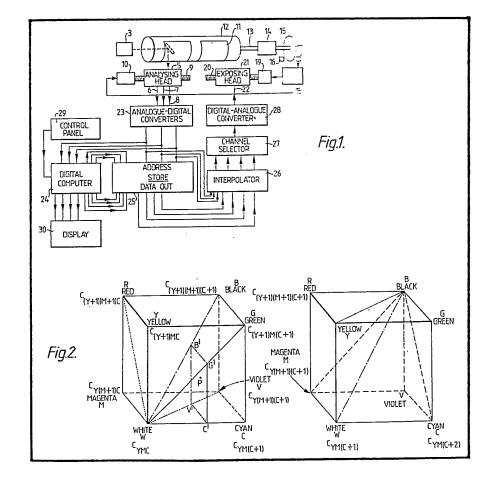
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(54) Improvements in Interpolation Methods and Apparatus

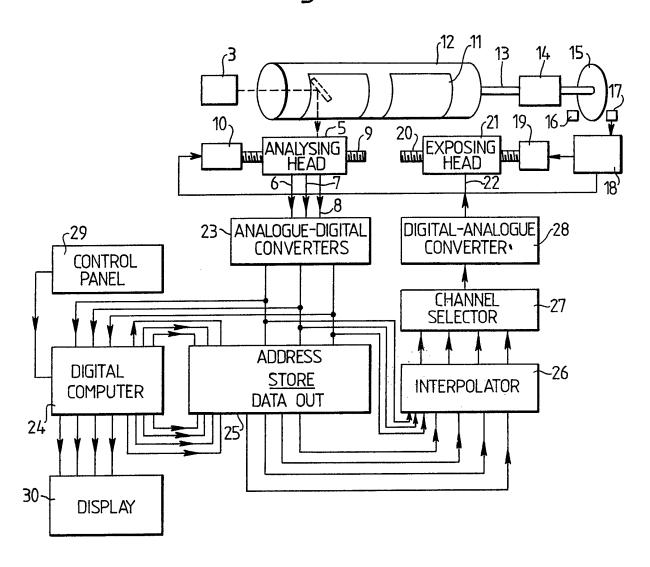
(57) The invention relates to methods and apparatus for interpolating between coarse stored data to achieve a more accurate answer, and is particularly applicable to colour scanning reprographic equipment. Colour scanners (5) analyse an original to obtain digital signals (8) representing three primary colour intensities. The values for the intensities of each of four printing

colours, including black, are functions of all three primary colour intensities, and a limited quantity of these sets of four values is stored as a three dimensional matrix (25), consisting of cubes with values at their corners. To obtain values from these coarse stored data corresponding to a point (P) within a cube, an interpolator (26) determines which one, of the three pyramids (e.g. W B G C V in Figure 2) comprising the cube, contains the point, and interpolates within that pyramid between the values at its five vertices.

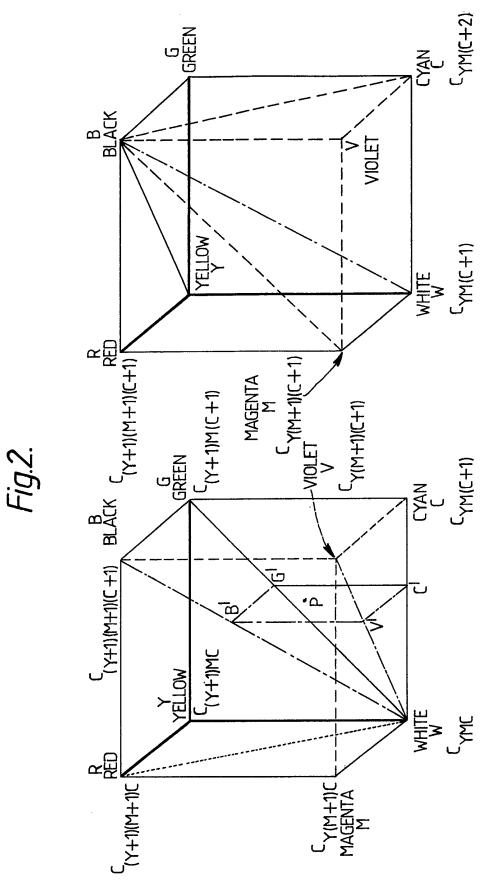


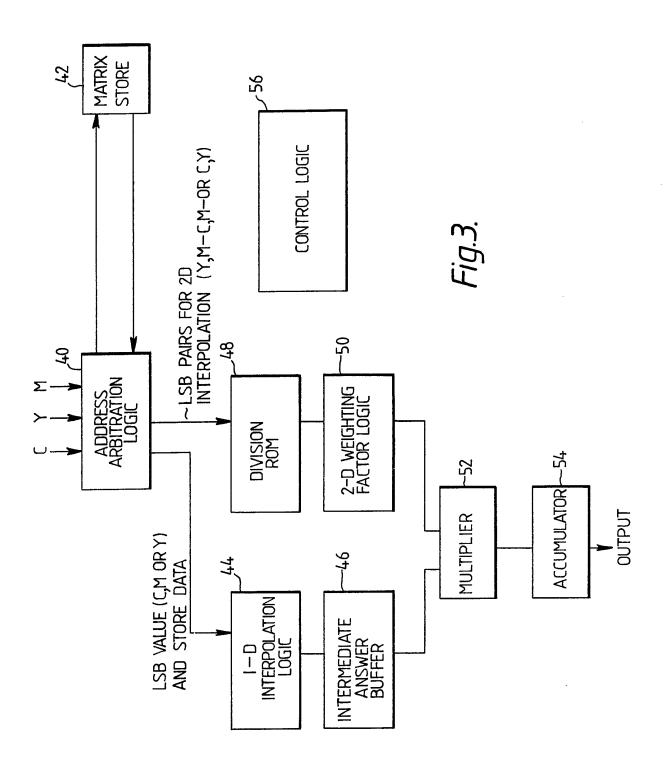
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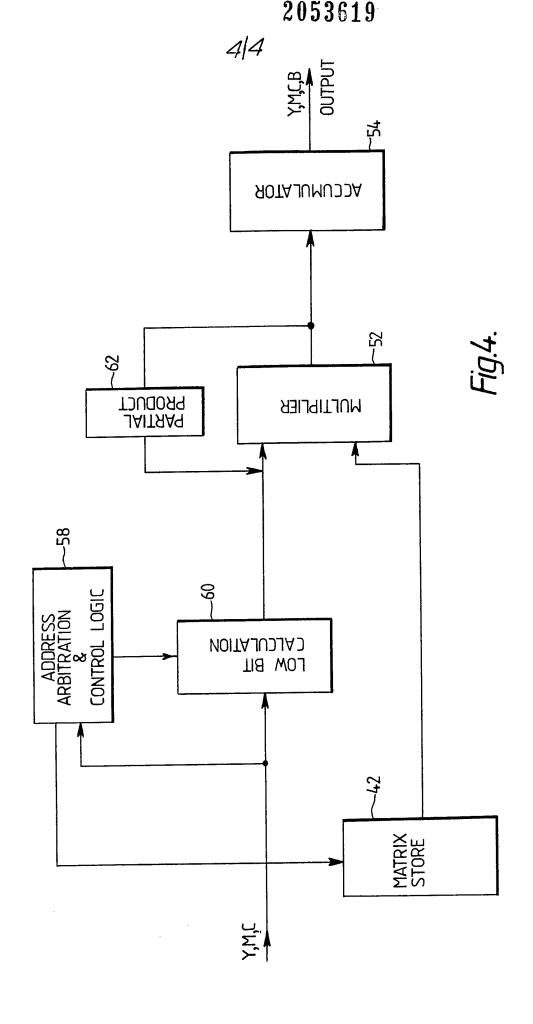
Fig.1.











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SPECIFICATION

Improvements in Interpolation Methods and Apparatus

This invention relates to methods and apparatus for interpolating between coarse stored data to achieve a more accurate answer. The invention is particularly applicable to colour scanning reprographic equipment.

In colour reproduction equipment, minicomputers and microprocessors are being utilised more and more to enable more powerful processing to be implemented. However, these colour scanners run at very high speeds and even the fastest computers cannot execute the required calculations in "realtime" for practical scanners.

A known solution to this problem is to set up the required reproduction characteristics and then to compute the output of the scanner for all possible input combinations and to store the output data in a "look-up table". In subsequent scanning of a picture, no processing needs to be done — the input values are merely used to address the look-up table to locate the required answer.

Colour scanners anlyse an original to be reproduced with three primary colour analysing 15 channels, and in a digital scanner these inputs must be quantised, preferably to at least eight bits, to 15 achieve a high quality print. This would give 224 possible input combinations and would necessitate a correspondingly large look-up table store which would be prohibitive in terms of cost and in the time taken to load it. A solution to this problem is given in our British Patent Specification No. 1,369,702, wherein the look-up table is computed only from the four most significant bits of each channel, giving 20 212 combinations. During scanning, the four most significant digits of each channel are used to address 20 this "coarse" look-up table, while the four least significant digits of each channel are used to interpolate between neighbouring points of the table.

The interpolator described in the above mentioned patent specification is a linear interpolator i.e. it assumes that the function being interpolated is linear within the space between the coarse table 25 points. This is not generally true and some error most occur since curves are being approximated to by a series of straight lines. In most cases the errors are small and quite acceptable but in some instances, in particular black printer generation, the errors can be serious. The present invention seeks to eliminate or reduce these errors.

Before defining the invention, the difficulties created by linear interpolation will be illustrated by 30 means of an example involving three-dimensional colour space, with reference to Figure 2 of the accompanying drawings which shows an interpolator "cube", i.e. the conceptual cube formed by an addressed point in the look-up table and the seven neighbouring points which would be addressed by incrementing by one "coarse" unit the four most significant bits of each channel singly and in all combinations.

Figure 2 shows an interpolator cube taken from a "linear matrix" of cyan values. The term linear matrix is used to describe a look-up table in which any input value addresses a location in store where the value itself is stored. In this case, whatever input comes in to the scanner the same value is obtained at the output. It will be appreciated that in general it is not possible to interpolate between a coarse signal C and the incremented signal C+1 solely from a consideration of the fraction c 40 represented by the least significant bits of the digital cyan signal; this is because the amount of cyan required is also affected by the values of the yellow and magenta signals.

If the linear matrix look-up table is addressed with the input combination

0010 0000=32 decimal 0000=32 decimal 0010 0000=32 decimal 0010

the interpolator cube addressed will be as shown in Figure 2 for cyan. Analogous cubes will be addressed for magenta, yellow and black, where a black printer is used. The point C_{Y,M,C} in Figure 2 represents the decimal value (32,32,32) referred to above and will be referred to as "white" for the purposes of the interpolation. The point $C_{(M+1)(Y+1)(C+1)}$, incremented by one coarse unit in each direction, thus represents in decimal terms a point (48,48,48). The values for c, y, m are given by the four least significant digits of the terms of the input combination and are expressed as fractions, i.e. the bit combination 1000, being a half of the basic "coarse" unit, gives a value of one half for the corresponding colour "remainder" m, y or c.

The known interpolator algorithm is:

55 Cyan output= $C_{YMC} \times (1-m)(1-y)(1-c)$ 55 $+C_{MY(C+1)}\times(1-m)(1-y)c$ $+C_{M(Y+1)c}\times(1-m)y(1-c)$ $+C_{M(Y+1)(C+1)}\times(1-m)yc$ $+C_{(M+1)YC}\times m(1-y)(1-c)$ (1) 60 $+C_{(M+1)Y(C+1)}\times m(1-y)c$ 60 $+C_{(M+1)(Y+1)C} \times my(1-c)$ $+C_{(M+1)(Y+1)(C+1)} \times myc$

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This algorithm states that the cyan output is the weighted average of the cyan value obtained by the initial address and the values which would have been addressed if the address bits were incremented in each colour direction, the weighting functions being determined by the low bit triple products. If a point P is chosen in the centre of the cube, the algorithm gives as output:

5 $32 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$ $+32 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$ $+48 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$ $=40 (y=m=c=\frac{1}{2}).$

This is exactly the right answer, being midway between 32 and 48.

The black printer however is determined by the lowest of the three colour signals — there is a large black content in neutral areas, but little in the pure colours. As a simplified example, take the case where the black printer value is equal to the lowest of the three input colour signals (in practice a more complicated function would be used). For this example, in terms of the interpolator cube of Figure 2 the black content would be 32 in all corners except the black corner which would have 48.

A similar calculation for the black printer, involving the terms Black_(Y,M,C) etc, would therefore give:

$$(7 \times 32 \times 1/8) + (1/8 \times 48) = 34$$

This is erroneous, as the true value should again be 40. The error arises because the algorithm is not able to resolve the non-linearity arising from the fact that black increases along the neutral axis, but 25 not along the colour directions.

For simplicity, in illustrating the black printer error in the example given above, a linear matrix look-up table has been assumed. It will be appreciated that in practice for colour scanner purposes such linear matrix look-up tables do not occur and that as a consequence the values obtained by interpolation for the colour components cyan, magenta and yellow are also in general incorrect due to the fact that the above-quoted interpolation algorithm operates in a linear manner while the function defined by the look-up table has curvature.

It will be recognised that in interpolation procedures, all polynomial methods of degree greater than one are ineffective when used across a singularity, such as the line singularity along the blackwhite diagonal in the case of the black printer discussed above. To take account of this, it is necessary to sub-divide the cube so that the black-white diagonal is an edge of the sub-divided volume.

In the case of a rectangle, it has been proposed to sub-divide the unit rectangle into triangles. Interpolation within triangles has been discussed, for example by R. H. Gallagher in "Finite Element Analysis Fundamentals", published by Prentice-Hall, New Jersey, 1975. In this publication, the author first discusses interpolation procedures for triangular elements and derives co-ordinate values for a point within the triangle, each co-ordinate value being the sum of three products, each product involving the rectangular co-ordinates of a respective corner of the triangle and the ratio of the area of a smaller triangle, defined by the other two corners and the point within the triangle, to the area of the triangle as a whole. Thereafter, the use of the tetrahedron, the three-dimensional counterpart of the planar triangle, is discussed and volume ratios are derived to replace the area ratios used in the case of the triangle.

The present invention consists in a method of reproducing a coloured original in which the original is scanned to obtain signals representing three colour-component densities of successively scanned picture elements of the original and in which the said signals are corrected before being used to control the treatment of an output surface, the method comprising, prior to the scanning of the 50 original, the steps of deriving for each of a number of sets of three input digital colour-component values, less in number than the sets of possible input digital colour-component values available from the scanner, a set of four corrected colour component values in digital form, one for each of the three colour components and one for black, and loading the sets of four corrected colour-component digital values into the storage locations of a three-dimensional store; and thereafter the steps of referring to 55 the store in accordance with the succession of sets of three colour-component signals derived from the scanning of the original to obtain from the store a succession of corrected digital values and of obtaining values intermediate the sets of digital values stored for unit cubes within the threedimensional store by on-line interpolation, and then controlling the treatment of the output surface in accordance with the four values obtained, and in which each of the four values for a point within a unit interpolation cube of the three-dimensional colour space is obtained by first determining in which of three pyramids, which together make up the unit interpolation cube and have as a common edge the "neutral axis" of the unit interpolation cube, the said point is contained, and then deriving a value for

the said point by interpolation within the pyramid.

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	To interpolate within the pyramid, a "parallel plane" method of linear interpolation is preferably	
	used.	
	The term "cube" has been used for brevity but is intended to cover any unit interpolation rectangular parallelepiped.	
5	The expression "neutral axis" as used in this specification is intended to mean the axis of	5
J	increasing blackness. Thus, "neutral axis" covers not only white-black axis for unit interpolation cubes so positioned in colour space that the white-black axis of colour space passes through them, but also the axis parallel to the white-black axis for unit interpolation cubes which do not have the white-black	
	axis passing through them. It will be seen that although a point on the "neutral axis" in these latter	10
10	cubes does not represent a grey tone, the axis is nevertheless an axis of increasing blackness. In order that the invention may be better understood, an example of colour reproduction	10
	equipment embodying the invention will now be described with reference to the accompanying	
	drawings, in which:	
	Figure 1 illustrates diagrammatically an apparatus and control circuit for image reproduction;	
15	Figure 2 illustrates the manner in which a unit cube of three-dimensional colour space is divided	15
	into pyramids for interpolation purposes;	
	Figure 3 is a diagram illustrating the manner in which the interpolation is carried out; and	
	Figure 4 is a diagram showing an alternative to the apparatus of Figure 3. In Figure 1, a transparent original 1 to be reproduced is wrapped around the surface of a	
20	transparent drum 2. A xenon lamp 3 directs light rays into the drum and on to a 45° mirror 4, from	20
20	which the rays pass through the wall of the drum and through the transparent original 1. These light	
	rays reach an analysing head 5 containing colour filters and photoelectric devices such that signals	
	representing the red, blue and green densities of the scanned element of the picture 1 are produced on	
	lines 6, 7 and 8 respectively. Because printing is carried out in subtractive colours, the lines 6, 7 and 8 will be considered to be part of the cyan, yellow and magenta colour channels. The analysing head 5 is	25
25	mounted on a lead screw 9 which is driven in synchronism with the rotation of the drum 2 by a motor	20
	10. As a consequence, the analysing head sees a point on the drum 2 which as the drum rotates and	
	the analysing head moves along its lead screw, traces out a helical path along the drum 2 and	
	consequently traces out a number of parallel scanning lines on the original 1.	20
30	A light-sensitive sheet 11 to be exposed is mounted on a drum 12, which in this case, has a larger diameter than the drum 2. Both drums are mounted on a shaft 13 driven by a motor 14. The	30
	motor also drives a slotted disc 15, the slotted periphery of which rotates between a light source 16	
	and a photoelectric cell 17. Pulses derived from the photoelectric cell 17 are applied to a control unit	
	18 which controls the rotation of the motor 10, driving the lead screw for the analysing head, and a	
35	motor 19 which drives a lead screw 20 on which is mounted an exposing head 21. The exposing head	35
	21 includes a light source which traces out a helical pattern on the drum 12 and which is modulated by a signal on a line 22. This signal is derived from the input signals on lines 6, 7 and 8 in the following	
	manner.	
	The signals on the lines 6, 7 and 8 are first applied to analogue-digital converters 23, the digital	
40	outputs of which can be connected to a digital computer 24 and also to a digital store 25 and an	40
	interpolator 26. The store 25 uses the three digitial signals from the converters 23 as address signals	
	and provides at its output four signals which are stored in the location represented by that address.	
	These four signals are the corrected signals for cyan, yellow and magenta, together with a black signal. The black signal is approximately equal to the smallest of the colour signals and the values of the	
45	colour signals obtained from the store are reduced in accordance with the value of the black signal. In	45
. •	effect, the store 25 is equivalent to 4 look-up tables, one for each of the three colour components and	
	one for black; each look-up table is addressed with each of the three input colour components signals.	
	In the example shown, the interpolator permits the required output-input relationship to be	
50	maintained for changes in signal level finer than would be permitted by the store 25, as will be described. A channel selector 27 receives the four signals, representing the cyan, yellow and magenta	50
30	printer values and the black printer value, and selects the one which corresponds to the separation to	
	be made with the light-sensitive sheet 11. This signal is converted into analogue form in the converter	
	28 and is then used to modulate the light source in the exposing head 21.	
	For the preliminary loading of the store with the matrix of output values, a control panel 29	55
55	enables parameter values to be set in accordance with the system characteristics and the characteristics of the original to be reproduced. These parameter values are entered into the digital	55
	computer, which is programmed to provide the required output-input relationship. A display 30 permits	
	the effect of this relationship and the effect of the parameter settings to be inspected before the matrix	
	of output values is calculated by the computer 24 and entered into the store 25.	
60	As an example, the parameter controls may be used to adjust tone compensation and to set any	60
	required "editorial" colour changes. The digital computer programme may take into account the transparency colour correction, the derivation of a black printer signal and the consequent removal of	

transparency colour correction, the derivation of a black printer signal and the consequent removal of

"undercolour" from the colour-component signals, the ink grey balance and the printing characteristic.
Figure 2 shows two "unit interpolation cubes" in which the division into pyramids is illustrated.
The three pyramids have in common the W-B line or "neutral axis" i.e. this line is an edge of all three

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pyramids. In the left cube, one of the three pyramids has the five vertices W, B, G, V and C, a second has the vertices W, Y, R, B and G, and the third has the vertices W, M, R, B and V. It will be seen that each of these pyramids has a base consisting of one complete face of the cube and has two sides each comprised of one half face of the cube. Also, the cyan, yellow and magenta corners (i.e. those corners corresponding to the printing inks), are all contained within different pyramids. In the right cube, the division into three pyramids is made so that the Black vertex, and not the White vertex, is common to all three pyramids. The cubes of the storage could be divided into pyramids in the same way, so that for example the cube on the left in Figure 2 would be repeated throughout the storage. However, the edges of the pyramids of different cubes would not then be aligned at adjacent cube faces, although 10 the results from this method of interpolation are satisfactory, the results can be improved by ensuring 10 that no edge of any pyramid lies across a face of any other pyramid. The interpolation is more efficient if the pyramids of adjacent cubes share the same edges. Preferably, alternate cubes of the storage are divided according to the left and the right cubes of Figure 2. Thus each cube divided with the White vertex common to three pyramids is surrounded by six cubes of the type with the Black vertex common 15 to three pyramids, and vice versa. All the cubes of a given type have the same orientation, as shown in 15 Figure 2. With this arrangement, the edges of adjacent pyramids are matched; for example the Red/White diagonal in the cube on the left of Figure 2 is matched with the Black/Cyan diagonal of a cube similar to the cube on the right of Figure 2. The following description applies to this preferable system of division. 20 In carrying out the interpolation, the first step is to choose the pyramid in which lies the point for 20

which interpolation is required. This depends on the "low bits" of the colour channel signals; the high bits define the unit interpolation cube in which the point falls and the low bits define the position of that point within the selected cube. For the cube on the left in Figure 2, the point lies in one of the pyramids according to which of the colour channel signals has the highest value in its low bits. For the 25 cube on the right, which divides into three different pyramids, the point lies in one of the pyramids according to which of the colour channel signals has the lowest value in its low bits. For example, a point at which the cyan low bits have the lowest value must be placed in the pyramid whose vertices are W, B, R, M and Y. With the cube on the left of Figure 2, when the cyan channel has the highest value of "low bits" the pyramid chosen is the one having for its vertices W, B, C, G and V. When 30 magenta has the highest low bits, the selected pyramid is that having for its vertices W, B, R, M and V. Finally for the case in which the yellow channel has the highest low bits, the pyramid selected has the vertices W, B, G, Y and R.

If the low bits of all three channels are equal, it does not matter which pyramid is chosen, since the point lies on the common "neutral axis".

In the left cube in Figure 2, the pyramid shown is that which is used when the cyan low bits are highest. For a "parallel plane" method of interpolation, the procedure is as follows. First the square base BGCV of the pyramid is projected on to the parallel plane B'G'C'V', which is the plane for the cyan low-bit value and therefore passes through the point for which interpolation is required.

The output values at the points B'G'C'V' are obtained by linear interpolation along the lines 40 WB'B, WG'G and WV'V using the cyan low bits:-

$$B'=W(1-c)+B.c$$
 (1a)
 $G'=W(1-c)+G.c$ (1b)
 $C'=W(1-c)+C.c$ (1c)
 $V'=W(1-c)+V.c$ (1d)

The final answer is obtained from these four intermediate values by two-dimensional interpolation within the square B'G'C'V' using the yellow and magenta low bits. The yellow and magenta low bits must be scaled by the cyan low bits to give the proper weights to the points B'G'C'V', the scaled values being

Final Output

Figure 3 shows diagrammatically one embodiment of apparatus for carrying the invention into effect. In Figure 3, the picture signal values are fed into an "address arbitration logic" block 40 which selects which of the three pyramids encloses the interpolation point and thus which five corners of the cube must be addressed. The white point is always addressed and is obtained first from the matrix

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store 42. The next point obtained from the matrix store is the Black point, for example. The white and black values W, B and the cyan LSB (least significant bit) are supplied to a linear 1-dimensional interpolation unit 44 in which a linear interpolation is performed between the White and Black points using the cyan LSB (least significant bit) value. This gives the intermediate answer B' according to equation (1a) and B' is then stored in a buffer store 46. The address arbitration logic 40 also determines which two LSB values are needed for the subsequent 2-dimensional interpolation, in this example y and m, and supplies these to the division ROM 48. The y and m values must be scaled by dividing by the c value; the resulting values y' and m' are transferred to a two-dimensional weighting factor calculator 50, which provides at its output a value y'm' or y'(1-m'), for example. The intermediate answer B' is then fed to a multiplier 52 where it is multiplied by a weighting factor (in this case y'm') according to equation (2a). The result of this multiplication is stored in an accumulator 54.

Next the Green point, say, is obtained and subjected to 1-dimensional and 2-dimensional interpolation according to equations (1b) and (2b). The result is added to the accumulator. The process is repeated for the Cyan and Violet corners and the final result can then be taken from the accumulator.

Next, the whole process may be repeated for yellow, magenta and black colours. Alternatively, it may be that only one or two colour separations are required, in which case only the corrected colour component values for those colours that are required are extracted from the matrix store.

The sequence of operations is controlled by a control unit 56. The process described above involves extracting up to four corrected colour component values from the matrix store and processing 20 them in sequence. However, they may be extracted in sets of two or more, and processed in parallel, for example using two or more sets of the processing units of Figures 3 or 4.

Figure 4 shows an alternative embodiment of apparatus according to the invention. In Figure 4, the picture signal values are fed into a unit 58 for address arbitration and control logic, which performs the functions of the units labelled 40 and 56 in Figure 3. The matrix store 42 is addressable by the unit 25 58, and stores the five values at the vertices of the pyramid containing the point corresponding to the picture signal values. A low bit calculation unit 60 is responsible for the derivation of the scaled values, for example y'm', as described above.

The multiplier unit 52 multiplies the values (e.g. B, W) from the matrix store 42 by scaled values from the low bit calculation unit 60, intermediate products being fed back to the multiplier unit 52 via a partial product unit 62. The final output value is obtained by accumulating and adding the products from the multiplier unit 52, as described above.

The address arbitration logic unit 40, or the address arbitration and control logic unit 58, may decide which pyramid contains the point by the following method.

If there are two alternating types of cube, as shown in Figure 2, then the first task is to determine 35 which type of cube contains the point. The fourth most significant bit of each channel signal is used in this determination. The MSB co-ordinates of adjacent cubes differ in this fourth bit. It will be appreciated that the sum of the fourth MSB's from the three colour channel signals is either odd or even; this determines which type of cube contains the point represented by those signals. For example, if the sum of the fourth MSB's is even, it will end in "O", and it is determined that the point is in a cube 40 of the type shown on the left of Figure 2.

The next task is to compare the values of the LSB's of the colour channel signals. For the left cube, the point lies in whichever pyramid has, as one of its vertices, the colour with the highest value in the LSB's. For the right cube, the point lies in whichever pyramid does not have, as one of its vertices, the colour with the lowest value in the LSB's.

45 Claims

45 1. A method of reproducing a coloured original in which the original is scanned to obtain signals representing three colour-component densities of successively scanned picture elements of the original and in which the said signals are corrected before being used to control the treatment of an output surface, the method comprising, prior to the scanning of the original, the steps of deriving, for each of a number of sets of three input digital colour-component values less in number than the sets of possible 50 input digital colour-component values available from the scanner, a set of four corrected colour component values in digital form, one for each of the three colour components and one for black, and loading the sets of four corrected colour-component digital values into the storage locations of a threedimensional store; and thereafter the steps of referring to the store in accordance with the succession 55 of sets of three colour-component signals derived from the scanning of the original to obtain from the 55 store a succession of corrected digital values and of obtaining values intermediate the sets of digital values stored for unit cubes within the three-dimensional store by on-line interpolation, and then controlling the treatment of the output surface in accordance with the four values obtained, and in which each of the four values for a point within a unit interpolation cube of the three-dimensional colour space is obtained by first determining in which of three pyramids, which together make up to the 60 unit interpolation cube and have as a common edge the "neutral axis" of the unit interpolation cube, the said point is contained, and then deriving a value for the said point by interpolation within the

pyramid. 2. A method in accordance with claim 1, in which the unit cubes are divided into three pyramids

each with a vertex at the "white" corner or each at the "black" corner, wherein any two adjacent cubes are divided in these two different ways, so that no edge of any pyramid lies across a face of another pyramid.

3. A method in accordance with claim 1 or 2, in which the interpolated value is obtained by first obtaining interpolated values for the corners of a plane intersecting the pyramid and parallel to its base and containing the required point, and then interpolating within the said plane to obtain a value for the said point.

4. Apparatus for reproducing a coloured original, comprising a scanner for analysing the original to obtain three signals representing three colour-component densities of successively scanned picture 10 elements, an analogue-to-digital converter, a digital memory storing for each of a number of sets of three digital colour-component values, a set of values comprising corrected values for the three colourcomponents and a black printer value, the said number being less than the number of digital values which can be provided by the said converter, means operable to refer to the store in accordance with the succession of sets of three colour-component signals derived from the original by the scanner to 15 obtain from the store a succession of signal values for controlling the means for treating the output surface, and an interpolator operating on-line in accordance with the signals derived from the scanner to provide sets of corrected colour-component values intermediate the sets of stored digital values, and in which the interpolation unit comprises means for determining in which of three pyramids making up a unit interpolation cube in three-dimensional colour-space, the required point is contained, and means 20 for interpolating within the said pyramid to obtain a value for the required point.

5. Apparatus in accordance with claim 4, in which the interpolation unit divides the unit cubes into three pyramids each with a vertex at the "white" corner or each at the "black" corner, wherein any two adjacent cubes are divided in these two different ways, so that no edge of any pyramid lies across a face of another pyramid.

6. Apparatus in accordance with claim 4 or 5, in which the interpolation unit includes means for obtaining interpolated values for each of the four corners of a plane parallel to the base of the selected pyramid and containing the required point; and means for interpolating linearly within the said plane to obtain a value for the required point.

A method or apparatus for reproducing a coloured original, substantially as described herein 30 with reference to the accompanying drawings.

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