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MEASURING FINANCIAL ASSET RETURN AND VOLATILITY SPILLOVERS,  
WITH APPLICATION TO GLOBAL EQUITY MARKETS

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Measuring Financial Asset Return and Volatility Spillovers, With Application to Global Equity Markets

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**ABSTRACT**

We provide a simple and intuitive measure of interdependence of asset returns and/or volatilities. In particular, we formulate and examine precise and separate measures of return spillovers and volatility spillovers. Our framework facilitates study of both non-crisis and crisis episodes, including trends and bursts in spillovers, and both turn out to be empirically important. In particular, in an analysis of nineteen global equity markets from the early 1990s to the present, we find striking evidence of divergent behavior in the dynamics of return spillovers vs. volatility spillovers: Return spillovers display a gently increasing trend but no bursts, whereas volatility spillovers display no trend but clear bursts.

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## 1. Introduction

For many years but especially following the late 1990s Asian crisis, much has been made of the nature of financial market interdependence, both in terms of returns and return volatilities (e.g., King, Sentana and Wadhvani, 1994; Forbes and Rigobon, 2002). Against this background, we propose a simple quantitative measure of such interdependence, which we call a spillover index, and associated tools that we call spillover tables and spillover plots.

The intensity of spillovers may of course vary over time, and the nature of any time-variation is of potentially great interest. We allow for it in an analysis of a broad set of global equity returns and volatilities from the early 1990s to the present, and we show that spillovers are important, spillover intensity is indeed time-varying, and the nature of the time-variation is strikingly different for returns vs. volatilities.

We proceed by proposing the spillover index in Section 2 and describing our global equity data in Section 3. We perform a full-sample spillover analysis in Section 4 and a rolling-sample analysis allowing for time-varying spillovers in Section 5. We briefly assess the robustness of our results in section 6, and we summarize and conclude in Section 7.

## 2. The Spillover Index

We base our measurement of return and volatility spillovers on vector autoregressive (VAR) models in the broad tradition of Engle, Ito and Lin (1990). Our approach, however, is very different. We focus on variance decompositions, which are already well-understood and widely-calculated. As we will show, they allow us to aggregate spillover effects across markets, distilling a wealth of information into a single spillover measure.

The basic spillover index idea is simple and intuitive, yet rigorous and replicable, following directly from the familiar notion of a variance decomposition associated with an N-variable VAR. Roughly, for each asset  $i$  we simply add the shares of its forecast error variance coming from shocks to asset  $j$ , for all  $j \neq i$ , and then we add across all  $i = 1, \dots, N$ .

To minimize notational clutter, consider first the simple example of a covariance stationary first-order two-variable VAR,

$$x_t = \Phi x_{t-1} + \varepsilon_t,$$

where  $x_t = (x_{1,t}, x_{2,t})'$  and  $\Phi$  is a 2x2 parameter matrix. In our subsequent empirical work,  $x$  will be either a vector of stock returns or a vector of stock return volatilities. By covariance stationarity, the moving average representation of the VAR exists and is given by

$$x_t = \Theta(L)\varepsilon_t,$$

where  $\Theta(L) = (I - \Phi L)^{-1}$ . It will prove useful to rewrite the moving average representation as

$$x_t = A(L)u_t,$$

where  $A(L) = \Theta(L)Q_t^{-1}$ ,  $u_t = Q_t\varepsilon_t$ ,  $E(u_t u_t') = I$ , and  $Q_t^{-1}$  is the unique lower-triangular Cholesky factor of the covariance matrix of  $\varepsilon_t$ .

Now consider 1-step-ahead forecasting. Immediately, the optimal forecast (more precisely, the Wiener-Kolmogorov linear least-squares forecast) is

$$x_{t+1,t} = \Phi x_t,$$

with corresponding 1-step-ahead error vector

$$e_{t+1,t} = x_{t+1} - x_{t+1,t} = A_0 u_{t+1} = \begin{bmatrix} a_{0,11} & a_{0,12} \\ a_{0,21} & a_{0,22} \end{bmatrix} \begin{bmatrix} u_{1,t+1} \\ u_{2,t+1} \end{bmatrix},$$

which has covariance matrix

$$E(e_{t+1,t} e_{t+1,t}') = A_0 A_0'.$$

Hence, in particular, the variance of the 1-step-ahead error in forecasting  $x_{1t}$  is  $a_{0,11}^2 + a_{0,12}^2$ , and the variance of the 1-step-ahead error in forecasting  $x_{2t}$  is  $a_{0,21}^2 + a_{0,22}^2$ .

Variance decompositions allow us to split the forecast error variances of each variable into parts attributable to the various system shocks. More precisely, for the example at hand, they answer the questions: What fraction of the 1-step-ahead error variance in forecasting  $x_1$  is due to shocks to  $x_1$ ? Shocks to  $x_2$ ? And similarly, what fraction of the 1-step-ahead error variance in forecasting  $x_2$  is due to shocks to  $x_1$ ? Shocks to  $x_2$ ?

Let us define *own variance shares* to be the fractions of the 1-step-ahead error variances in forecasting  $x_i$  due to shocks to  $x_i$ , for  $i=1, 2$ , and *cross variance shares, or spillovers*, to be the fractions of the 1-step-ahead error variances in forecasting  $x_i$  due to shocks to  $x_j$ , for  $i, j=1, 2$ ,  $i \neq j$ . There are two possible spillovers in our simple two-variable example:  $x_{1t}$  shocks that affect the forecast error variance of  $x_{2t}$  (with contribution  $a_{0,21}^2$ ), and  $x_{2t}$  shocks that affect the forecast error variance of  $x_{1t}$  (with contribution  $a_{0,12}^2$ ). Hence the total spillover is  $a_{0,12}^2 + a_{0,21}^2$ . We can convert total spillover to an easily-interpreted index by expressing it relative to total forecast error variation, which is  $a_{0,11}^2 + a_{0,12}^2 + a_{0,21}^2 + a_{0,22}^2 = \text{trace}(A_0 A_0')$ . Expressing the ratio as a percent, the *Spillover Index* is

$$S = \frac{a_{0,12}^2 + a_{0,21}^2}{\text{trace}(A_0 A_0')} \cdot 100.$$

Having illustrated the Spillover Index in a simple first-order two-variable case, it is a simple matter to generalize it to richer dynamic environments. In particular, for a  $p^{\text{th}}$ -order  $N$ -variable VAR (but still using 1-step-ahead forecasts) we immediately have

$$S = \frac{\sum_{\substack{i,j=1 \\ i \neq j}}^N a_{0,ij}^2}{\text{trace}(A_0 A_0')} \cdot 100,$$

and for the fully general case of a  $p^{\text{th}}$ -order  $N$ -variable VAR, using  $H$ -step-ahead forecasts, we have

$$S = \frac{\sum_{h=0}^{H-1} \sum_{\substack{i,j=1 \\ i \neq j}}^N a_{h,ij}^2}{\sum_{h=0}^{H-1} \text{trace}(A_h A_h')} \cdot 100.$$

Such generality is often useful. In much of the empirical work that follows, for example, we use second-order 19-variable VARs with 10-step-ahead forecasts.

### 3. Global Equity Market Return and Volatility Data

Our underlying data are daily nominal local-currency stock market indexes, January 1992 – November 2007, taken from Datastream and Global Financial Data. We examine seven developed stock markets (for the U.S., U.K., France, Germany, Hong Kong, Japan and Australia) and twelve emerging markets (Indonesia, South Korea, Malaysia, Philippines, Singapore, Taiwan, Thailand, Argentina, Brazil, Chile, Mexico, and Turkey).

We calculate returns as the change in log price, Wednesday-to-Wednesday. When price data for Wednesday are not available due to a holiday, we use Thursday. We then convert weekly returns from nominal to real terms using monthly consumer price indexes from the IMF's *International Financial Statistics*. To do so we assume that the weekly inflation rate  $\pi_t$  is constant within the month, in which case we can calculate it simply as the 1/4<sup>th</sup> power of the monthly inflation rate, and we then calculate the weekly real return as  $\frac{1+i_t}{1+\pi_t} - 1$ , where  $i_t$  is the weekly nominal return. We provide a variety of descriptive statistics for returns in Table 1.

We assume that volatility is fixed within periods (in this case, weeks) but variable across periods. Then, following Garman and Klass (1980) and Alizadeh, Brandt and Diebold (2002), we can use weekly high, low, opening and closing prices obtained from underlying daily high/low/open/close data to estimate weekly stock return volatility:

$$\tilde{\sigma}^2 = 0.511(H_t - L_t)^2 - 0.019[(C_t - O_t)(H_t + L_t - 2O_t) - 2(H_t - O_t)(L_t - O_t)] - 0.383(C_t - O_t)^2,$$

where  $H$  is the Monday-Friday high,  $L$  is the Monday-Friday low,  $O$  is the Monday open and  $C$  is the Friday close (all in natural logarithms). We provide descriptive statistics for volatilities in Table 2.

### 4. Full-Sample Analysis: Spillover Tables

Here we provide a full-sample analysis of global stock market return and volatility spillovers. As part of that analysis, we propose decomposing the Spillover Index into all of the forecast error variance components for variable  $i$  coming from shocks to variable  $j$ , for all  $i$  and  $j$ .

We begin by characterizing return and volatility spillovers over the entire sample, January 1992-November 2007. Subsequently we will track time variation in spillovers via rolling window estimation.) We report Spillover Indexes for returns and volatility in the lower right corners of Tables 3 and 4, respectively. Before discussing them, however, let us describe the rest

of the two tables, which we call *Spillover Tables*. The  $ij^{th}$  entry in the table is the estimated contribution to the forecast error variance of country  $i$  (returns in Table 3, volatility in Table 4) coming from innovations to country  $j$  (again, returns in Table 3, volatility in Table 4).<sup>1</sup> Hence the off-diagonal column sums (labeled Contributions to Others) or row sums (labeled Contributions from Others), when totaled across countries, give the numerator of the Spillover Index. Similarly, the column sums or row sums (including diagonals), when totaled across countries, give the denominator of the Spillover Index.

The Spillover Table, then, provides an “input-output” decomposition of the Spillover Index. For example, we learn from Spillover Table 3 (for returns) that innovations to U.S. returns are responsible for 22.2 percent of the error variance in forecasting 10-week-ahead Mexican returns, but only 3.0 percent of the error variance in forecasting 10-week-ahead Turkish returns. That is, return spillovers from the U.S. to Mexico are larger than for the U.S. to Turkey. As another example, we see from Table 4 (volatility) that total volatility spillovers from Hong Kong to others (that is, Hong Kong Contributions to Others) are much larger than total volatility spillovers from others to Hong Kong (Hong Kong Contributions from Others).

The key substantive summary result to emerge from Tables 3 and 4 is that, distilling all of the various cross-country spillovers into a single Spillover Index for our full 1992-2007 data sample, we find that almost forty percent of forecast error variance comes from spillovers, both for returns (36 percent) and volatilities (40 percent). Hence spillovers are important in both returns and volatilities, and on average – that is, unconditionally – return and volatility spillovers are of the same magnitude.

However, at any given point in time – that is, conditionally – return and volatility spillovers may be very different, and more generally, their dynamics may be very different. We now substantiate these assertions by moving from a static full-sample analysis to a dynamic rolling-sample analysis.

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<sup>1</sup> The results are based on weekly vector autoregressions of order 2 (selected using the Schwarz criterion), identified using a Cholesky factorization with the ordering as shown in the column heading, and 10-week-ahead forecasts.

## 5. Rolling-Sample Analysis: Spillover Plots

Clearly, many changes took place during the years in our sample, 1992-2007. Some are well-described as more-or-less continuous evolution, such as increased linkages among global financial markets and increased mobility of capital, due to globalization, the move to electronic trading, and the rise of hedge funds. Others are better described as bursts that subsequently subside, such as the various Asian currency crises around 1997.

Given this background of financial market evolution and turbulence, it seems unlikely that any single fixed-parameter model would apply over the entire sample. Hence the full-sample Spillover Tables and Spillover Indexes obtained earlier, although providing a useful summary of “average” behavior, likely miss the potentially important secular and cyclical movements in spillovers. To address this issue, we now estimate the models using 200-week rolling samples, and we assess the extent and nature of spillover variation over time via the corresponding time series of Spillover Indexes, which we examine graphically in *Spillover Plots*.

We present the Spillover Plot for returns in Figure 1. It is largely uneventful, displaying a gently increasing trend, but little else. Notice that even as the estimation window moves beyond the mid-1990s, the return Spillover Plots never decline to their earlier lower range. This is consistent with a maintained increase in financial market integration. In recent years, however, the upward trend in the return Spillover Plot has become steeper.

We also present the Spillover Plot for volatility in Figure 1. It is radically different, ranging widely and responding to economic events. Some of those events are major, including (1) the East Asian currency crisis in late 1997 (the devaluation of Thai Baht in July 1997, the spread to Hong Kong in October 1997, and further spread to other major economies in the region such as South Korea, Malaysia and Indonesia through January 1998), (2) the June-August 1998 Russian crisis (the first wave was controlled by the IMF’s announcement of a support package in June 1998, and the final outbreak occurred in August 1998), (3) the intense reversal of capital flows from emerging markets following strong signals from the U.S. Federal Reserve of likely additional hikes in the Fed Funds rate during May-June 2006, and finally, (4) the financial market turmoil associated with the subprime mortgage market that started in July-August 2007, as well as the first signs of the problem in march 2007.



Additional important events generating volatility spillovers include (1) the Brazilian crisis of January 1999, (2) the U.S. terrorist attack of September 11, 2001, and (3) the “dollar crisis” of March 2005, associated with remarks from policy makers in several emerging and industrialized countries (South Korea, Russia, China, India and Japan) indicating that they were considering central bank reserve diversification away from the U.S. dollar. In any event, the key insight is that many well-known events produced large volatility spillovers, whereas, with the possible exception of the recent subprime episode (which generates the highest value of the volatility Spillover Index since the East Asian crisis of 1997-1998), *none* produced return spillovers.<sup>2</sup>

## 6. Robustness

We now perform some simple variations on our basic analysis, with an eye toward checking robustness with respect to the rolling window width, the forecast horizon, and the ordering of the VAR.

In Figure 2 we show Spillover Plots produced using a shorter 75-week rolling window width, and two variance decomposition forecast horizons. (We use the original 10-week forecast horizon in panel 2a and a shorter 2-week horizon in panel 2b.) Our earlier results appear largely robust to all variations. The reduced smoothing due to the shorter window width, moreover, lets us track movements in volatility spillovers with greater resolution.

In Figure 3 we show Spillover Plots produced using a still-shorter 75-week rolling window width, and very short 10-day and 2-day variance decomposition forecast horizons. Our results again appear robust to window width and forecast horizon. Indeed they are also robust to choice of volatility estimator: We conduct the analyses underlying Figure 3 using daily, as opposed to weekly, range-based volatilities.<sup>3</sup>

In Figure 4 we explore robustness to VAR ordering, plotting maximum and minimum volatility spillovers across a variety of alternative VAR orderings, estimated using 200-week rolling windows. Computational considerations generally prohibit exploration of robustness of volatility Spillover Plots to all  $N!$  possible variable orderings of an  $N$ -variable VAR. (In our case, for example,  $N=19$ , resulting in roughly  $10^{17}$  possible orderings.) Hence in panel 4a we present results for eighteen “rotated” orderings corresponding to moving the U.S. to last, and then

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<sup>2</sup> We provide weekly updated spillover plots, for both returns and volatilities, at <http://data.economicresearchforum.org/erf/SpillOverIndex.aspx?lang=en>

<sup>3</sup> Because of different holidays, one or more markets may be closed on any day. To circumvent this problem, we set missing days’ volatilities equal to previous-day observations. We also assume that all stock markets are closed on Christmas day, New Year’s Eve, and Easter, because an overwhelming majority of markets are closed then.

moving the U.K. to last, and so on, and in panel 4b we present results for fifty randomly-chosen orderings. Throughout, the spillover range is small, and the same patterns are clearly revealed.

## **7. Summary and Concluding Remarks**

We have proposed a simple framework for measuring linkages in asset returns and return volatilities. In particular, we have formulated and examined precise measures of *return spillovers* and *volatility spillovers* based directly on the familiar notion of variance decompositions in vector autoregressions. Our spillover measures have the appealing virtue of conveying important and useful information while nevertheless sidestepping the contentious issue of definition and existence of episodes of “contagion” so vigorously debated in recent literature such as Forbes and Rigobon (2002).

Our framework facilitates study of both crisis and non-crisis episodes, including trends as well as bursts in spillovers. In an analysis of nineteen global equity markets from the early 1990s to the present, we find striking evidence of divergent behavior in the dynamics of return spillovers vs. volatility spillovers. To a good approximation, return spillovers display no bursts but a gently increasing trend, presumably associated with the gradually increasing financial market integration of the last fifteen years. Volatility spillovers, in contrast, display no trend but clear bursts associated with readily-identified “crisis” events. Why this should be so is a tremendously interesting question, albeit one about which existing theory evidently has little to say. We hope that our measurement will stimulate new theory that speaks to the distinction between return and volatility spillovers.

As for future work, there are several interesting directions for extension. On the theoretical side, it would be interesting to attempt to bound the range of spillovers corresponding to all  $N!$  variance decompositions associated with the set of all possible VAR orderings (e.g., building on Faust, 1998), or to produce spillover plots based on variance decompositions invariant to ordering (e.g., building on Pesaran and Shin, 1998). On the substantive empirical side, it will be interesting to analyze volatility spillovers not only in stock markets, but also within and across other financial markets, as well as in cross-country real activity and inflation.

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**Table 1**  
**Descriptive Statistics, Global Stock Market RETURNS, 1/10/1992 – 11/23/2007**

	<b>United States</b> <b>US</b>	<b>United Kingdom</b> <b>UK</b>	<b>France</b> <b>FRA</b>	<b>Germany</b> <b>GER</b>	<b>Hong Kong</b> <b>HKG</b>	<b>Japan</b> <b>JPN</b>	<b>Australia</b> <b>AUS</b>
<b>Mean</b>	0.00108	0.00038	0.00096	0.00148	0.00144	-0.00048	0.00100
<b>Median</b>	0.00249	0.00134	0.00116	0.00375	0.00266	0.00080	0.00212
<b>Maximum</b>	0.08015	0.09915	0.10981	0.12942	0.13616	0.11076	0.07044
<b>Minimum</b>	-0.15445	-0.08823	-0.12169	-0.14036	-0.20150	-0.11425	-0.05281
<b>Std. Dev.</b>	0.02086	0.02071	0.02709	0.02950	0.03479	0.02878	0.01610
<b>Skewness</b>	-0.72791	-0.10964	-0.13368	-0.27980	-0.44671	-0.02000	-0.19040
<b>Kurtosis</b>	7.606	4.780	4.143	5.182	5.912	3.968	3.875
	<b>Indonesia</b> <b>IDN</b>	<b>S. Korea</b> <b>KOR</b>	<b>Malaysia</b> <b>MYS</b>	<b>Philippines</b> <b>PHL</b>	<b>Singapore</b> <b>SGP</b>	<b>Taiwan</b> <b>TAI</b>	<b>Thailand</b> <b>THA</b>
<b>Mean</b>	0.00057	0.00048	0.00052	0.00001	0.00090	0.00032	-0.00055
<b>Median</b>	0.00163	0.00163	0.00084	0.00036	0.00147	0.00236	0.00080
<b>Maximum</b>	0.18192	0.17486	0.24264	0.15988	0.18363	0.18671	0.21783
<b>Minimum</b>	-0.20091	-0.21828	-0.19102	-0.22084	-0.24265	-0.14154	-0.17293
<b>Std. Dev.</b>	0.03827	0.04210	0.03220	0.03536	0.03069	0.03566	0.03905
<b>Skewness</b>	-0.29091	-0.33285	0.13408	-0.31194	-0.61057	0.01157	0.14976
<b>Kurtosis</b>	7.594	6.209	11.137	7.128	12.996	5.211	5.429
	<b>Argentina</b> <b>ARG</b>	<b>Brazil</b> <b>BRA</b>	<b>Chile</b> <b>CHL</b>	<b>Mexico</b> <b>MEX</b>	<b>Turkey</b> <b>TUR</b>		
<b>Mean</b>	-0.00002	0.00225	0.00112	0.00134	-0.00183		
<b>Median</b>	0.00338	0.00448	0.00102	0.00365	-0.00035		
<b>Maximum</b>	0.24283	0.21935	0.09088	0.17031	0.31552		
<b>Minimum</b>	-0.20193	-0.25158	-0.07129	-0.17829	-0.38140		
<b>Std. Dev.</b>	0.05120	0.05548	0.02093	0.03599	0.06477		
<b>Skewness</b>	0.02265	-0.29569	0.07717	-0.30595	-0.27740		
<b>Kurtosis</b>	5.467	5.077	4.507	5.352	7.147		

**Table 2**  
**Descriptive Statistics, Global Stock Market VOLATILITY, 1/10/1992 – 11/23/2007**

	<b>US</b>	<b>UK</b>	<b>FRA</b>	<b>GER</b>	<b>HKG</b>	<b>JPN</b>	<b>AUS</b>
<b>Mean</b>	0.00042	0.00049	0.00075	0.00083	0.00099	0.00072	0.00023
<b>Median</b>	0.00025	0.00024	0.00043	0.00035	0.00050	0.00050	0.00015
<b>Maximum</b>	0.00595	0.00926	0.01013	0.01630	0.03794	0.00798	0.01045
<b>Minimum</b>	0.00002	0.00001	0.00003	0.00001	0.00002	0.00002	0.00001
<b>Std. Dev.</b>	0.00056	0.00079	0.00104	0.00148	0.00204	0.00079	0.00044
<b>Skewness</b>	4.4198	5.4561	4.2555	4.8072	10.2854	3.5656	16.3669
<b>Kurtosis</b>	30.742	44.801	27.337	34.111	156.420	22.417	361.967
	<b>IDN</b>	<b>KOR</b>	<b>MYS</b>	<b>PHL</b>	<b>SGP</b>	<b>TAI</b>	<b>THA</b>
<b>Mean</b>	0.00088	0.00128	0.00085	0.00065	0.00045	0.00079	0.00111
<b>Median</b>	0.00036	0.00064	0.00024	0.00033	0.00020	0.00049	0.00056
<b>Maximum</b>	0.02074	0.01869	0.04592	0.01798	0.01050	0.01376	0.02356
<b>Minimum</b>	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00003
<b>Std. Dev.</b>	0.00169	0.00192	0.00287	0.00137	0.00081	0.00099	0.00179
<b>Skewness</b>	5.0567	3.8836	10.5119	8.3102	5.3390	4.7681	5.7314
<b>Kurtosis</b>	39.067	23.236	137.335	92.211	45.602	45.597	52.310
	<b>ARG</b>	<b>BRA</b>	<b>CHL</b>	<b>MEX</b>	<b>TUR</b>		
<b>Mean</b>	0.00187	0.00210	0.00021	0.00102	0.00317		
<b>Median</b>	0.00085	0.00108	0.00010	0.00053	0.00152		
<b>Maximum</b>	0.03371	0.06133	0.00816	0.02871	0.07689		
<b>Minimum</b>	0.00001	0.00000	0.00000	0.00000	0.00000		
<b>Std. Dev.</b>	0.00327	0.00419	0.00048	0.00180	0.00539		
<b>Skewness</b>	4.9933	7.7243	8.8249	7.8728	6.7978		
<b>Kurtosis</b>	35.897	82.961	113.737	96.061	73.763		

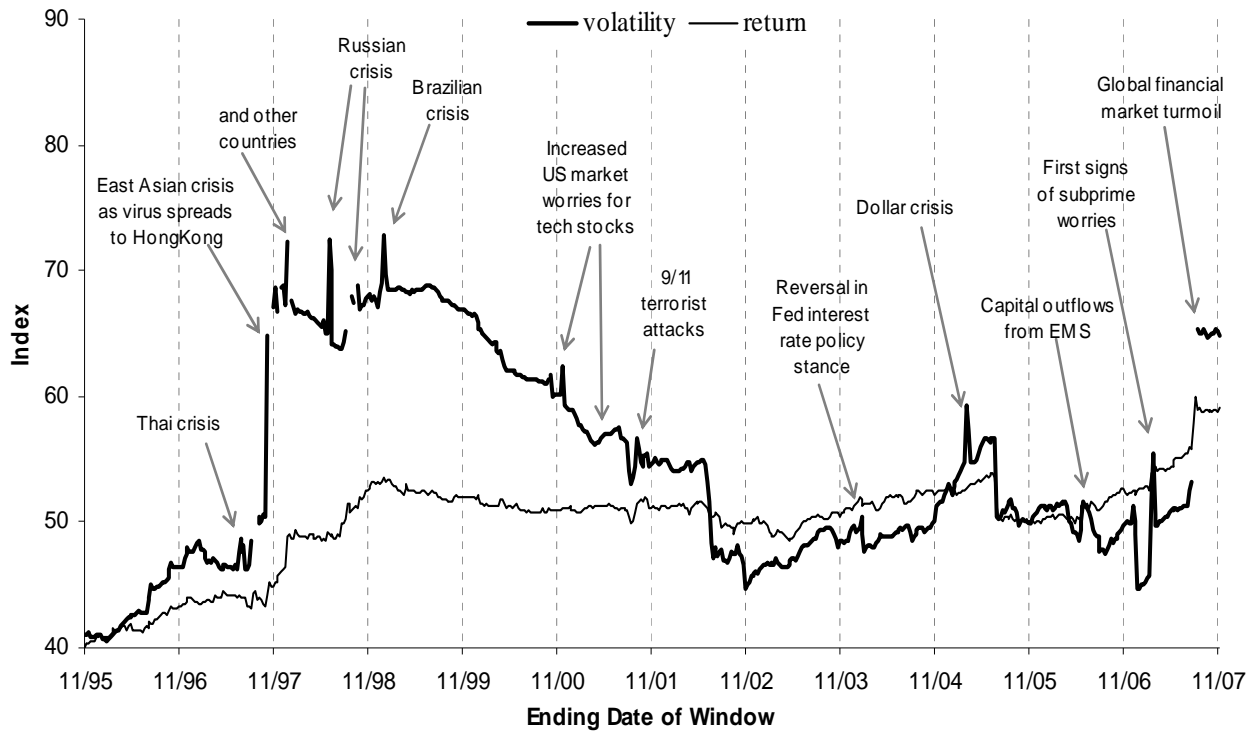
**Table 3 - Spillover Table, Global Stock Market RETURNS, 1/10/1992-11/23/2007**

		<b>F R O M</b>																			<b>Contribution From Others</b>	
		<b>US</b>	<b>UK</b>	<b>FRA</b>	<b>DEU</b>	<b>HKG</b>	<b>JPN</b>	<b>AUS</b>	<b>IDN</b>	<b>KOR</b>	<b>MYS</b>	<b>PHL</b>	<b>SGP</b>	<b>TAI</b>	<b>THA</b>	<b>ARG</b>	<b>BRA</b>	<b>CHL</b>	<b>MEX</b>	<b>TUR</b>		
<b>T O</b>	<b>US</b>	93.6	1.6	1.5	0.0	0.3	0.2	0.1	0.1	0.2	0.3	0.2	0.2	0.3	0.2	0.1	0.1	0.0	0.5	0.3	<b>6</b>	
	<b>UK</b>	40.3	55.7	0.7	0.4	0.1	0.5	0.1	0.2	0.2	0.3	0.2	0.0	0.1	0.1	0.1	0.1	0.0	0.4	0.5	<b>44</b>	
	<b>FRA</b>	38.3	21.7	37.2	0.1	0.0	0.2	0.3	0.3	0.3	0.2	0.2	0.1	0.1	0.3	0.1	0.1	0.1	0.1	0.1	0.3	<b>63</b>
	<b>DEU</b>	40.8	15.9	13.0	27.6	0.1	0.1	0.3	0.4	0.6	0.1	0.3	0.3	0.0	0.2	0.0	0.1	0.0	0.1	0.1	<b>72</b>	
	<b>HKG</b>	15.3	8.7	1.7	1.4	69.9	0.3	0.0	0.1	0.0	0.3	0.1	0.0	0.2	0.9	0.3	0.0	0.1	0.3	0.4	<b>30</b>	
	<b>JPN</b>	12.1	3.1	1.8	0.9	2.3	77.7	0.2	0.3	0.3	0.1	0.2	0.3	0.3	0.1	0.1	0.0	0.0	0.1	0.1	<b>22</b>	
	<b>AUS</b>	23.2	6.0	1.3	0.2	6.4	2.3	56.8	0.1	0.4	0.2	0.2	0.2	0.4	0.5	0.1	0.3	0.1	0.6	0.7	<b>43</b>	
	<b>IDN</b>	6.0	1.6	1.2	0.7	6.4	1.6	0.4	77.0	0.7	0.4	0.1	0.9	0.2	1.0	0.7	0.1	0.3	0.1	0.4	<b>23</b>	
	<b>KOR</b>	8.3	2.6	1.3	0.7	5.6	3.7	1.0	1.2	72.8	0.0	0.0	0.1	0.1	1.3	0.2	0.2	0.1	0.1	0.7	<b>27</b>	
	<b>MYS</b>	4.1	2.2	0.6	1.3	10.5	1.5	0.4	6.6	0.5	69.2	0.1	0.1	0.2	1.1	0.1	0.6	0.4	0.2	0.3	<b>31</b>	
	<b>PHL</b>	11.1	1.6	0.3	0.2	8.1	0.4	0.9	7.2	0.1	2.9	62.9	0.3	0.4	1.5	1.6	0.1	0.0	0.1	0.2	<b>37</b>	
	<b>SGP</b>	16.8	4.8	0.6	0.9	18.5	1.3	0.4	3.2	1.6	3.6	1.7	43.1	0.3	1.1	0.8	0.5	0.1	0.3	0.4	<b>57</b>	
	<b>TAI</b>	6.4	1.3	1.2	1.8	5.3	2.8	0.4	0.4	2.0	1.0	1.0	0.9	73.6	0.4	0.8	0.3	0.1	0.3	0.0	<b>26</b>	
	<b>THA</b>	6.3	2.4	1.0	0.7	7.8	0.2	0.8	7.6	4.6	4.0	2.3	2.2	0.3	58.2	0.5	0.2	0.1	0.4	0.3	<b>42</b>	
	<b>ARG</b>	11.9	2.1	1.6	0.1	1.3	0.8	1.3	0.4	0.4	0.6	0.4	0.6	1.1	0.2	75.3	0.1	0.1	1.4	0.3	<b>25</b>	
	<b>BRA</b>	14.1	1.3	1.0	0.7	1.3	1.4	1.6	0.5	0.5	0.7	1.0	0.8	0.1	0.7	7.1	65.8	0.1	0.6	0.7	<b>34</b>	
	<b>CHL</b>	11.8	1.1	1.0	0.0	3.2	0.6	1.4	2.3	0.3	0.3	0.1	0.9	0.3	0.8	2.9	4.0	65.8	2.7	0.4	<b>34</b>	
	<b>MEX</b>	22.2	3.5	1.2	0.4	3.0	0.3	1.2	0.2	0.3	0.9	1.0	0.1	0.3	0.5	5.4	1.6	0.3	56.9	0.6	<b>43</b>	
	<b>TUR</b>	3.0	2.5	0.2	0.7	0.6	0.9	0.6	0.1	0.6	0.3	0.6	0.1	0.9	0.8	0.5	1.1	0.6	0.2	85.8	<b>14</b>	
	<b>Contribution To Others</b>	<b>292</b>	<b>84</b>	<b>31</b>	<b>11</b>	<b>81</b>	<b>19</b>	<b>11</b>	<b>31</b>	<b>14</b>	<b>16</b>	<b>10</b>	<b>8</b>	<b>6</b>	<b>12</b>	<b>21</b>	<b>9</b>	<b>3</b>	<b>8</b>	<b>7</b>	<b>675.0</b>	
<b>Contribution Including Own</b>	<b>386</b>	<b>140</b>	<b>68</b>	<b>39</b>	<b>151</b>	<b>97</b>	<b>68</b>	<b>108</b>	<b>86</b>	<b>85</b>	<b>73</b>	<b>51</b>	<b>79</b>	<b>70</b>	<b>97</b>	<b>75</b>	<b>68</b>	<b>65</b>	<b>92</b>	<b>Spillover index=35.5%</b>		

**Table 4 - Spillover Table, Global Stock Market VOLATILITY, 1/10/1992-11/23/2007**

		<b>FROM</b>																			
		<b>US</b>	<b>UK</b>	<b>FRA</b>	<b>DEU</b>	<b>HKG</b>	<b>JPN</b>	<b>AUS</b>	<b>IDN</b>	<b>KOR</b>	<b>MYS</b>	<b>PHL</b>	<b>SGP</b>	<b>TAI</b>	<b>THA</b>	<b>ARG</b>	<b>BRA</b>	<b>CHL</b>	<b>MEX</b>	<b>TUR</b>	<b>Contribution From Others</b>
<b>T O</b>	<b>US</b>	63.9	14.9	3.9	1.9	4.9	0.2	1.8	0.3	1.6	0.9	0.4	2.6	0.3	0.1	0.1	0.0	0.1	0.2	2.0	<b>36</b>
	<b>UK</b>	22.9	54.5	5.0	1.3	7.4	0.5	2.1	0.3	1.0	0.8	0.1	2.4	0.2	0.2	0.4	0.2	0.1	0.1	0.7	<b>46</b>
	<b>FRA</b>	24.0	32.8	27.3	0.2	5.4	0.2	2.8	0.4	0.3	1.2	0.4	2.4	0.2	0.3	0.6	0.3	0.1	0.1	0.9	<b>73</b>
	<b>DEU</b>	26.9	29.5	13.6	13.7	4.8	0.2	3.9	0.2	0.2	1.3	0.8	2.0	0.2	0.4	0.6	0.3	0.1	0.2	1.0	<b>86</b>
	<b>HKG</b>	2.0	0.5	0.7	0.0	87.7	0.1	0.1	0.4	1.4	0.5	1.5	3.4	0.6	0.4	0.0	0.1	0.0	0.1	0.3	<b>12</b>
	<b>JPN</b>	2.7	3.3	0.4	0.7	1.6	82.9	0.1	0.1	0.9	1.1	0.1	1.6	0.3	0.0	0.6	0.3	0.3	0.2	2.8	<b>17</b>
	<b>AUS</b>	8.9	2.2	0.3	0.6	43.9	0.2	34.7	1.2	1.7	1.3	0.1	2.8	0.1	1.0	0.1	0.2	0.2	0.3	0.1	<b>65</b>
	<b>IDN</b>	2.8	0.9	0.3	1.0	6.1	0.3	0.6	71.4	6.9	2.3	2.5	2.8	0.7	0.0	0.0	0.3	0.2	0.2	0.9	<b>29</b>
	<b>KOR</b>	2.5	0.6	0.4	0.4	9.1	1.0	1.0	10.3	67.5	1.3	0.9	2.5	0.8	0.2	0.1	0.1	0.2	0.3	0.8	<b>32</b>
	<b>MYS</b>	1.3	0.6	0.3	0.6	7.2	1.0	0.9	0.8	1.7	70.7	3.1	6.1	0.3	0.5	0.9	0.6	0.1	1.5	1.9	<b>29</b>
	<b>PHL</b>	2.1	0.3	0.3	0.4	8.9	0.3	0.4	8.8	3.0	6.1	66.7	1.5	0.2	0.2	0.2	0.2	0.1	0.2	0.3	<b>33</b>
	<b>SGP</b>	12.5	4.1	0.6	0.1	12.2	0.8	0.8	7.6	7.2	2.8	1.5	45.8	0.5	0.1	0.7	0.7	0.0	0.7	1.2	<b>54</b>
	<b>TAI</b>	8.5	0.4	0.4	0.2	2.8	0.7	1.3	0.5	9.5	0.7	1.7	0.6	69.0	0.2	0.4	0.8	0.2	0.7	1.3	<b>31</b>
	<b>THA</b>	0.5	0.7	0.4	0.3	9.0	0.2	0.3	3.6	2.9	0.4	0.8	5.3	0.2	73.9	0.1	0.5	0.1	0.7	0.2	<b>26</b>
	<b>ARG</b>	3.5	1.5	1.6	0.4	2.7	0.5	1.2	0.3	0.1	2.1	0.2	0.8	0.4	0.3	81.0	0.9	0.8	0.6	1.0	<b>19</b>
	<b>BRA</b>	4.5	2.3	1.4	0.3	12.6	0.4	3.3	1.0	0.3	10.0	0.7	3.4	0.5	0.3	11.7	45.2	0.3	0.9	0.8	<b>55</b>
	<b>CHL</b>	3.5	0.7	0.7	0.3	2.7	0.1	3.6	1.1	0.2	1.8	0.3	1.8	0.3	0.4	3.6	5.0	73.7	0.2	0.1	<b>26</b>
	<b>MEX</b>	6.5	1.3	0.7	0.3	25.0	0.2	4.8	0.3	0.5	2.4	0.3	2.1	0.2	0.5	6.3	3.0	0.3	44.1	1.1	<b>56</b>
	<b>TUR</b>	2.8	1.7	0.8	0.7	3.9	0.3	1.2	0.3	1.1	2.7	0.5	0.9	4.0	0.1	0.7	0.3	0.2	1.1	76.8	<b>23</b>
	<b>Contribution To Others</b>		<b>138</b>	<b>98</b>	<b>32</b>	<b>10</b>	<b>170</b>	<b>7</b>	<b>30</b>	<b>38</b>	<b>41</b>	<b>40</b>	<b>16</b>	<b>45</b>	<b>10</b>	<b>5</b>	<b>27</b>	<b>14</b>	<b>3</b>	<b>8</b>	<b>17</b>
<b>Contribution Including Own</b>		<b>202</b>	<b>153</b>	<b>59</b>	<b>23</b>	<b>258</b>	<b>90</b>	<b>65</b>	<b>109</b>	<b>108</b>	<b>111</b>	<b>83</b>	<b>91</b>	<b>79</b>	<b>79</b>	<b>108</b>	<b>59</b>	<b>77</b>	<b>52</b>	<b>94</b>	<b>Spillover Index = 39.5%</b>

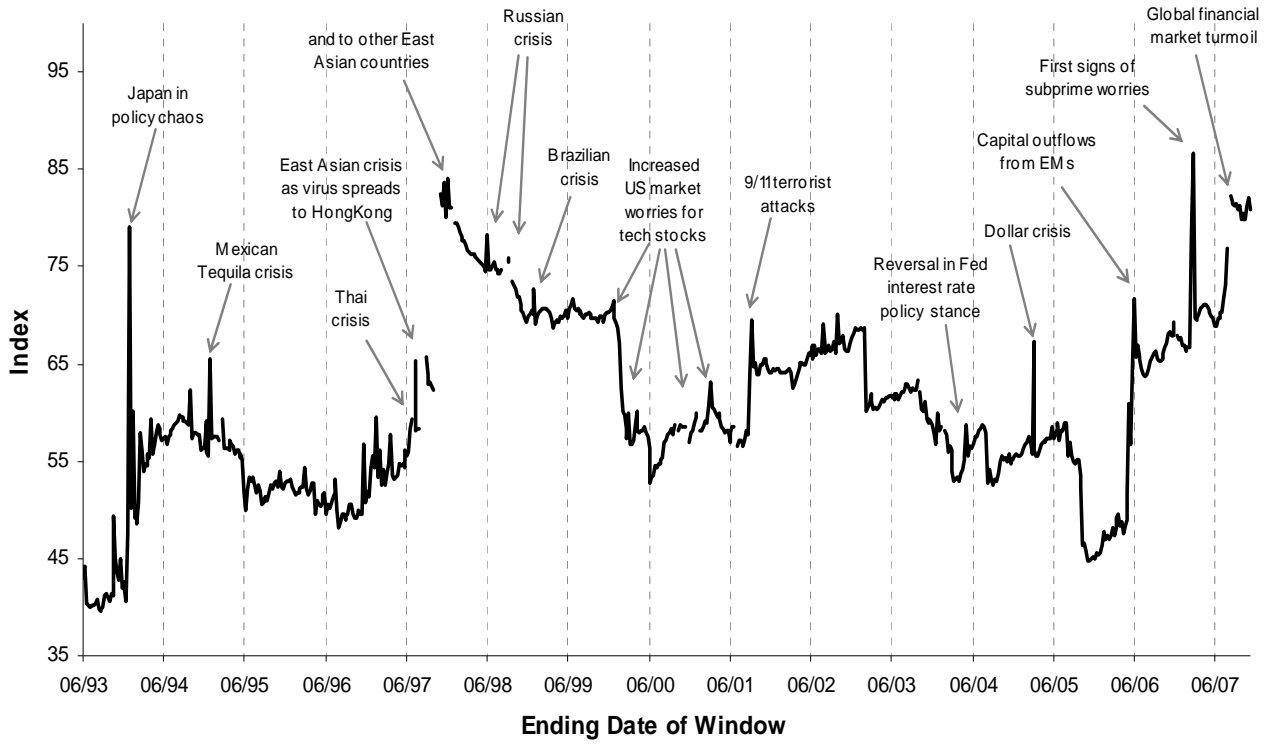
**Figure 1**  
**Spillover Plot, Global Stock Market RETURNS and VOLATILITY, 11/1995-11/2007**



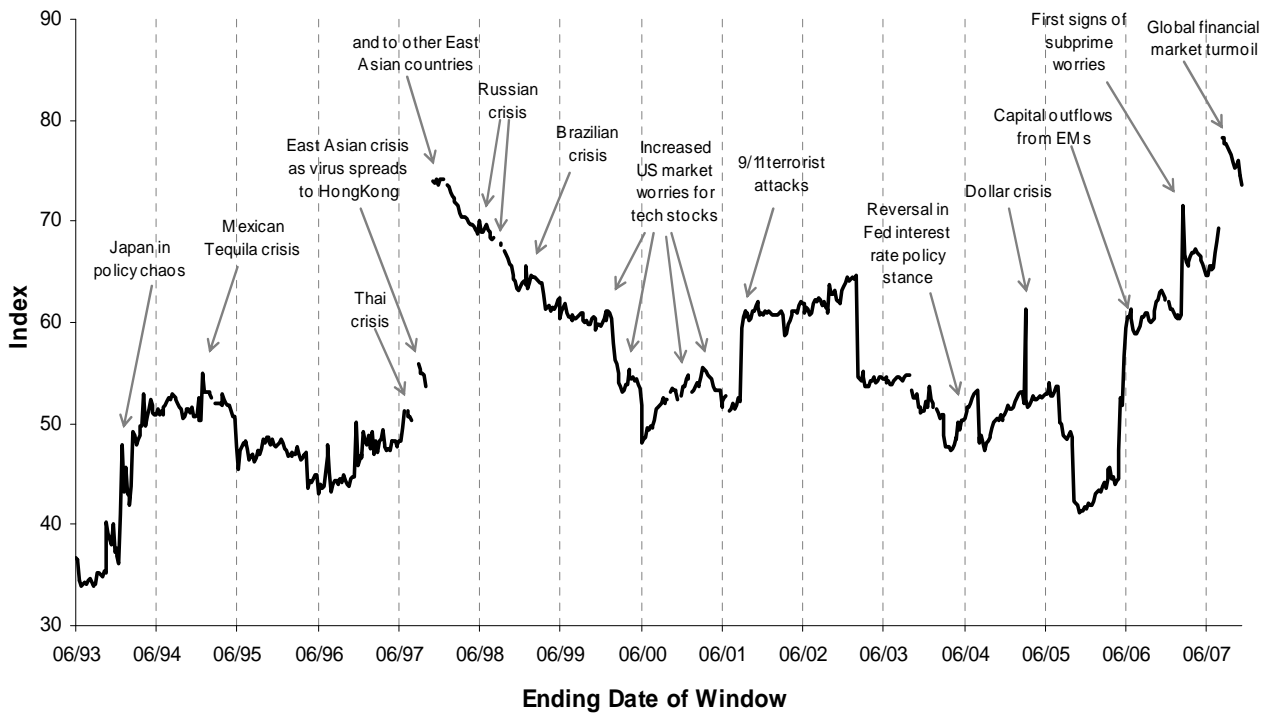


**Figure 2**  
**Spillover Plot, Global Stock Market Volatility, 6/1993-11/2007**

**a. 10-Week Forecast Horizon**

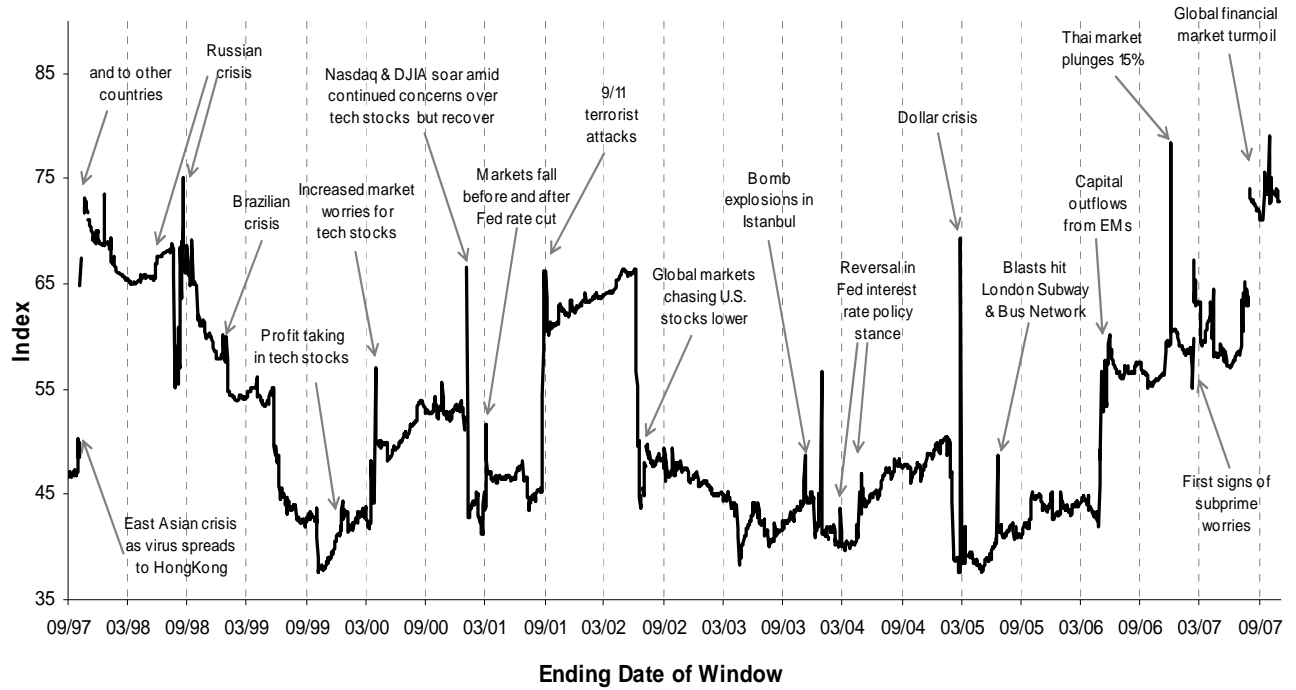


**b. 2-Week Forecast Horizon**

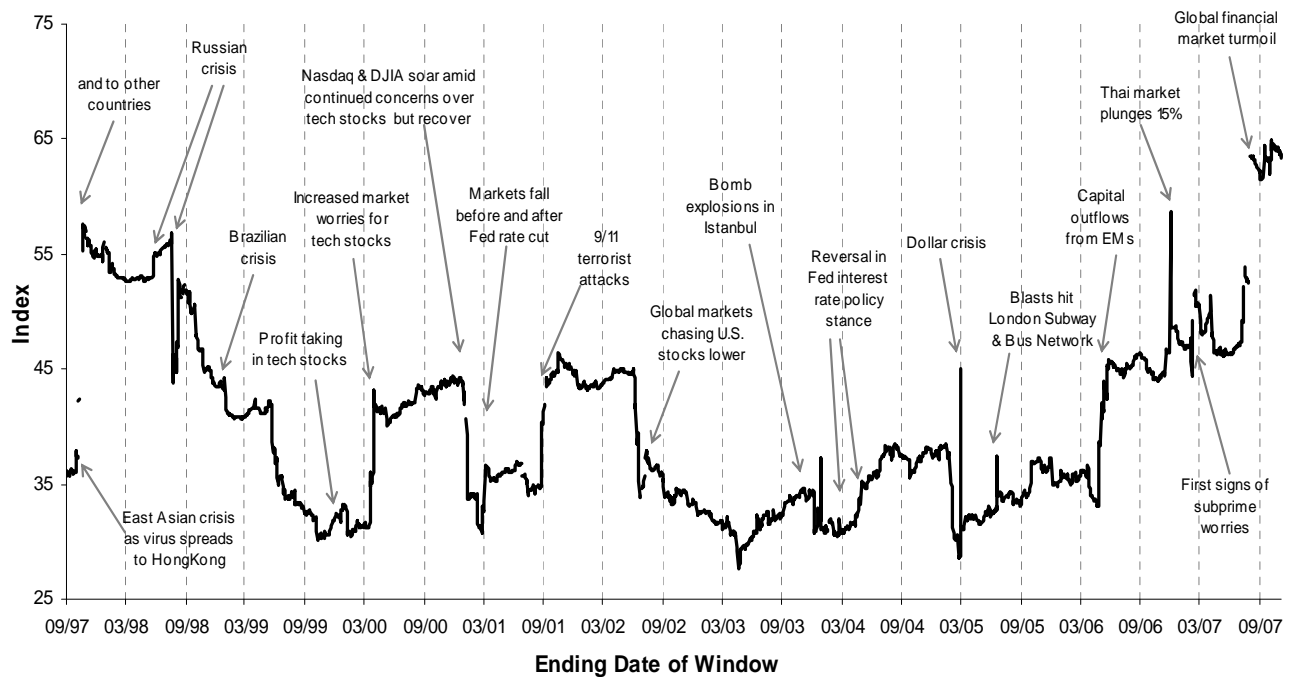


**Figure 3**  
**Spillover Plots, Global Stock Market Volatility, 12/1996-11/2007**

**a. 10-Day Forecast Horizon**

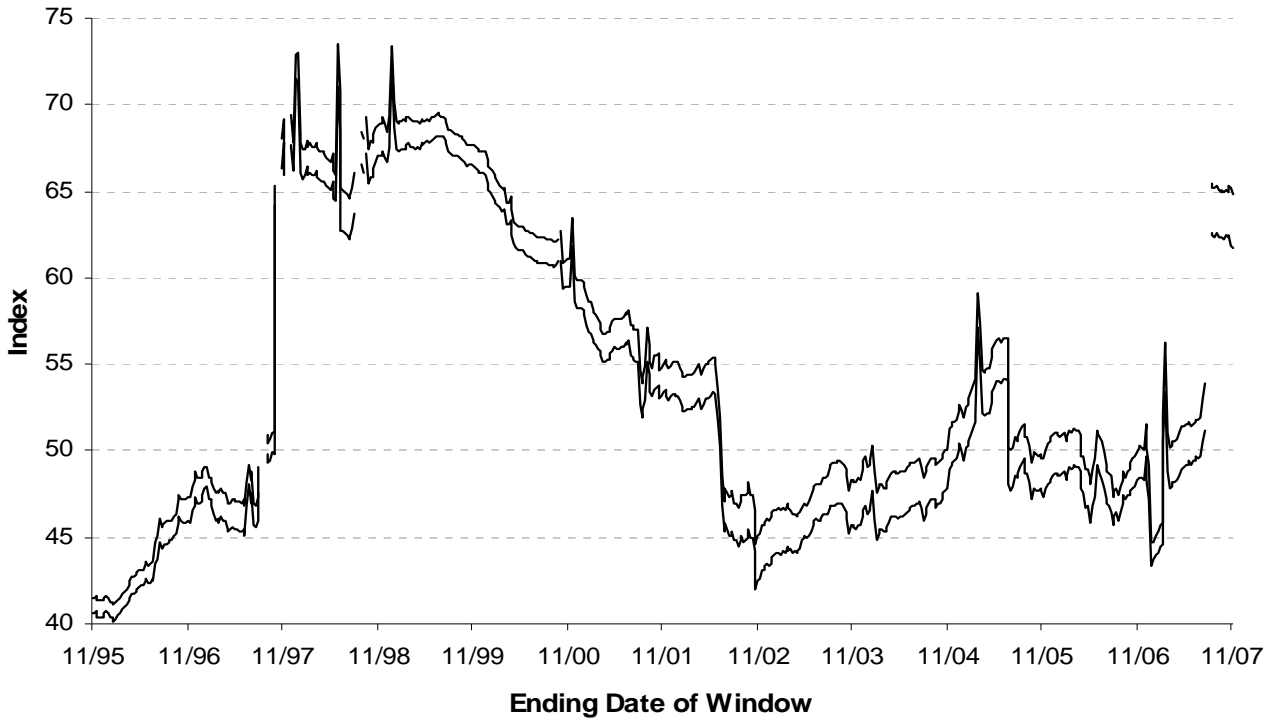


**b. 2-Day Forecast Horizon**

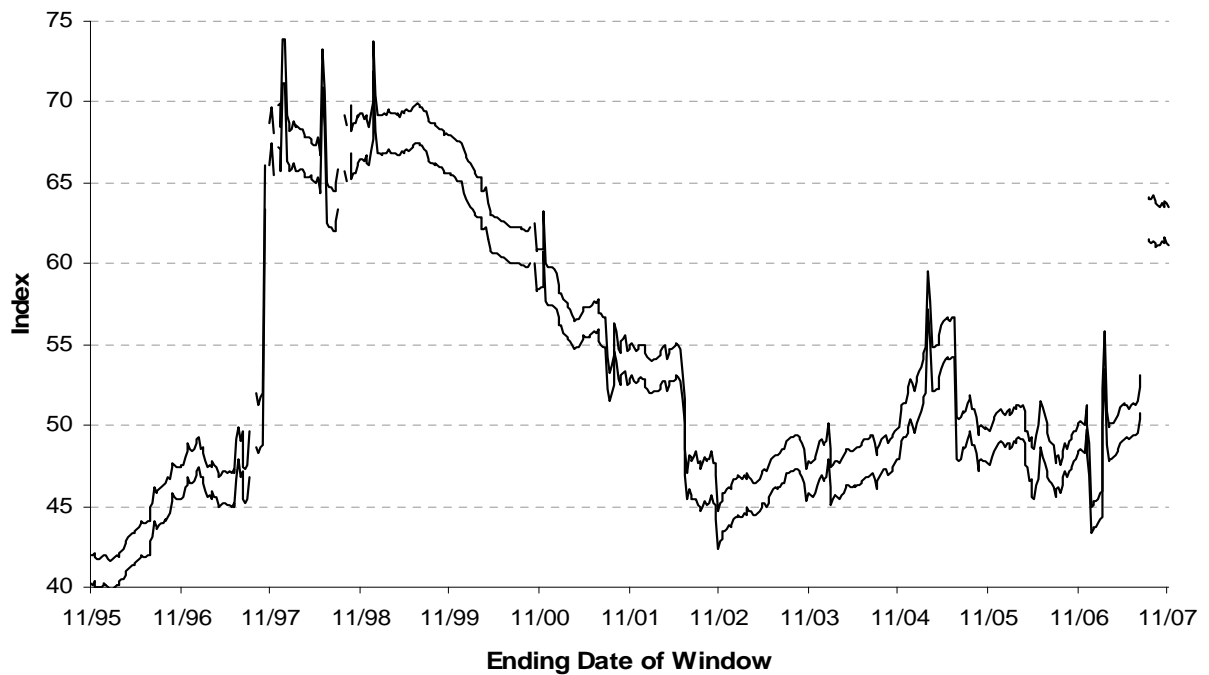


**Figure 4**  
**Maximum and Minimum Spillovers, Global Stock Market Volatility, 11/1995-11/2007**

**a. Based on 18 Rotated Orderings**



**b. Based on 50 Random Orderings**



### **Notes to Tables**

**Table 1:** Returns are in real terms and measured weekly, Friday-to-Friday. The sample size is 829. See text for details.

**Table 2:** Volatilities are for Monday-to-Friday returns. The mnemonics are as in Table 1. We calculate Chile's volatility using the Santiago Stock Exchange IGPA Index for 1/1992 – 5/2004 and the Santiago Stock Exchange IPSA index for June 2004 onward. The sample size is 829. See text for details.

**Table 3:** The underlying variance decomposition is based upon a weekly VAR of order 2, identified using a Cholesky factorization with the ordering as shown in the column heading. The (i, j)-th value is the estimated contribution TO the variance of the 10-week-ahead real stock return forecast error of country i coming FROM innovations to real stock returns of country j. The mnemonics are defined as in Table 1.

**Table 4:** The underlying variance decomposition is based upon a weekly VAR of order 2, identified using a Cholesky factorization with the ordering as shown in the column heading. The (i, j)-th value is the estimated contribution TO the variance of the 10-week-ahead stock return volatility forecast error of country i coming FROM innovations to the stock return volatility of country j. We calculate Chile's volatility using the Santiago Stock Exchange IGPA Index for January 1992-May 2004, and using the Santiago Stock Exchange IPSA index for June 2004 onward. The mnemonics are defined as in Table 1.

### **Notes to Figures**

**Figure 1:** We plot moving return and volatility Spillover Indexes, defined as the sum of all variance decomposition “contributions to others” from Tables 3 and 4, respectively, estimated using 200-week rolling windows. See text for details.

**Figure 2:** We plot a moving volatility Spillover Index, defined as the sum of all variance decomposition “contributions to others” from Table 4, estimated using 75-week rolling windows. See text for details.

**Figure 3:** We plot a moving volatility Spillover Index, defined as the sum of all variance decomposition “contributions to others” from Table 4, estimated using 200-day rolling windows. See text for details.

**Figure 4:** We plot maximum and minimum volatility spillovers across a variety of alternative VAR orderings, estimated using 200-week rolling windows. In panel 4a we present results for eighteen “rotated” orderings corresponding to moving US to last, and then moving UK to last, and so on. In panel 4b we present results for fifty randomly-chosen orderings. See text for details.