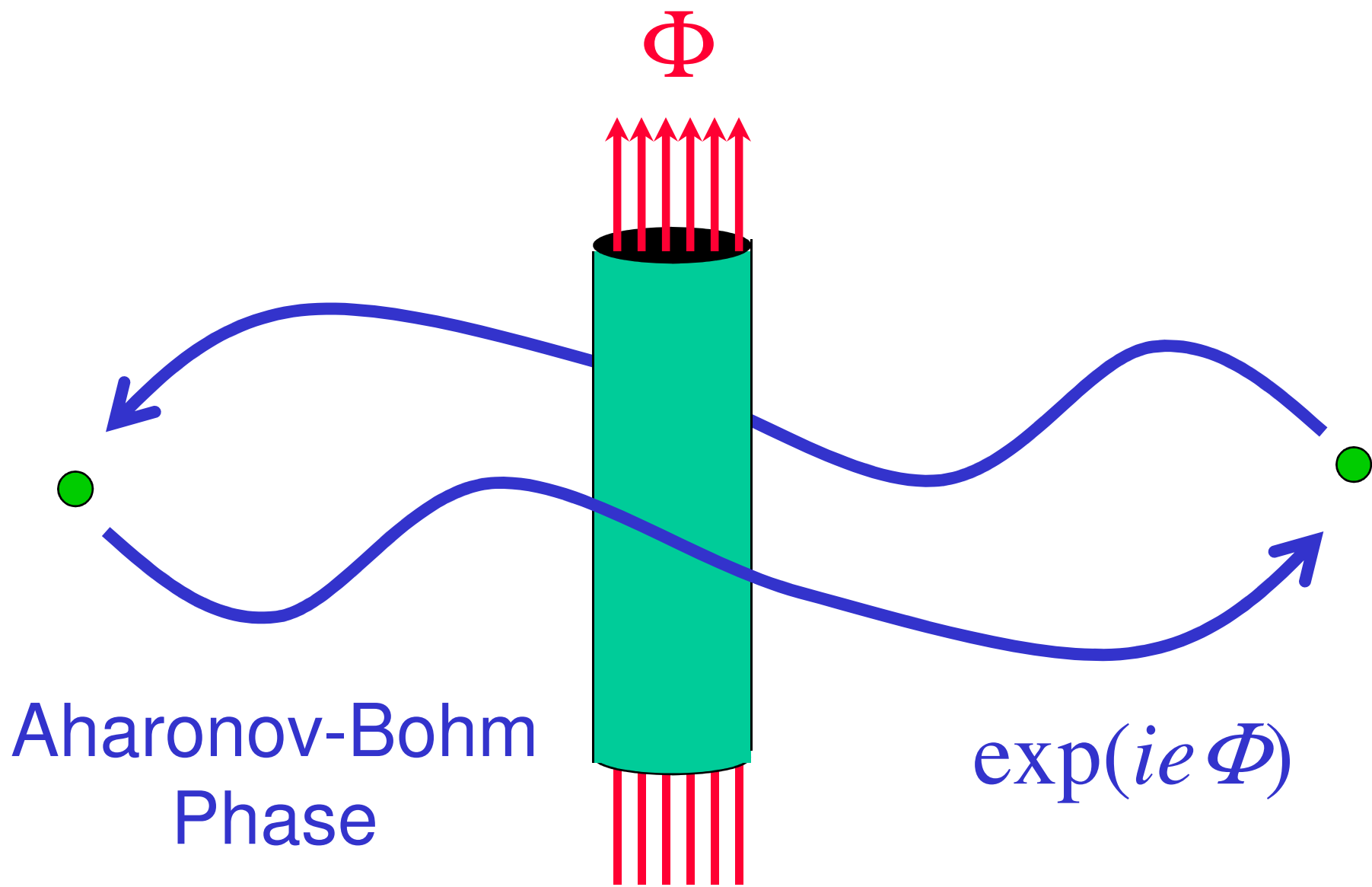






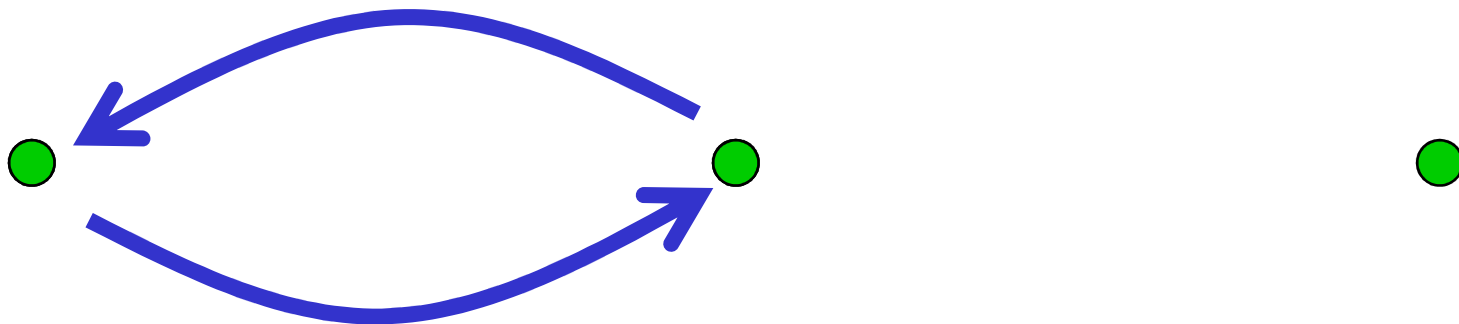
Aharonov-Bohm
Phase

$$\exp(ie\Phi)$$



Nonabelian anyons

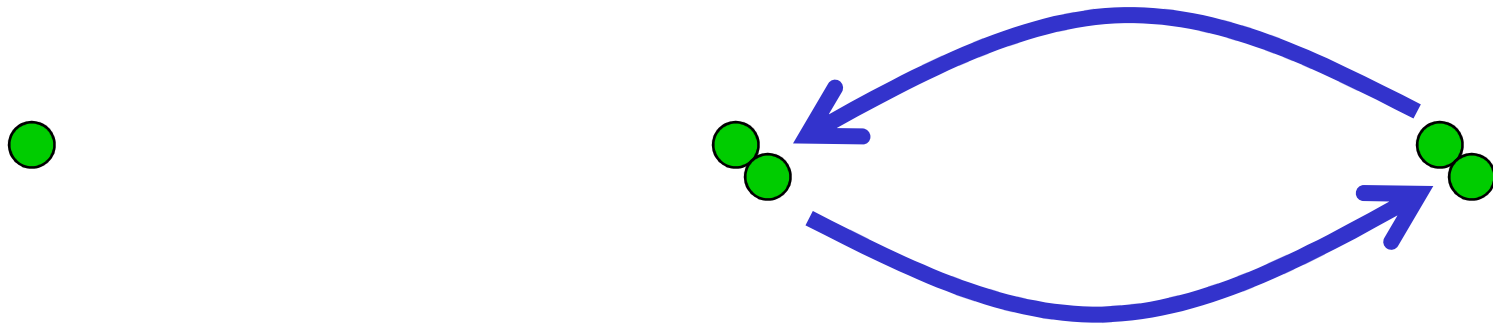
Quantum information can be stored in the collective state of exotic particles in two spatial dimensions (“anyons”).



The information can be processed by exchanging the positions of the anyons (even though the anyons never come close to one another).

Nonabelian anyons

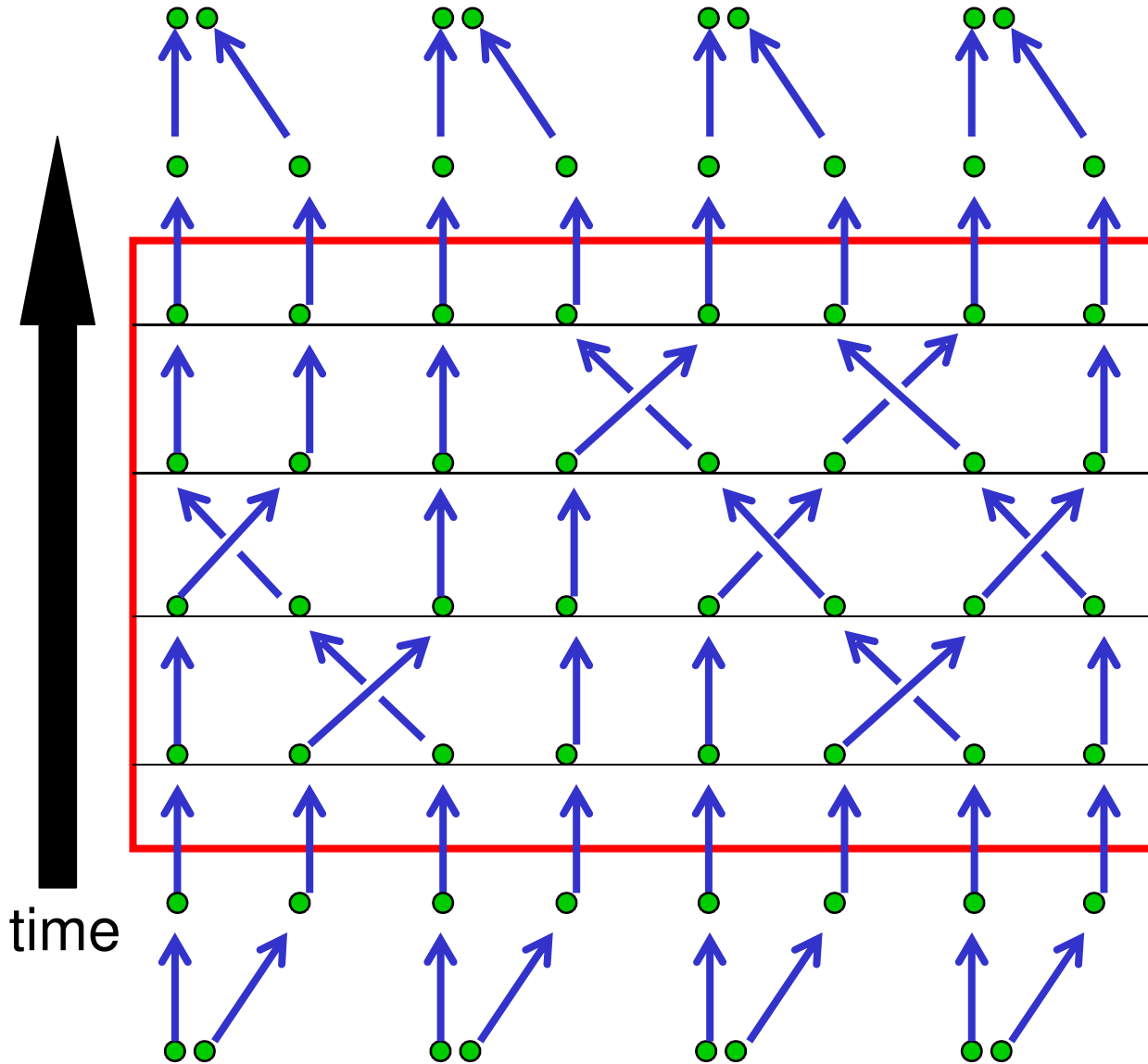
Quantum information can be stored in the collective state of exotic particles in two spatial dimensions (“anyons”).



The information can be processed by exchanging the positions of the anyons (even though the anyons never come close to one another).

Topological quantum computation

(Kitaev '97, FLW '00)



annihilate pairs?

braid

braid

braid

create pairs



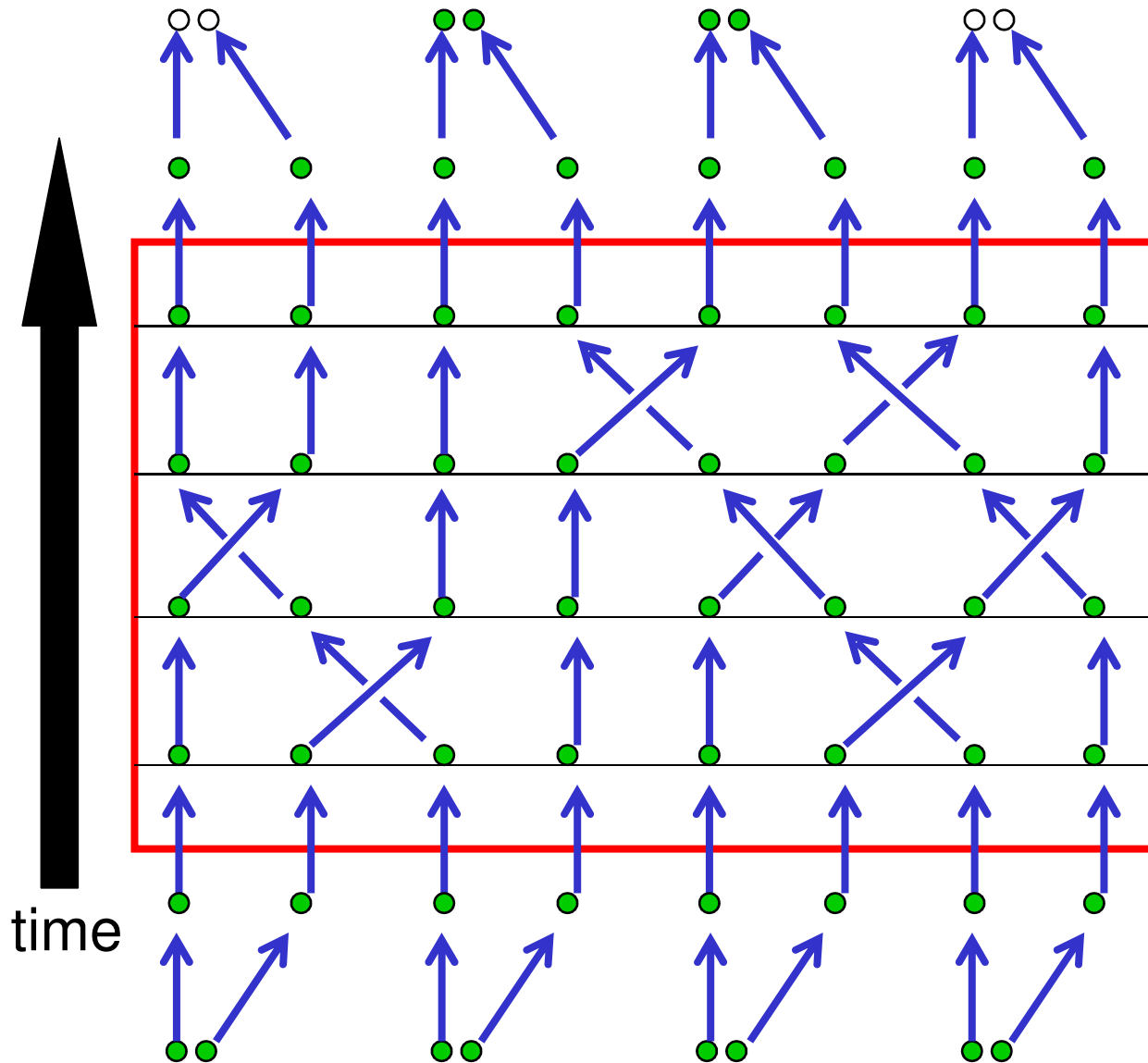
Kitaev



Freedman

Topological quantum computation

(Kitaev '97, FLW '00)



annihilate pairs?

braid

braid

braid

create pairs

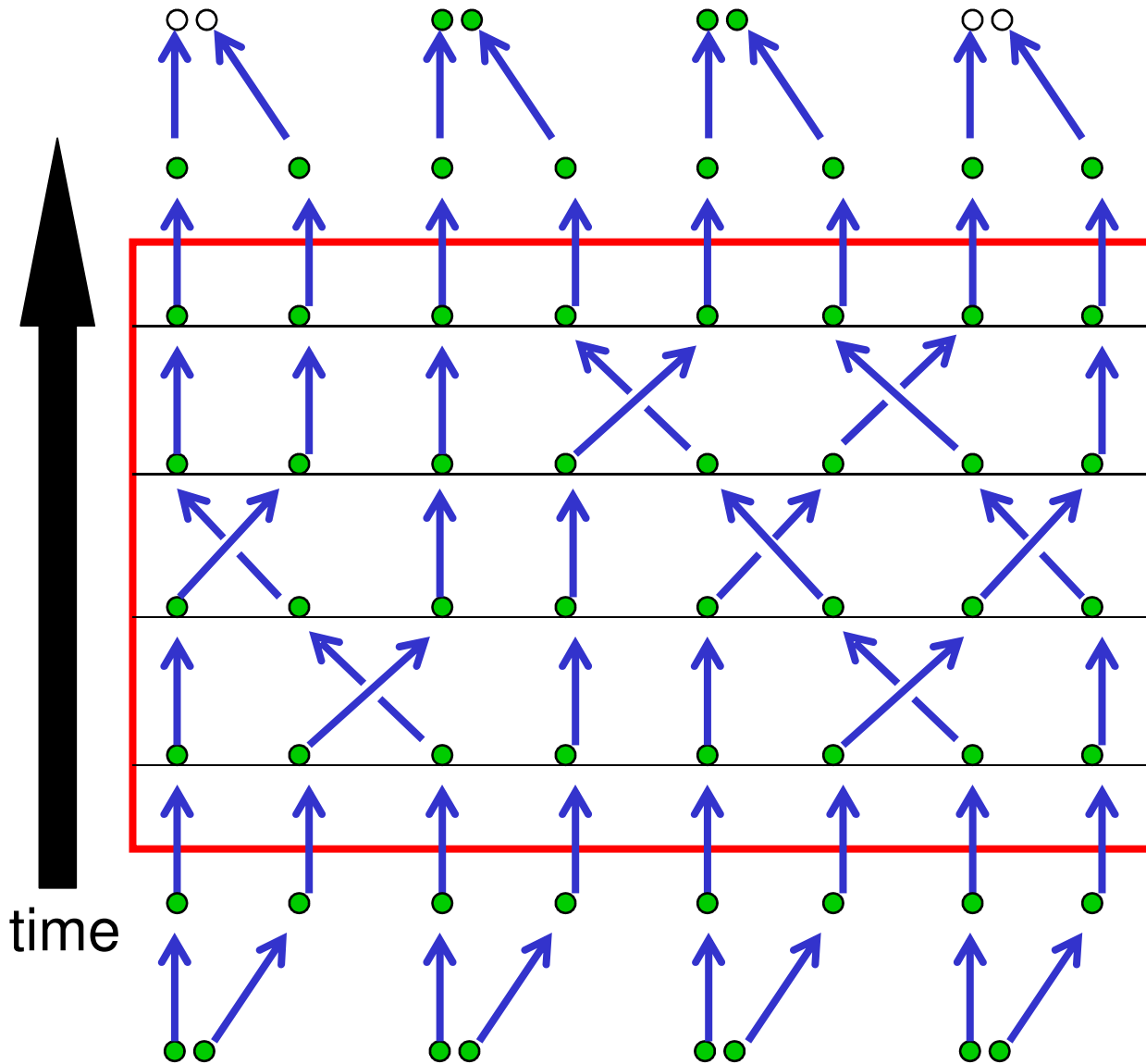


Kitaev



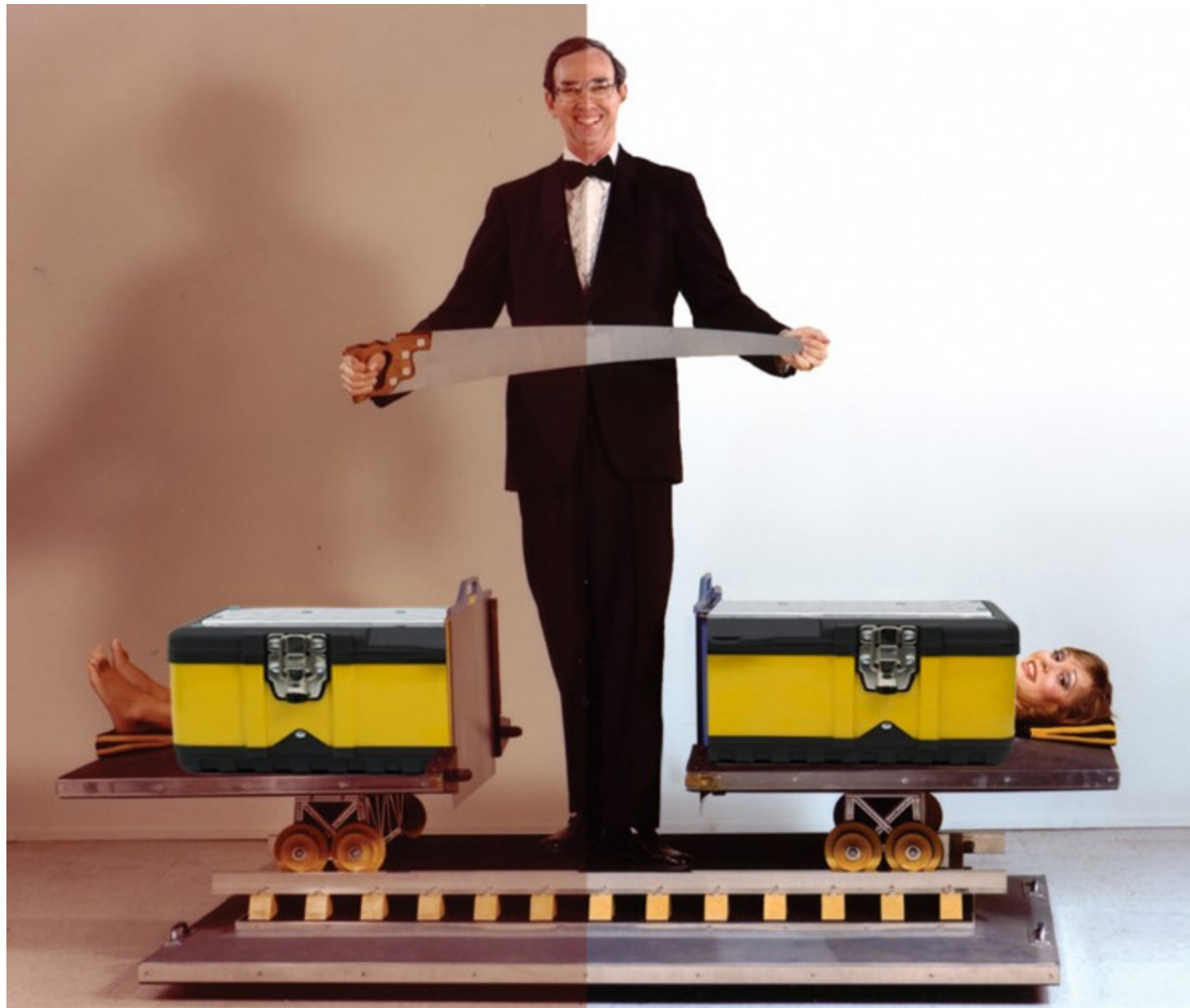
Freedman

Topological quantum computation

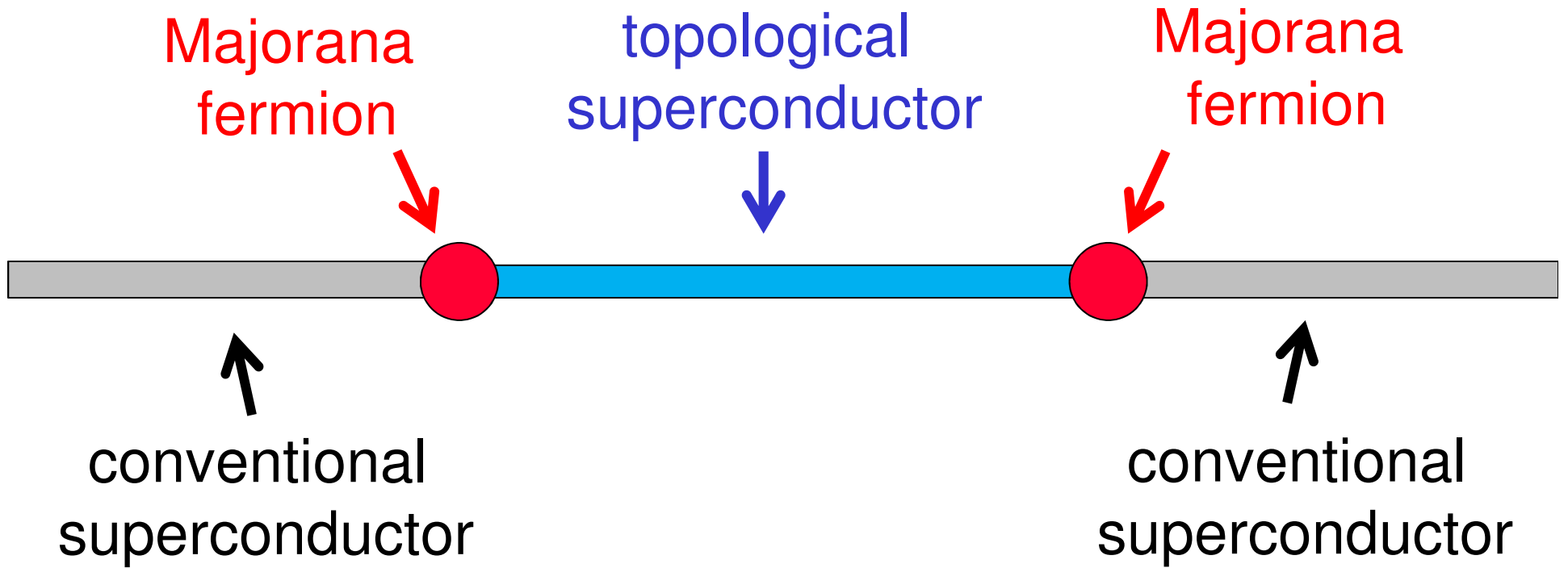


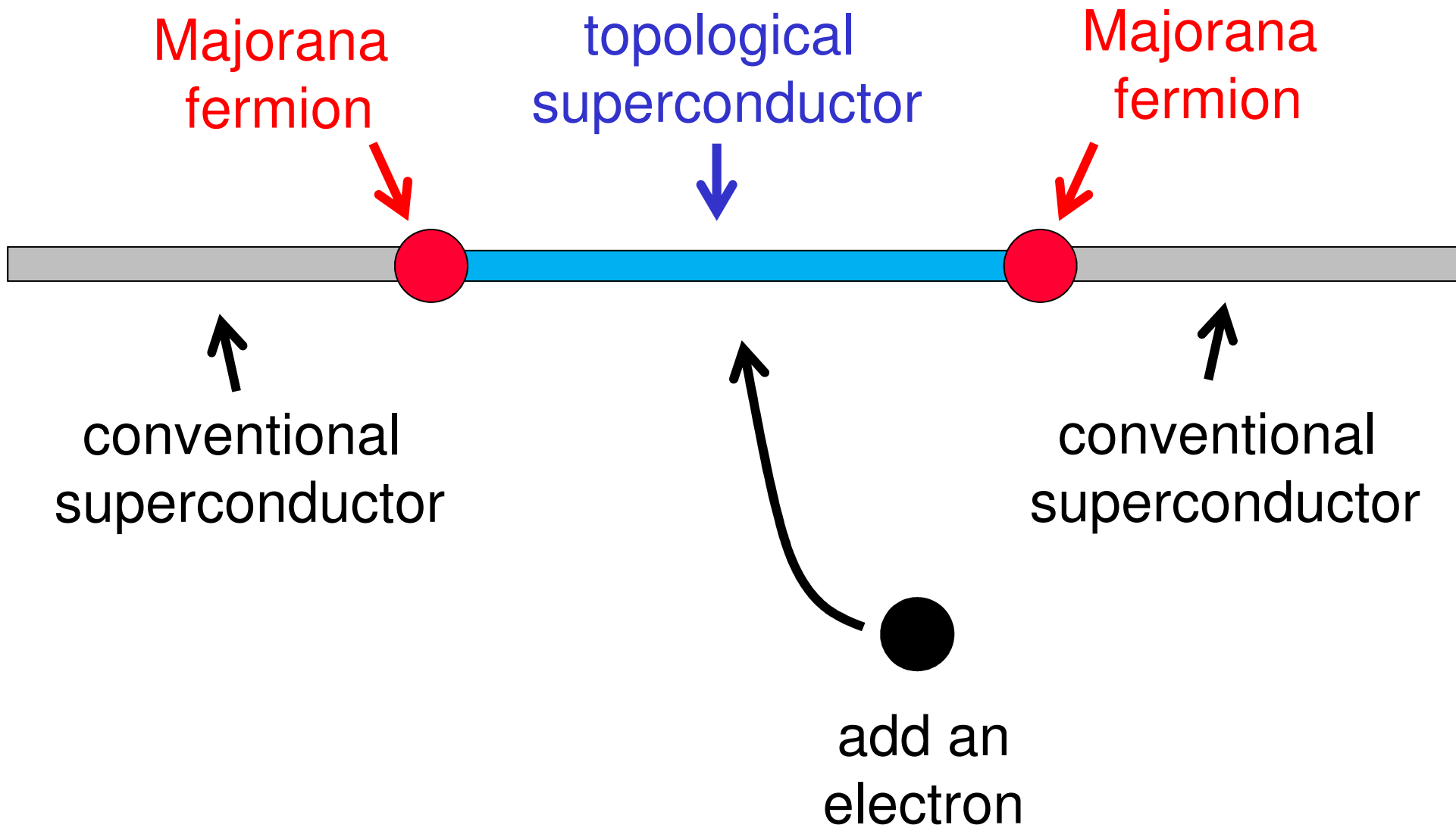
The computation is intrinsically resistant to decoherence.

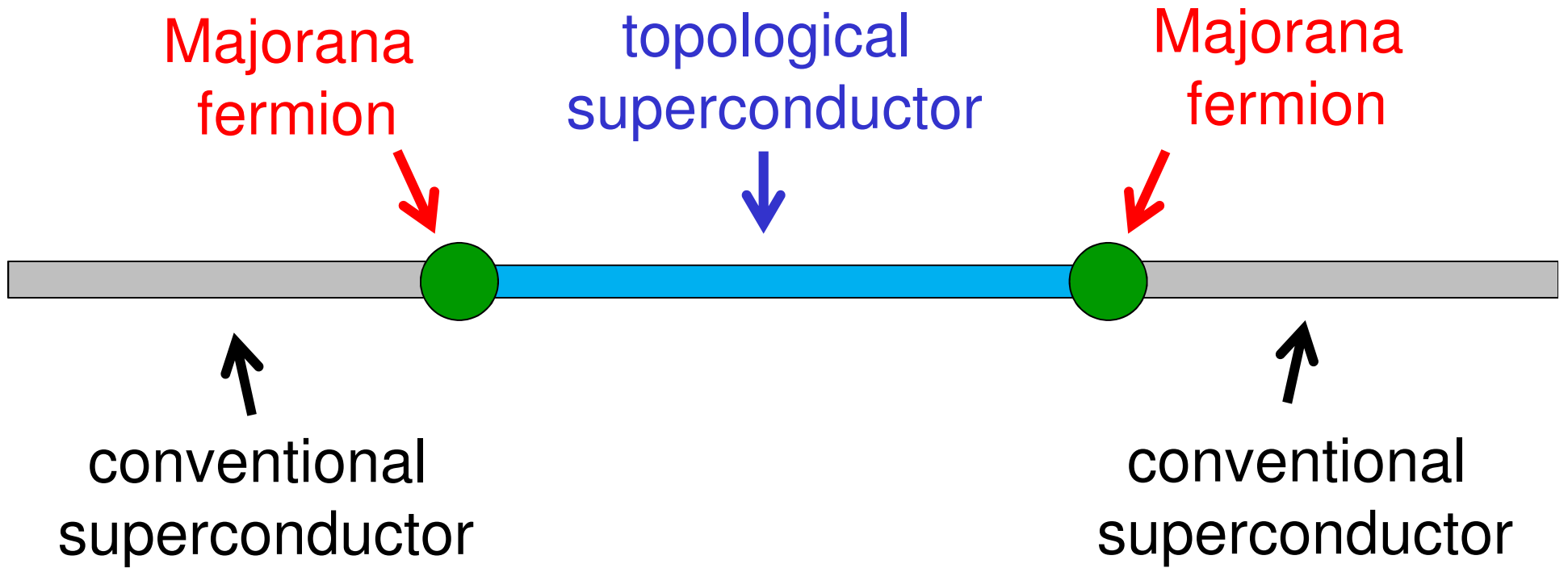
If the paths followed by the particles in spacetime execute the right braid, then the quantum computation is guaranteed to give the right answer!

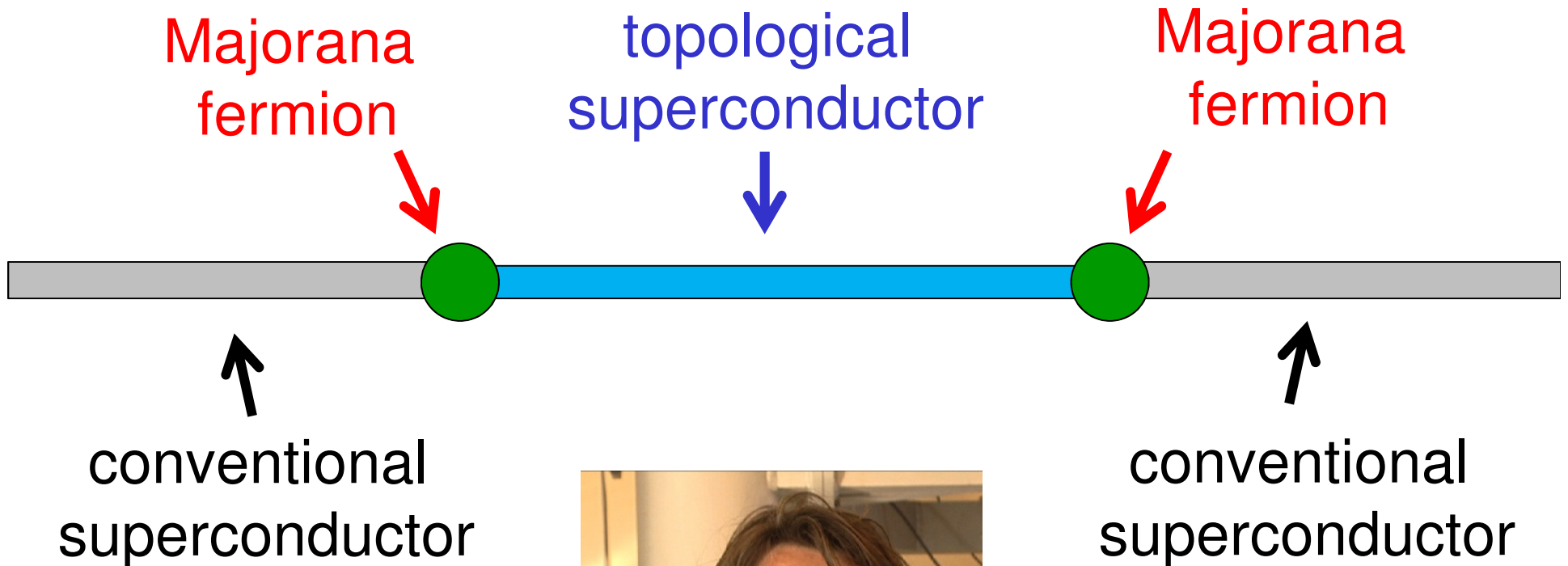


Kitaev's magic trick: sawing an *electron* in half!



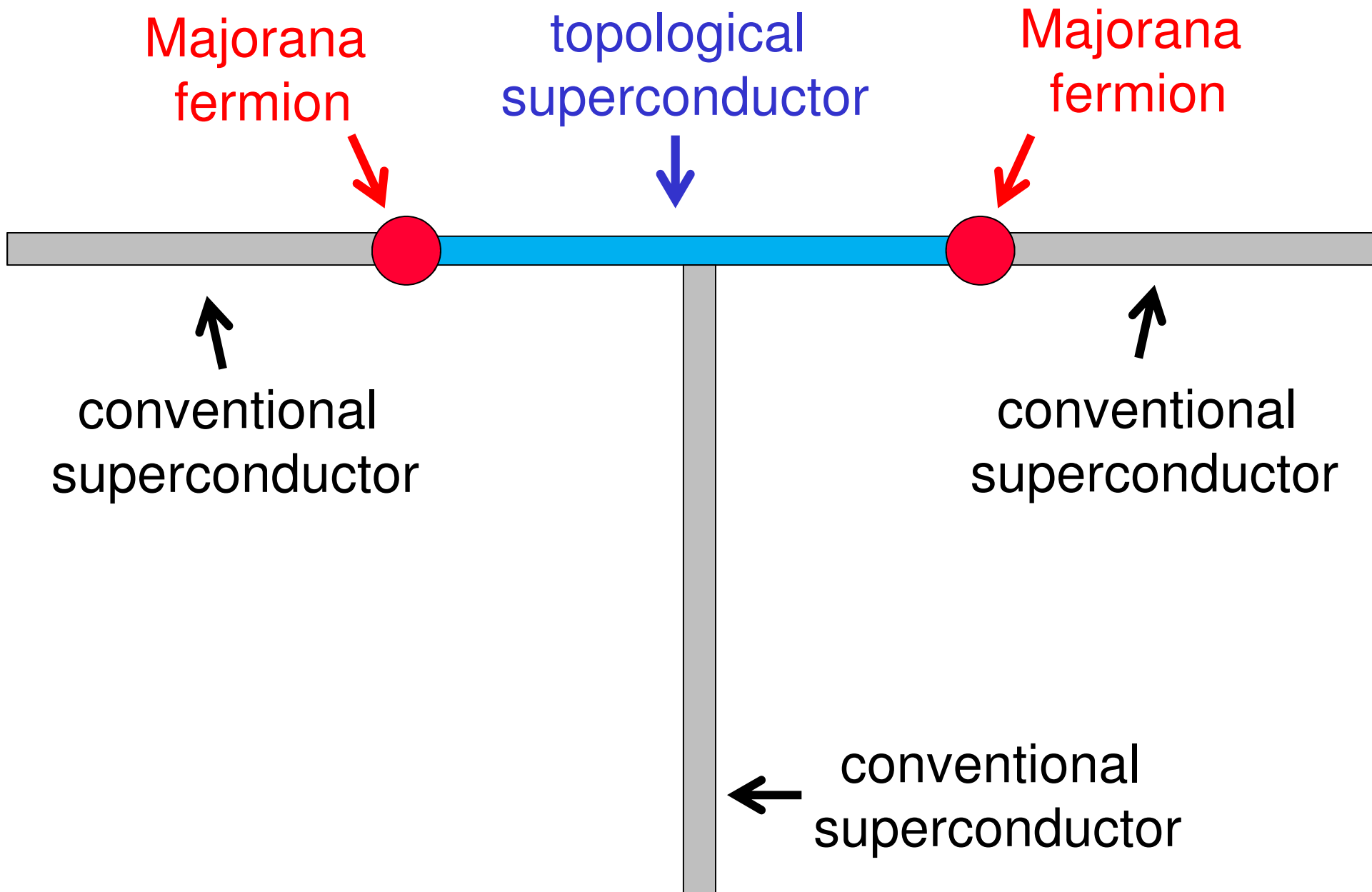


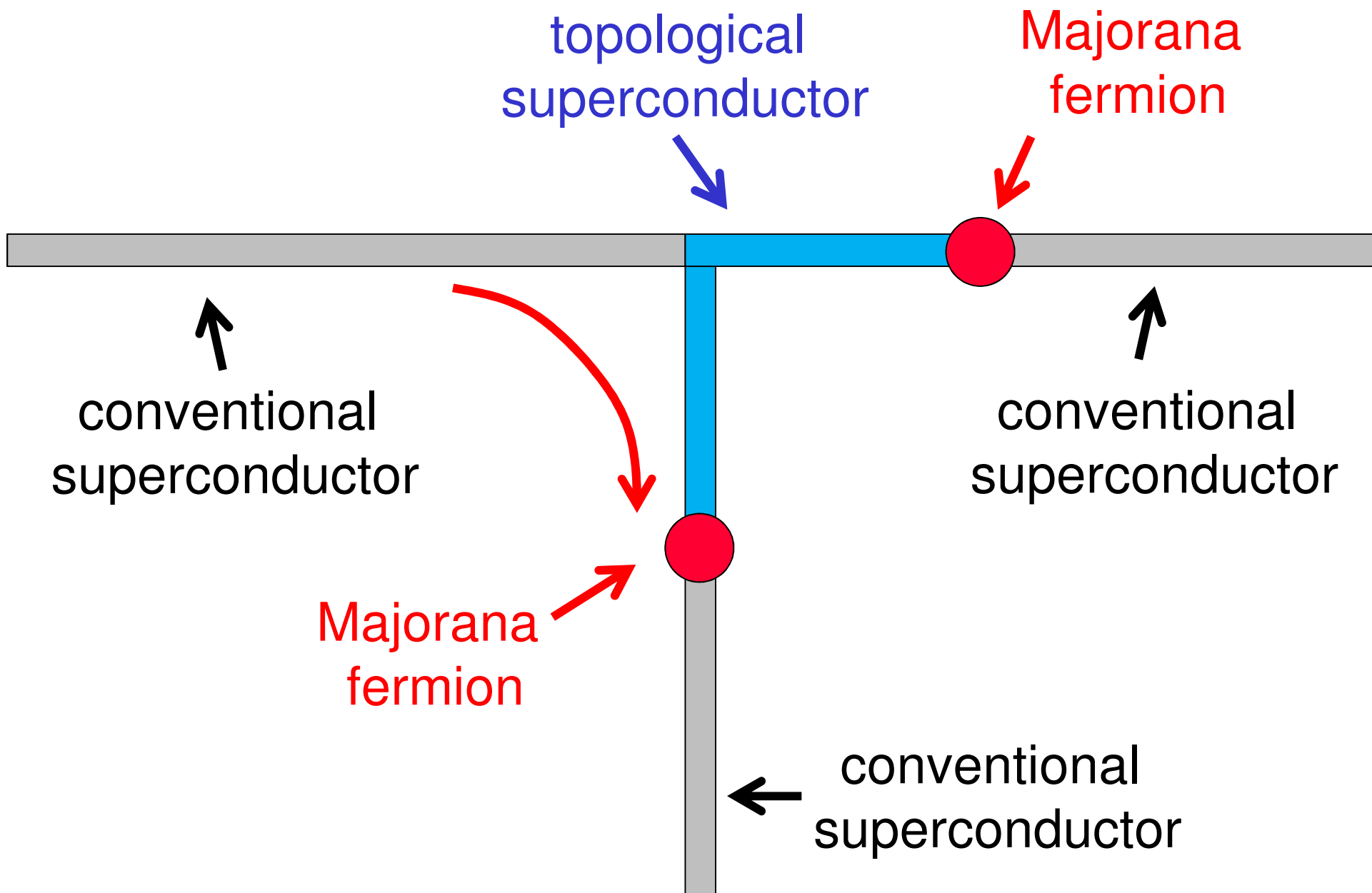


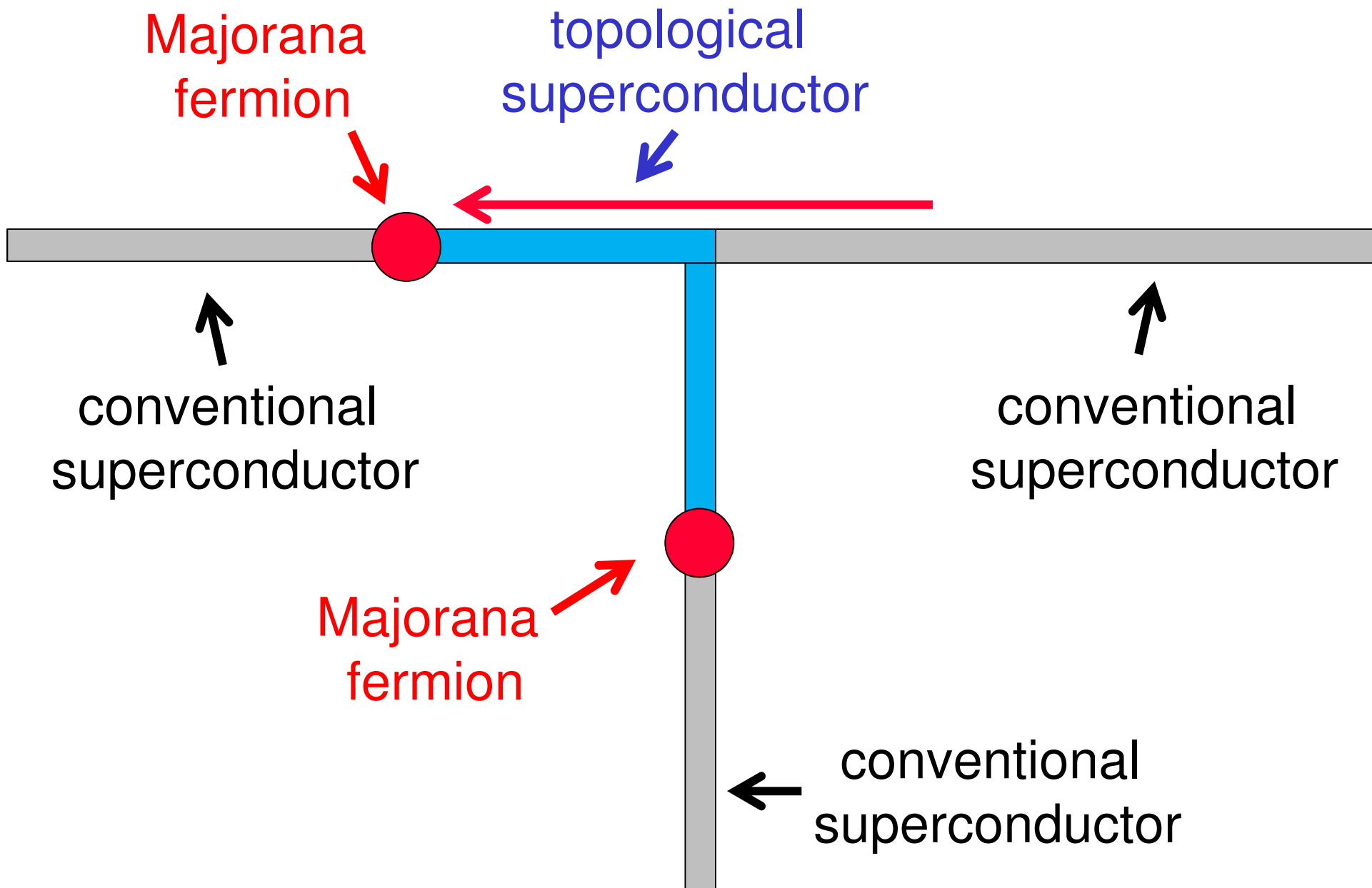


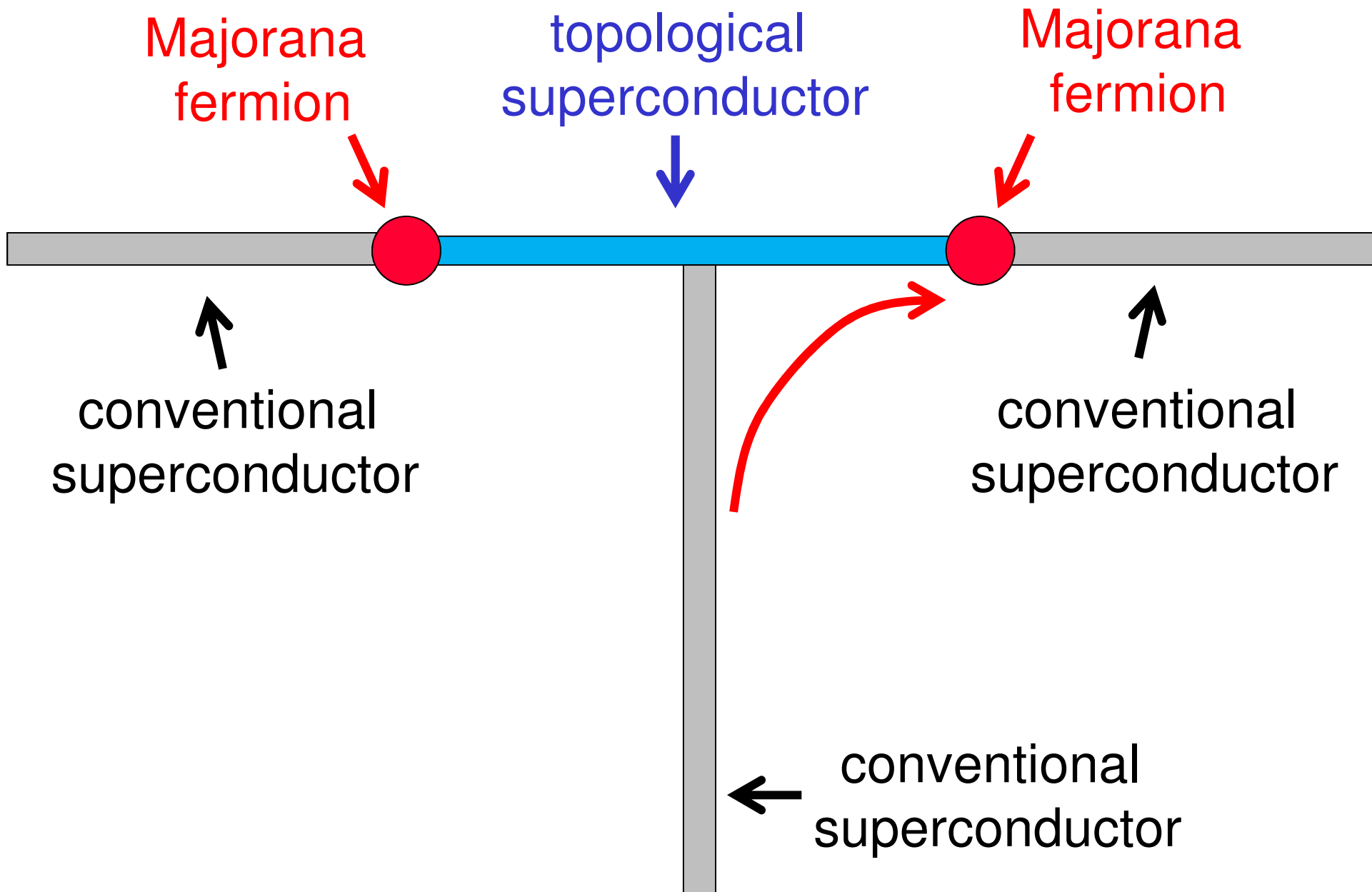
Kouwenhoven

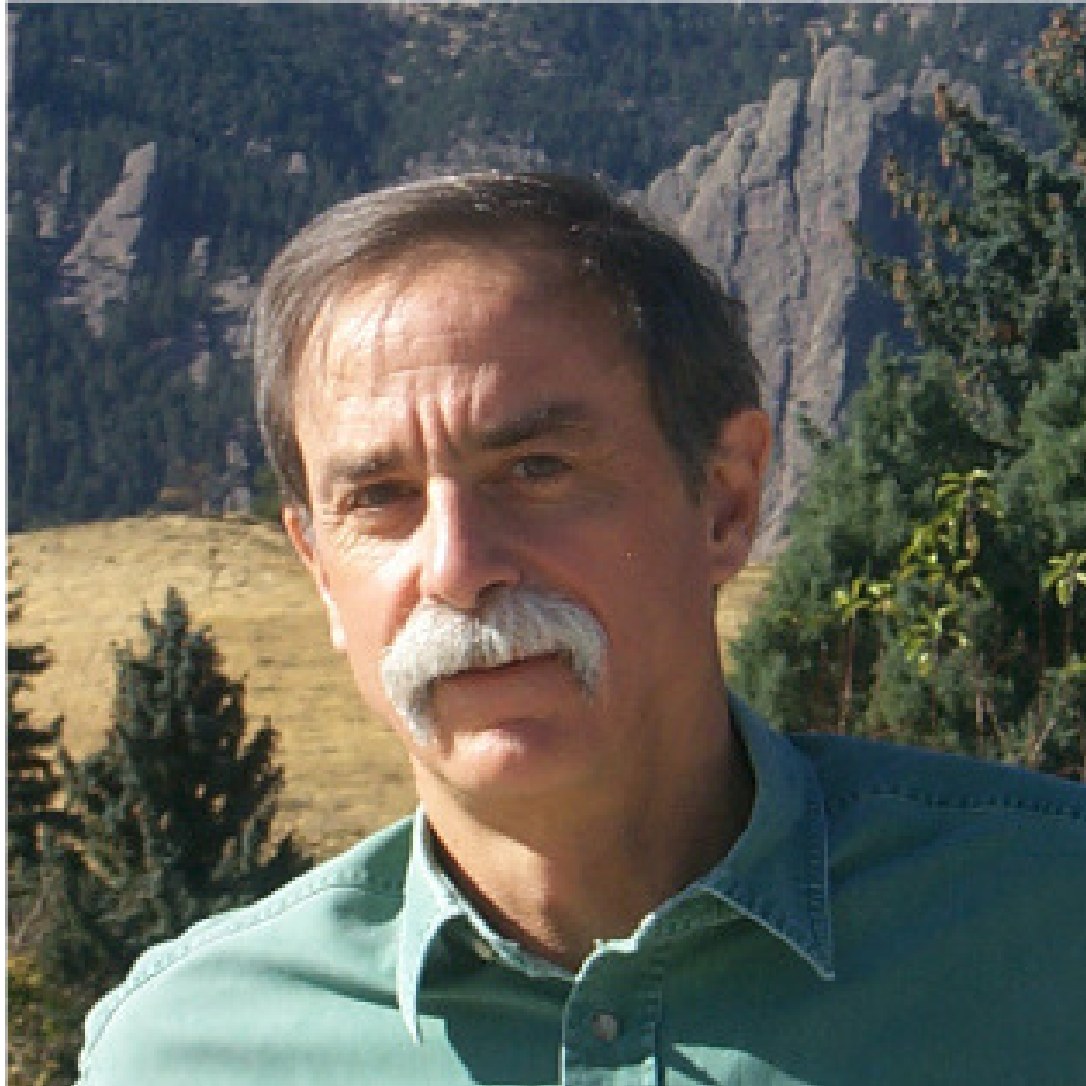
Mourik, Zuo, Frolov, Plissard, Bakkers, and Kouwenhoven (2012).







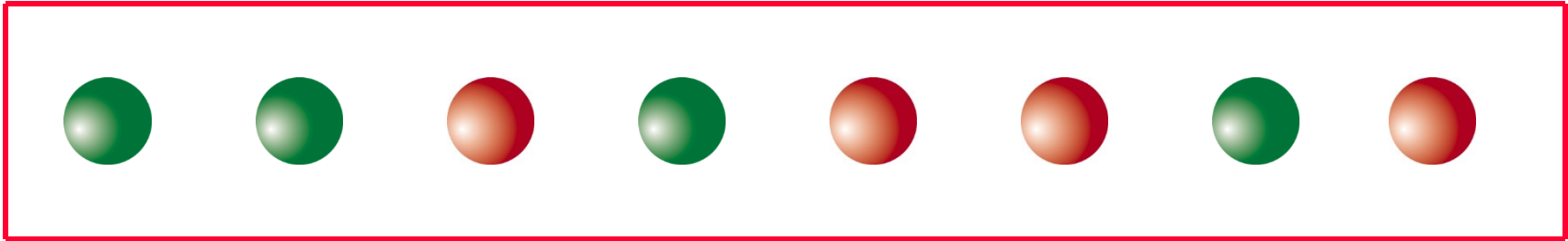




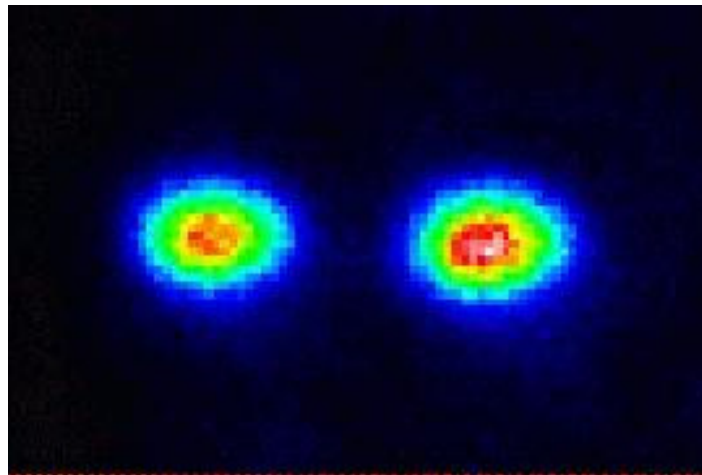
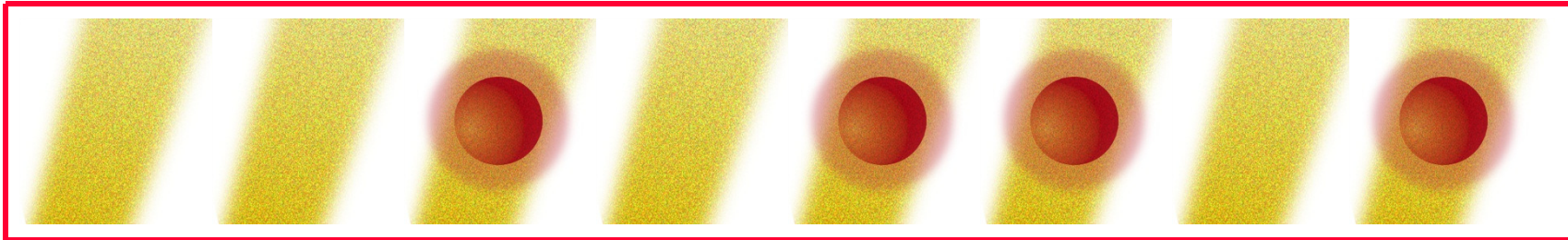
Dave Wineland

2012 Nobel Prize
in Physics

Ion Trap Quantum Computer

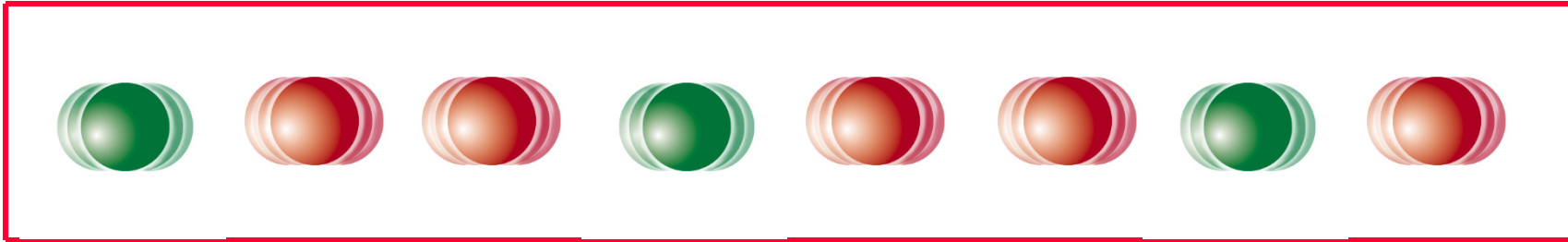


Ion Trap Quantum Computer

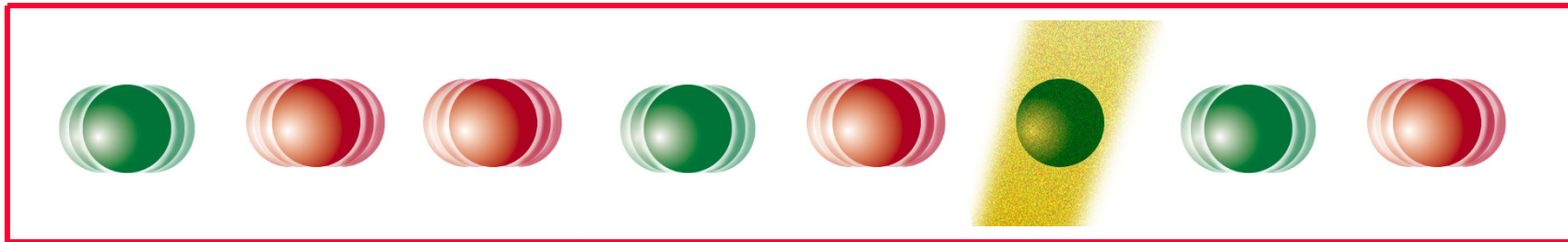


Two ${}^9\text{Be}^+$ ions in an ion trap at the National Institute of Standards and Technology (NIST) in Boulder, CO.

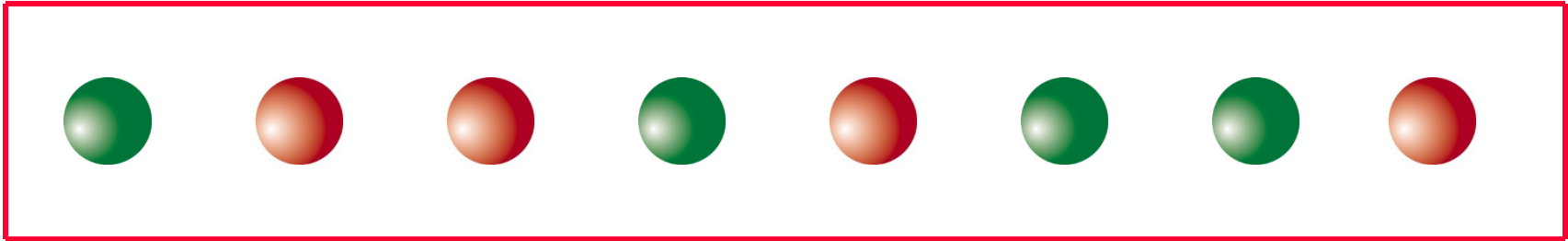
Ion Trap Quantum Computer



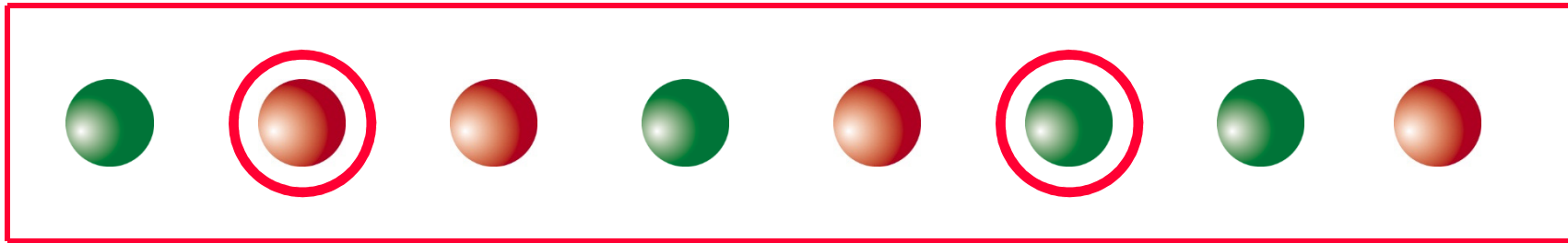
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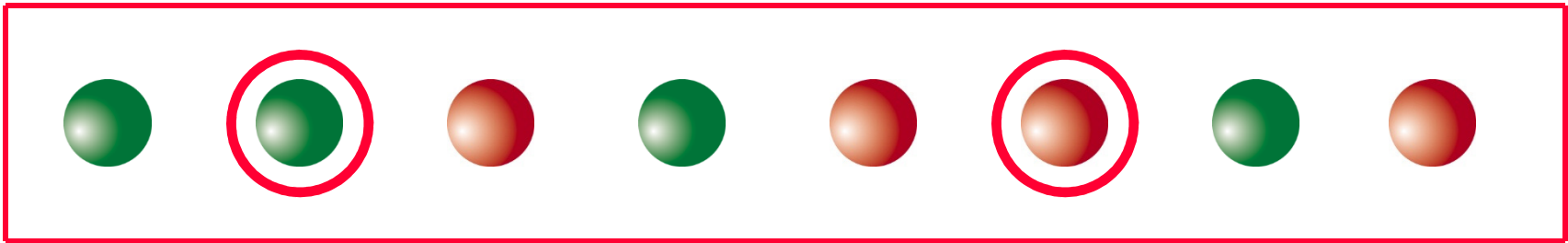
Ion Trap Quantum Computer



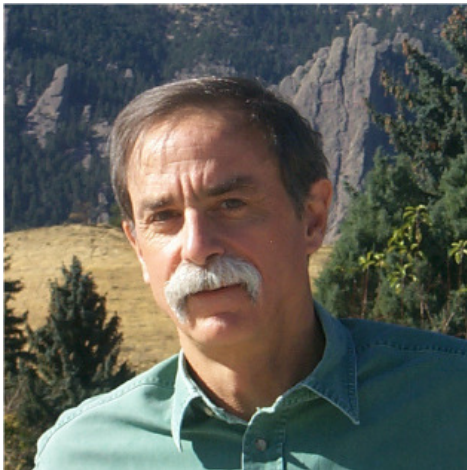
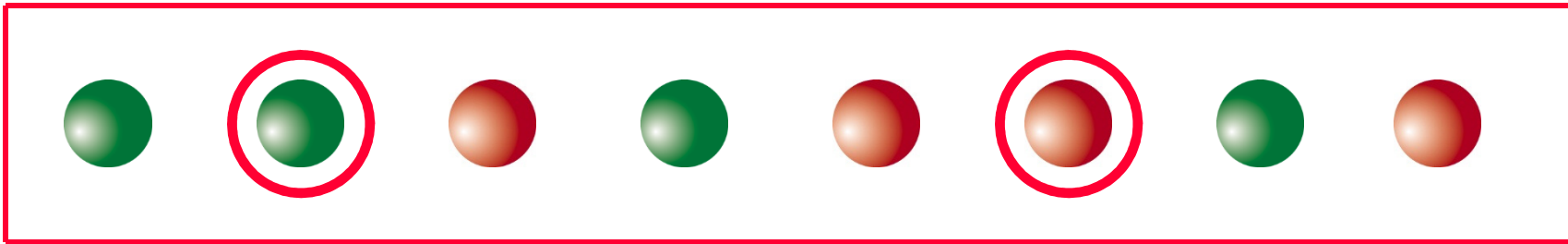
Ion Trap Quantum Computer



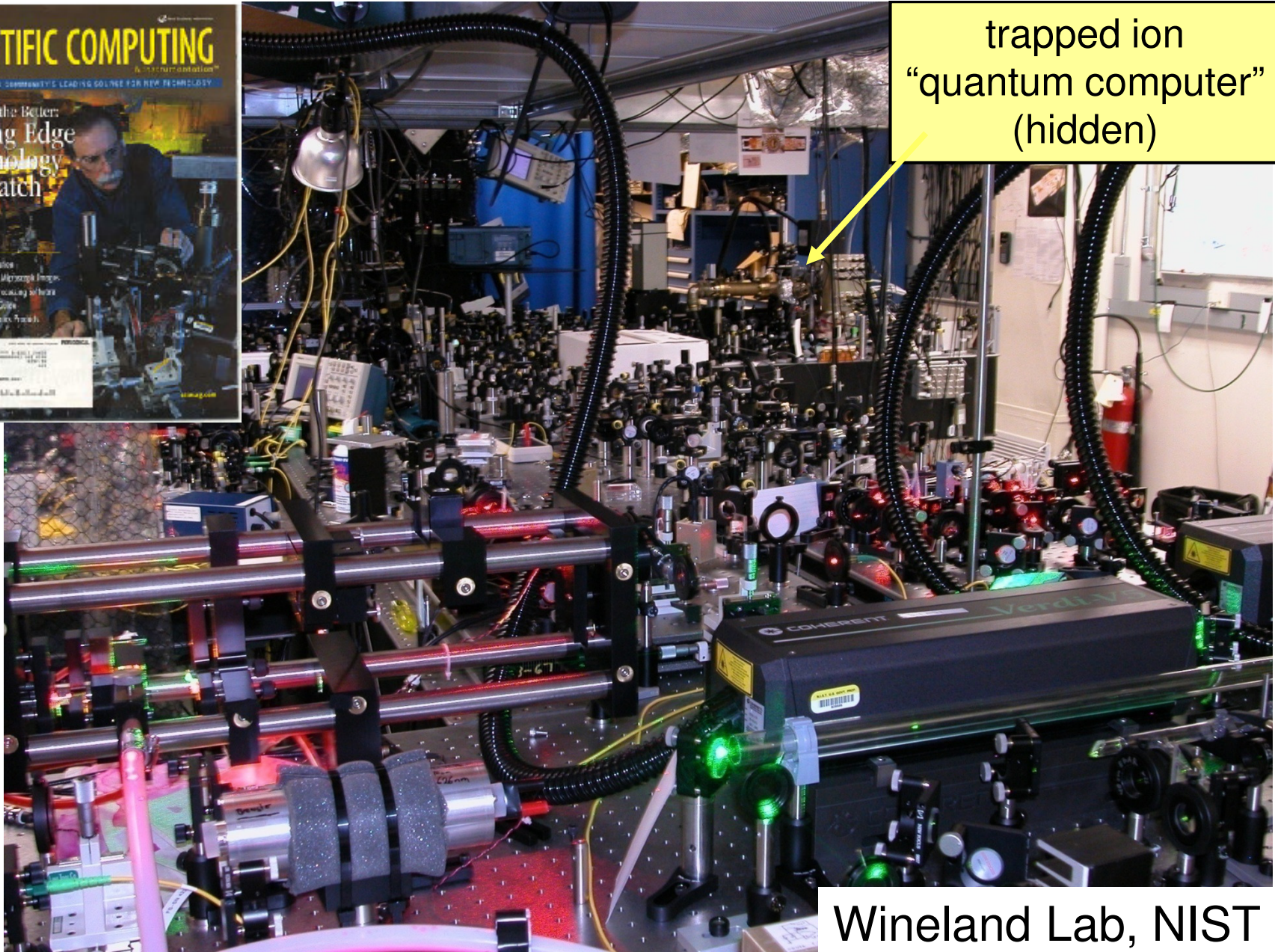
Ion Trap Quantum Computer



Ion Trap Quantum Computer

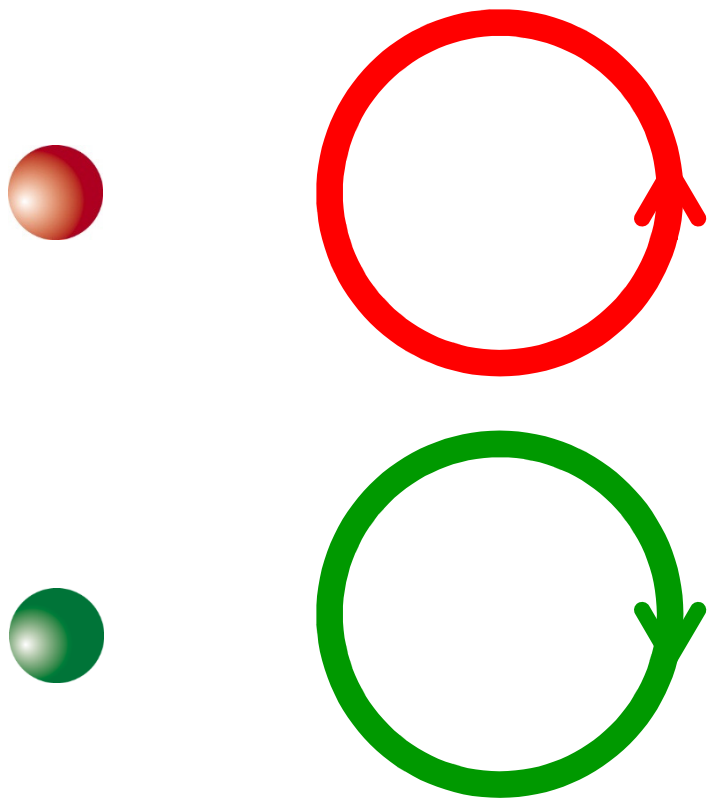


Dave
Wineland

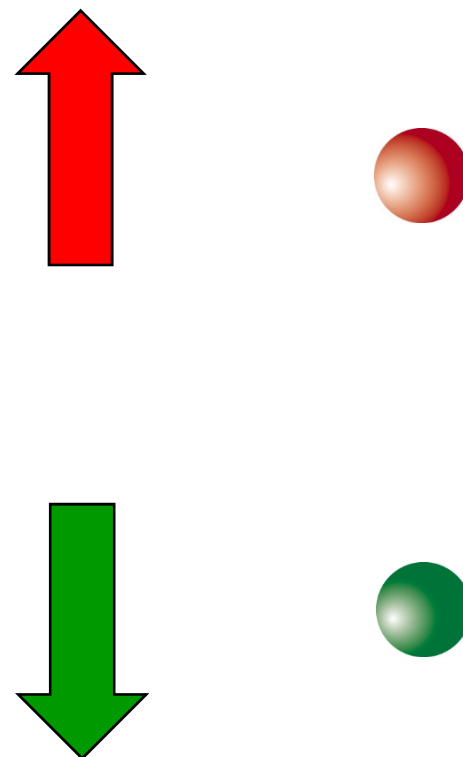


Ion trap quantum computer: **The Reality**

Persistent current in a superconducting circuit



Magnetic field of a single electron



Quantum Hardware



Schoelkopf

Two-level ions in a Paul trap, coupled to “phonons.”

Superconducting circuits with Josephson junctions.

Electron spin (or charge) in quantum dots.

Cold neutral atoms in optical lattices.

Two-level atoms in a high-finesse microcavity, strongly coupled to cavity modes of the electromagnetic field.

Linear optics with efficient single-photon sources and detectors.

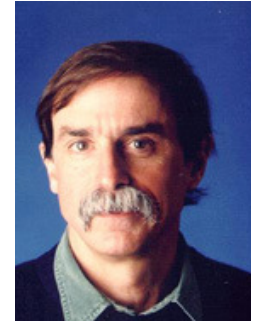
Nuclear spins in semiconductors, and in liquid state NMR.

Nitrogen vacancy centers in diamond.

Anyons in fractional quantum Hall systems, quantum wires, etc.



Yacoby



Wineland



Blatt



Marcus

Classical vs. Quantum Factoring



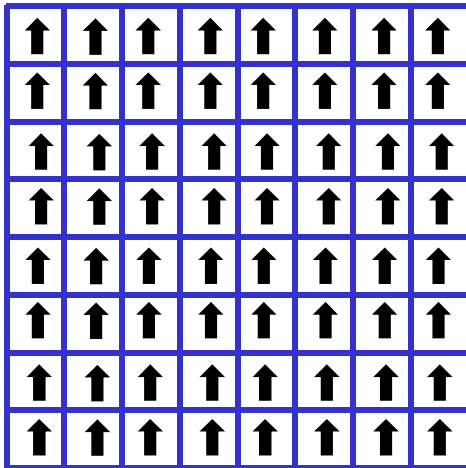
Martinis

Factoring 2048 bit number ...

Classical algorithm: 10 year run time and requires a server farm covering 1/4 of North America, at cost of $\$10^6$ trillion. Consumes 10^6 terawatt (10^5 times world output). Would consume world's supply of fossil fuels in one day.

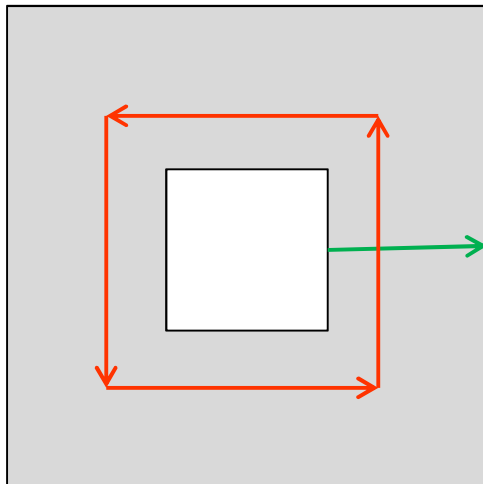
Quantum algorithm (brute force): 10K logical qubits and 10M physical (superconducting) qubits. 1 cm spacing to allow room for lost of wires. Costs $\$100B$ ($\$10K$ per physical qubit) and runs in 16 hours. Consumes 10 MWatt. (We need to get the cost down.)

Quantum error correction



Classical memory \Leftrightarrow ferromagnet order

Robust bit



Quantum memory \Leftrightarrow topological order

Robust qubit

Red path (door 1) or green path (door 2)

Realize physically, or simulate with generic hardware.

Some recently reported error rates

Ion trap – one-qubit gates:

$\sim 2 \times 10^{-5}$ [NIST]

Ion trap – two-qubit gates:

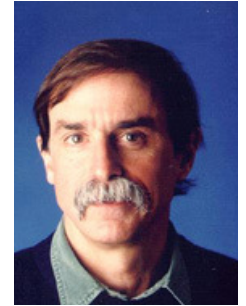
$\sim 5 \times 10^{-3}$ [Innsbruck]

Superconducting circuits – one-qubit gate

$\sim 2.5 \times 10^{-3}$ [Yale]

Quantum error correction becomes effective when gate error rates are low enough, and the overhead cost of error correction improves as hardware becomes more reliable.

Error rates are estimated by performing “circuits” of variable size, and observing how the error in the final readout grows with circuit size.



Wineland



Blatt



Schoelkopf

Three Questions About Quantum Computers

1. *Why* build one?

How will we use it, and what will we learn from it?

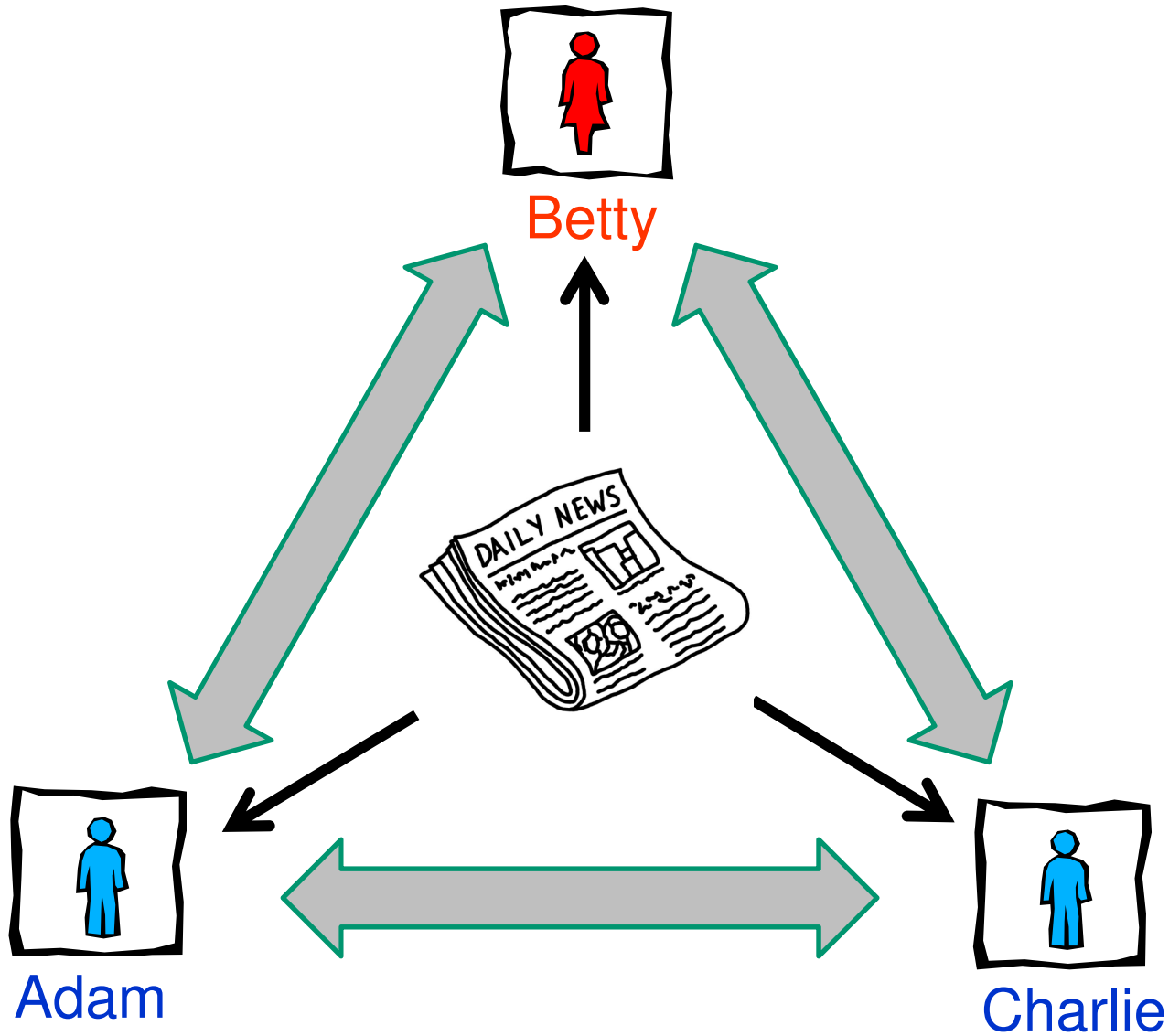
2. *Can* we build one?

Are there obstacles that will prevent us from building quantum computers as a matter of principle?

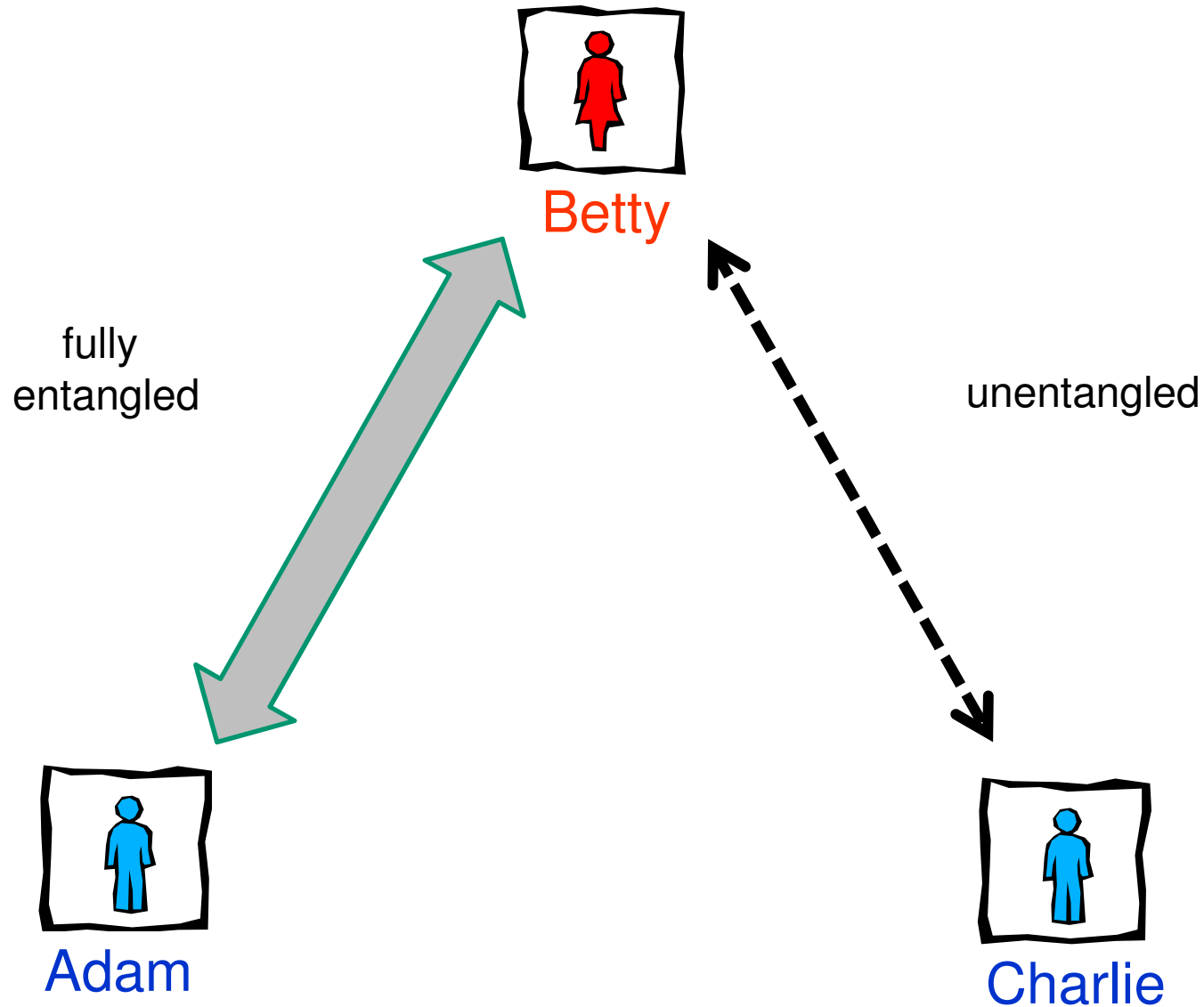
3. *How* will we build one?

What kind of quantum hardware is potentially scalable to large systems?

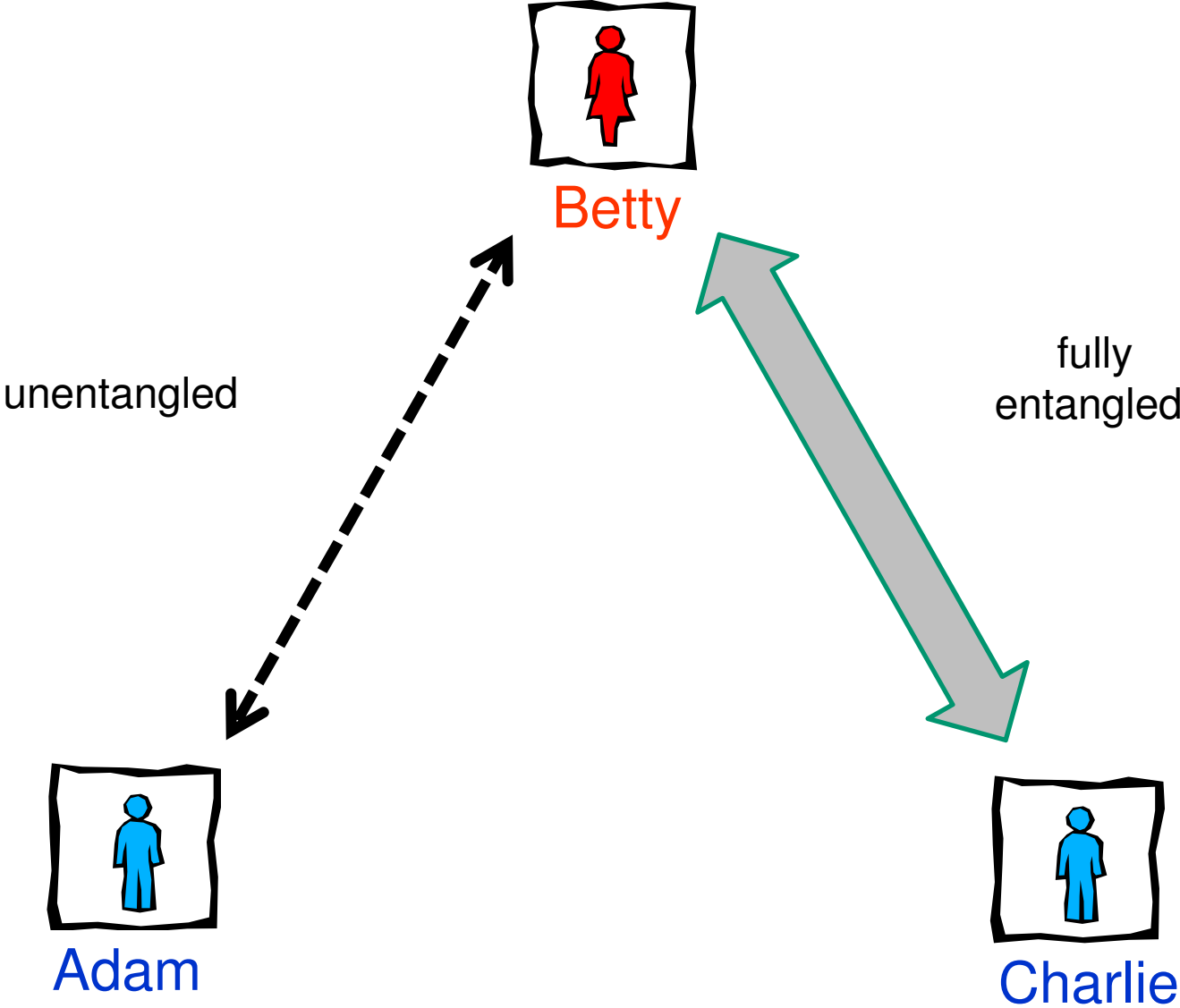
Classical correlations are polygamous



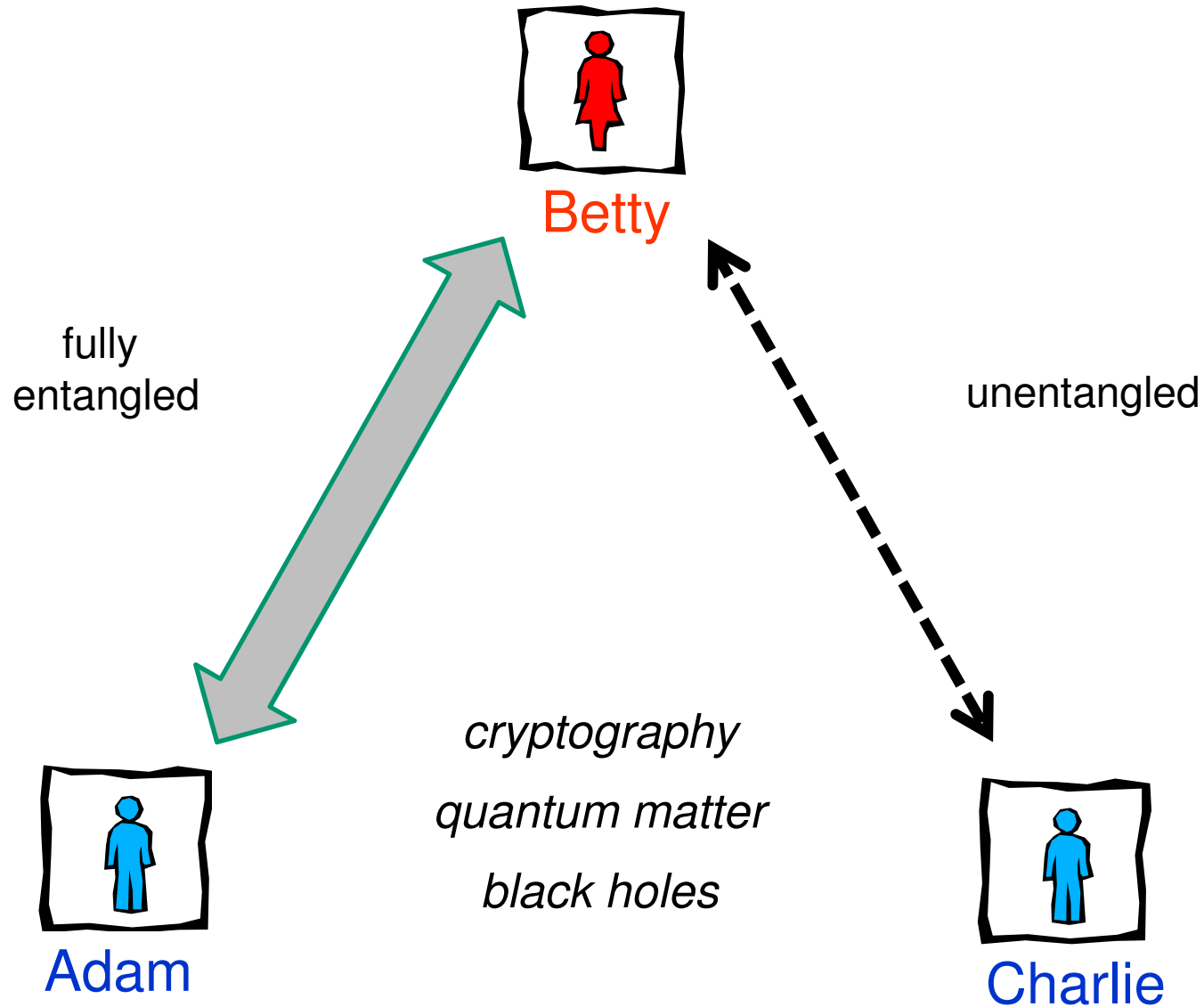
Quantum correlations are *monogamous*



Quantum correlations are *monogamous*



Monogamy is *frustrating!*



Information Puzzle:

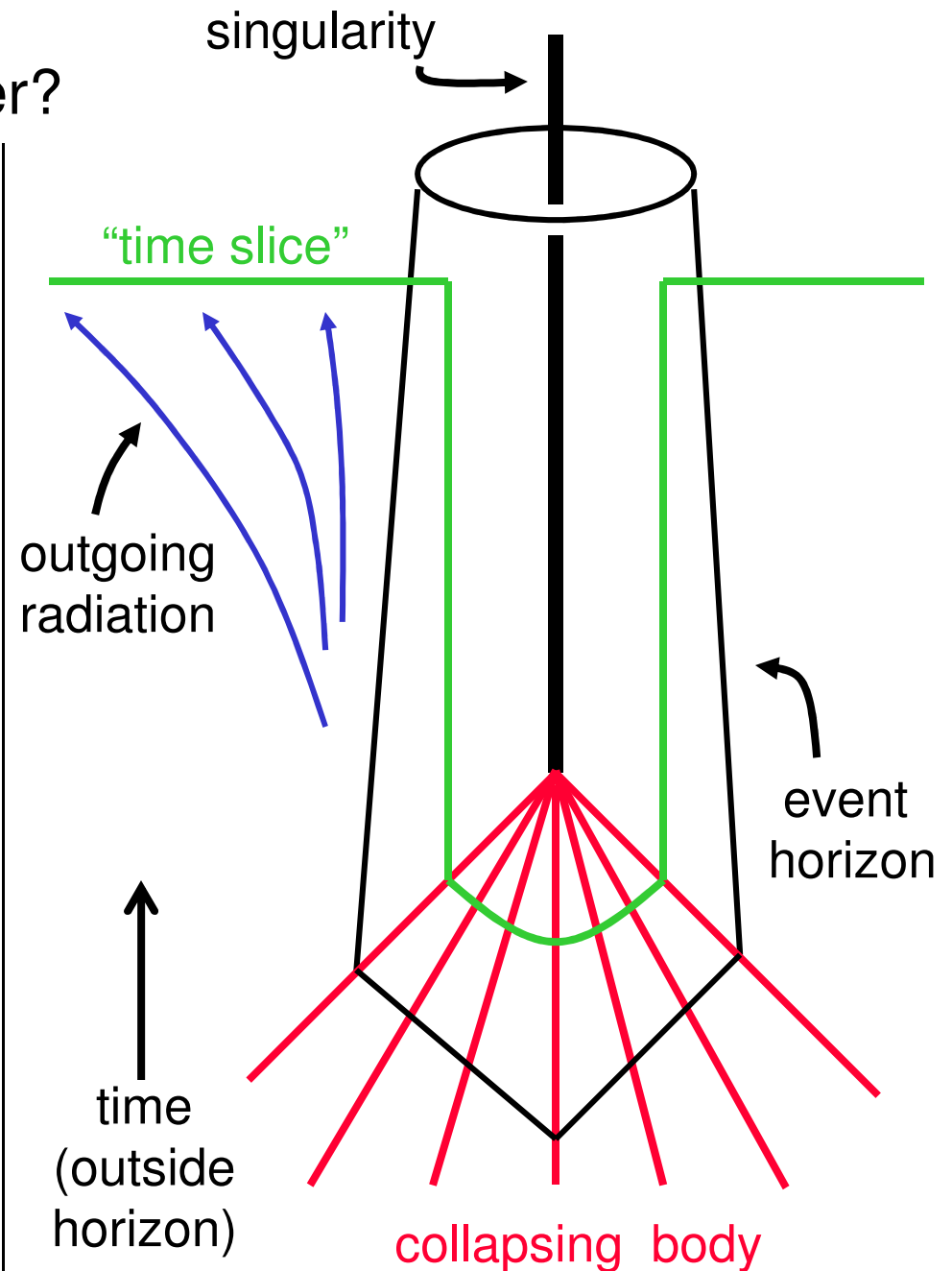
Is a black hole a quantum cloner?

Suppose that the collapsing body's quantum information is encoded in the emitted Hawking radiation; the information is *thermalized*, not destroyed.

The green time slice crosses both the collapsing body behind the horizon and nearly all of the radiation outside the horizon. *Thus the same (quantum) information is in two places at the same time.*

A quantum cloning machine has operated, which is not allowed by the linearity of quantum mechanics.

We're stuck: either information is destroyed or cloning occurs. Either way, quantum physics needs revision.

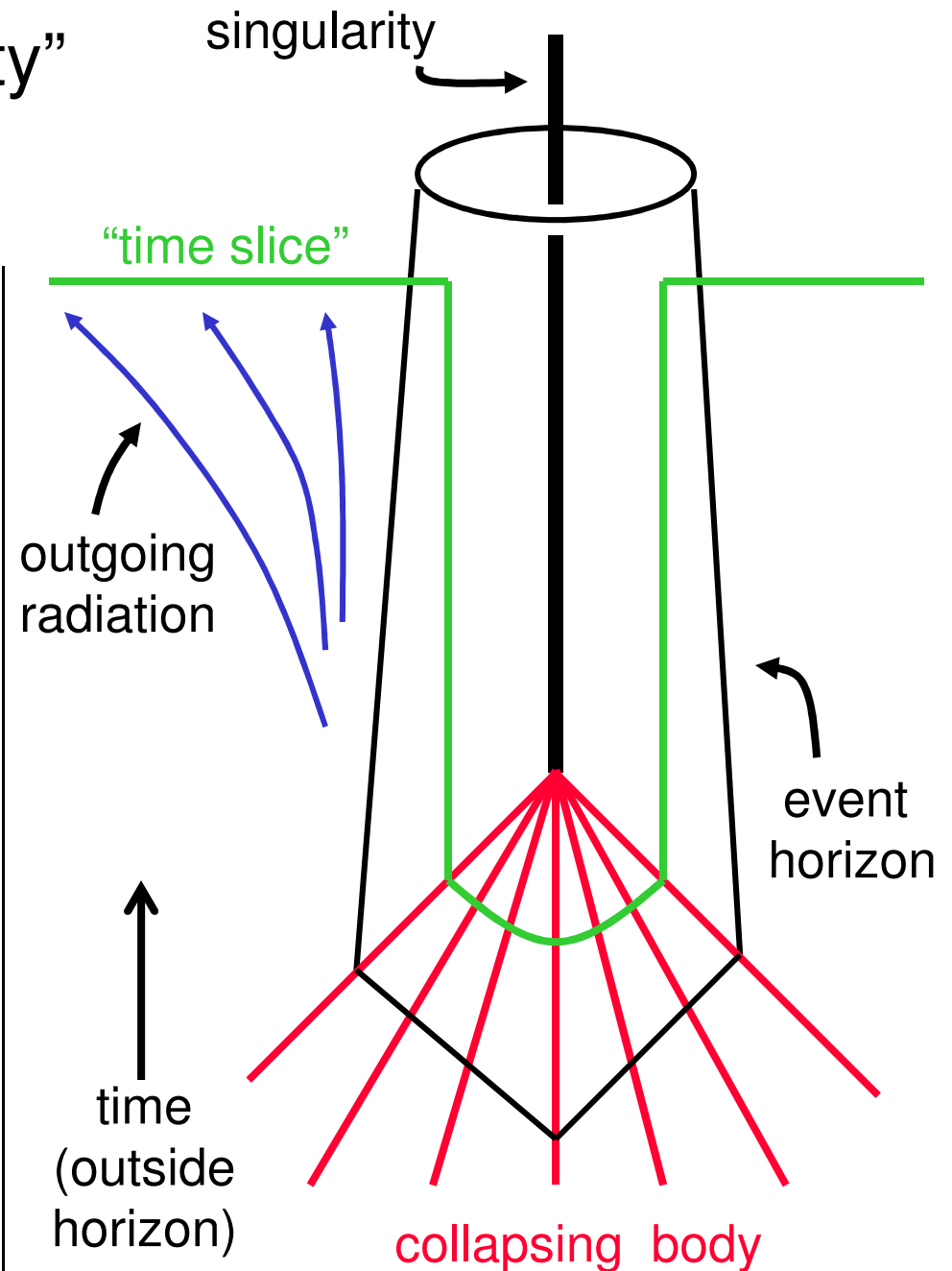


“Black hole complementarity”

Perhaps the lesson is that, for mysterious reasons that should be elucidated by a complete theory of quantum gravity, it is wrong to think of the “outside” and “inside” portions of the time slice as two separate subsystems of a composite system.

$$\mathcal{H} \neq \mathcal{H}_{\text{in}} \otimes \mathcal{H}_{\text{out}}$$

Rather, the inside and outside are merely complementary descriptions of the same system. Which description is appropriate depends on whether the observer enters the black hole or stays outside.

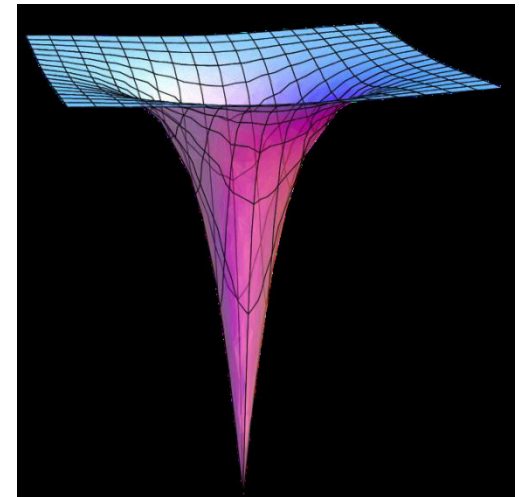
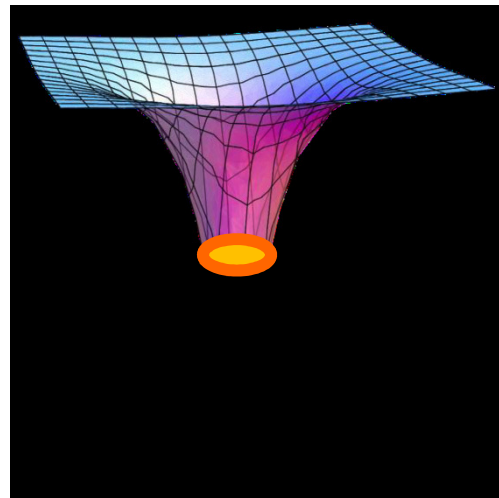


Black hole complementarity challenged

Three reasonable beliefs, not all true! [AMPS 2012]:

- (1) The black hole “scrambles” information, but does not destroy it.
- (2) An observer who falls through the black hole horizon sees nothing unusual (at least for a while).
- (3) An observer who stays outside the black hole sees nothing unusual.

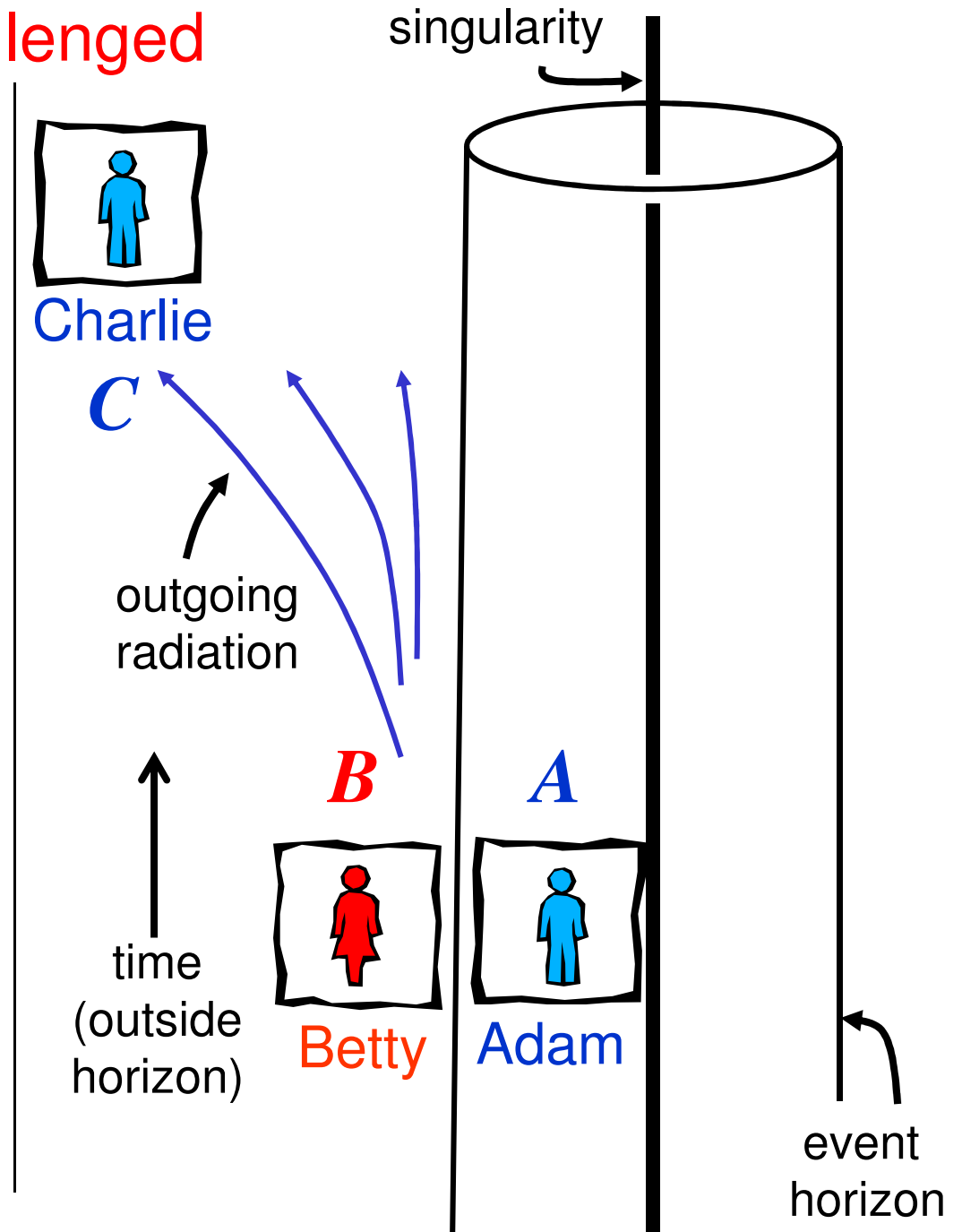
Conservative resolution:
A “firewall” at the horizon.



Complementarity Challenged

- (1) For an old black hole, recently emitted radiation (B) is highly entangled with radiation emitted earlier (C) by the time it reaches Charlie.
- (2) If freely falling observer sees vacuum at the horizon, then the recently emitted radiation (B) is highly entangled with modes behind the horizon (A).
- (3) If B is entangled with C by the time it reaches Charlie, it was already entangled with C at the time of emission from the black hole.

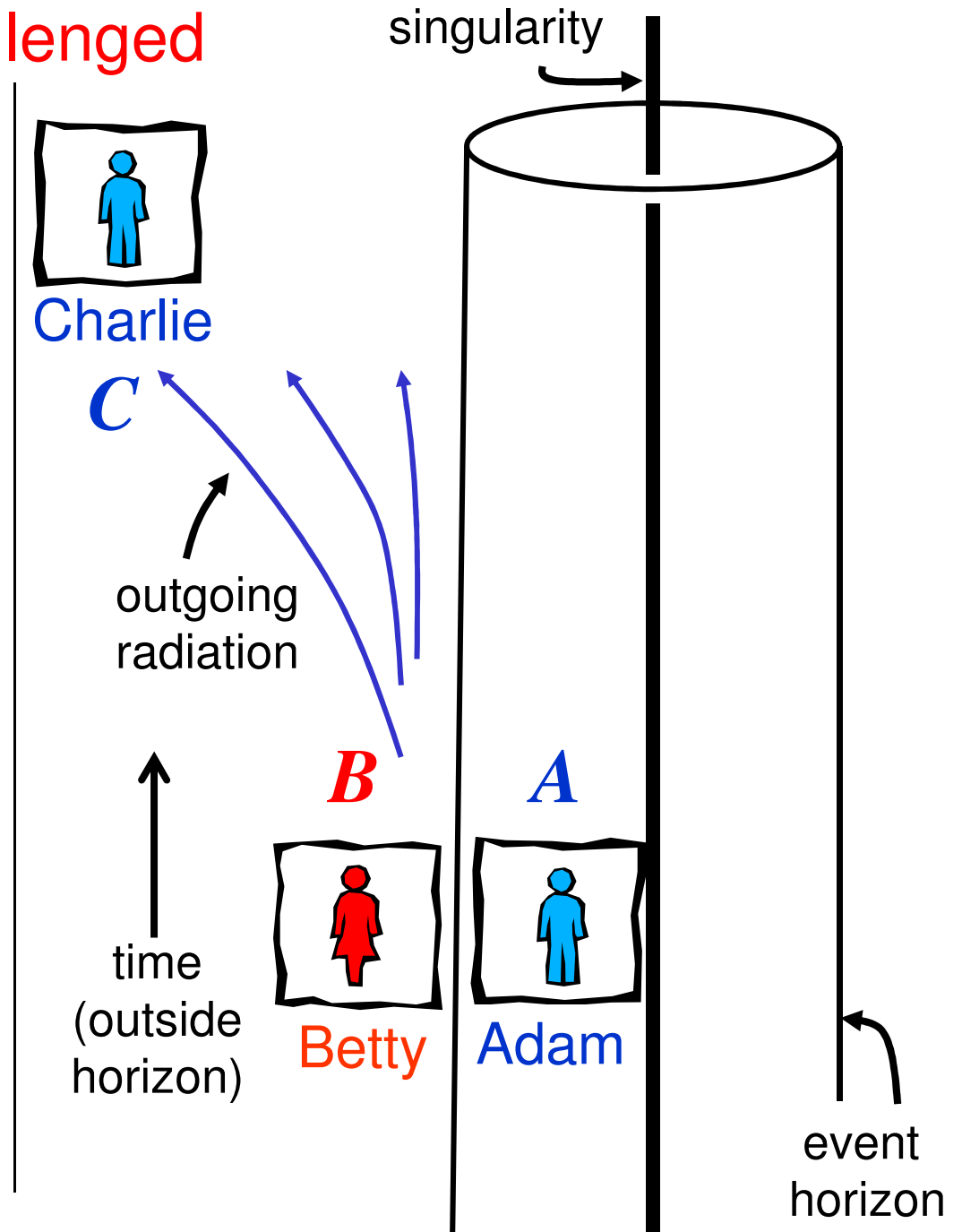
Monogamy of entanglement violated!



Complementarity Challenged

- (1) If A and B not entangled, a firewall at the horizon! Freely falling observer burns without warning.
- (2) If B and C not entangled, evolution is nonunitary and information is lost.
- (3) If B and C are entangled as B reaches C, but not before, entanglement is generated nonlocally.

It seems that a single observer ought to be able to verify both the BC entanglement and the AB entanglement, hence invoking complementarity does not seem to provide a pleasing resolution.



IQIM

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nature is subtle

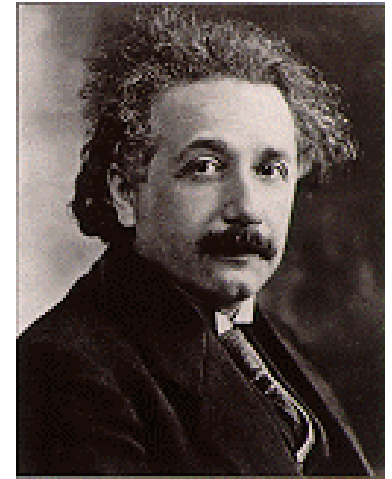
Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)

In a complete theory there is an element corresponding to each element of reality. A sufficient condition for the reality of a physical quantity is the possibility of predicting it with certainty, without disturbing the system. In quantum mechanics in the case of two physical quantities described by non-commuting operators, the knowledge of one precludes the knowledge of the other. Then either (1) the description of reality given by the wave function in

quantum mechanics is not complete or (2) these two quantities cannot have simultaneous reality. Consideration of the problem of making predictions concerning a system on the basis of measurements made on another system that had previously interacted with it leads to the result that if (1) is false then (2) is also false. One is thus led to conclude that the description of reality as given by a wave function is not complete.



“Nature is subtle” is a play on Einstein’s famous pronouncement: “Raffiniert ist der Herrgott aber boshaft ist er nicht” (**Subtle is the Lord, but malicious He is not**).

For all his genius, Einstein underestimated the subtlety of nature when he derisively dismissed quantum entanglement as “Spukhafte Fernwirkungen” (**Spooky action at a distance**). The aim of quantum information science is to relish, explore, and exploit the glorious subtlety of the quantum world in all its facets and ramifications.

Quantum computing and the entanglement frontier

