

1. Additional details for the experimental setup

The test functions of the benchmark are described in Table 1. Table 2 reports the the source of the implementations of the algorithms.

| Problem | Objective function | Domain | Local max. |
|---------------|--|--------------------------|------------|
| Auto MPG | $-\frac{1}{10} \sum_{k=1}^{10} \sum_{i \in D_k} (\hat{f}_k(X_i) - Y_i)^2$ | $[-2, 4] \times [-5, 5]$ | – |
| Breast Cancer | where: – $\hat{f}_k \in \underset{f \in \mathcal{H}_\sigma}{\operatorname{argmin}} \frac{1}{n- D_k } \sum_{i \notin D_k} (f(X_i) - Y_i)^2 + \lambda \ f\ _{\mathcal{H}_\sigma}$ | $[-2, 4] \times [-5, 5]$ | – |
| Concrete | – the data set $\{(X_i, Y_i)\}_{i=1}^n$ is split into 10 folds $D_1 \dots D_{10}$ – \mathcal{H}_σ denotes the gaussian RKHS of bandwidth σ | $[-2, 4] \times [-5, 5]$ | – |
| Yacht | – $\ f\ _{\mathcal{H}_\sigma}$ is the corresponding norm | $[-2, 4] \times [-5, 5]$ | – |
| Housing | – $\sigma = 10^{x_1}$ – $\lambda = 10^{x_2}$ | $[-2, 4] \times [-5, 5]$ | – |
| Holder Table | $ \sin(x_1) \times \cos(x_2) \times \exp(1 - (x_1^2 + x_2^2)^{1/2}/\pi)$ | $[-10, 10]^2$ | 36 |
| Rosenbrock | $-\sum_{i=1}^2 [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$ | $[-2.048, 2.048]^3$ | – |
| Sphere | $-(\sum_{i=1}^4 (x_i - \pi/16)^2)^{1/2}$ | $[0, 1]^4$ | 1 |
| Linear Slope | $\sum_{i=1}^4 10^{(i-1)/4} (x_i - 5)$ | $[-5, 5]^4$ | 1 |
| Deb N.1 | $\frac{1}{5} \sum_{i=1}^5 \sin^6(5\pi x_i)$ | $[-5, 5]^5$ | 36 |

Table 1. Description of the test functions of the benchmark. Dash symbols are used when a value could not be calculated.

| Library | Algorithms |
|--|-------------------|
| The CMA 1.1.06 package (Hansen, 2011) | CMA-ES |
| NLOpt Library (Johnson, 2014) | CRS, DIRECT, MLSL |
| BayesOpt Library (Martinez-Cantin, 2014) | BayesOpt |

Table 2. Source of the implementations of the algorithms used for comparison.

References

- Hansen, Nikolaus. The cma evolution strategy: A tutorial. Retrieved May 15, 2016, from <http://www.lri.fr/hansen/cmaesintro.html>, 2011.
- Johnson, Steven G. The NLOpt nonlinear-optimization package. Retrieved May 15, 2016, from <http://ab-initio.mit.edu/nlopt>, 2014.
- Martinez-Cantin, Ruben. Bayesopt: A bayesian optimization library for nonlinear optimization, experimental design and bandits. *The Journal of Machine Learning Research*, 15(1):3735–3739, 2014.