

# Two Attacks on the Wu-Hsu User Identification Scheme

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## Abstract

In 2000, Lee and Chang proposed a user identification scheme with key distribution preserving anonymity for distributed computer networks. Recently, Wu and Hsu pointed out that there are two weaknesses in the Lee-Chang scheme. They further not only proposed a new scheme to remedy the security leaks of the Lee-Chang scheme, but also reduced computation complexities and communication cost as compared with the Lee-Chang scheme. However, in this article we show that there are two attacks in their scheme.

*Keywords:* Anonymity, distributed computer networks, key distribution, user identification

## 1 Introduction

In 2000 [3], Lee and Chang proposed a user identification scheme based on the security of the factoring problem and the one-way hash function [1, 2]. Their scheme can let the service provider identify the legal user and, in the meanwhile, agree on session key with the user for distributed computer networks.

There are four advantages in the Lee-Chang scheme. The first is that users can request services without revealing their identities to public. The second is that each user needs to maintain only one secret. The third is that it is not required for service providers to record the password files for the users. The fourth is that no master key updating is needed if a new service provider is added into the system.

However, in 2004 [4], Wu and Hsu showed that there are two weaknesses in the Lee-Chang scheme. To remedy these two weaknesses, they further proposed an efficient scheme. Their scheme can reduce the computation complexities and communication cost as compared with the Lee-Chang scheme. However, in this article, we show that the Wu-Hsu scheme can not resist two attacks.

## 2 The Review of the Wu-Hsu User Identification Scheme

In Wu-Hsu scheme [4], it consists of two phases: key generation and anonymous user identification. In key generation phase, there is a Smart Card Producing Center, denoted as SCPC, whose initializes the system parameters, maintains public information, and assigns a secret token to each system member. In anonymous user identification phase, the service provider can identify a legal user and agree on a session key with the user. The details of these two phases are described in the following:

### Key Generation

First, SCPC selects two large primes  $p$  and  $q$ , computes  $N = pq$ , and picks an element  $g \in Z_N^*$  and a hash function  $f$ . After, SCPC selects a secret key  $d$  and then computes a public key  $e$  such that  $ed = 1 \pmod{(p-1)(q-1)}$ . Finally, some parameters  $N, e, g$ , and  $f$  are public. And  $d, p$ , and  $q$  are kept secret by SCPC. Each user can be assigned a secret token  $S_i$  by SCPC. SCPC computes

$$S_i = ID_i^d \pmod N,$$

where  $ID_i$  is the identity of user  $U_i$  or service provider  $P_i$ . Then SCPC sends  $S_i$  to each user  $U_i$  (or  $P_i$ ) through a secure channel.

### Anonymous User Identification

If  $U_i$  wants to request services from a service provider  $P_j$ , he/she submits a service request to  $P_j$ . Upon receiving the request,  $P_j$  chooses a random number  $k$  and computes  $z = g^k S_j \pmod N$  which is then sent to  $U_i$ . After receiving the  $z$ ,  $U_i$  chooses a random number  $t$  and computes  $a = z^e / ID_j \pmod N$ ,  $x = S_i f(a^t || T) \pmod N$ , and  $y = g^{et} \pmod N$ , where  $T$  is the timestamp. After that,  $U_i$  sends  $(x, y, T)$  to  $P_j$ . Finally,  $P_j$  checks  $T$  and verifies the following equation:

$$ID_i = (x/f(y^k || T))^e \pmod N.$$

If it holds for some  $ID_i$  existing in the identity list,  $U_i$  is accepted as an authorized user and the service request will be granted. After the user identification, the user and the service provider can agree on a common session key as

$$K_{ij} = a^{tx} = y^{kx} = g^{ektx} \bmod N.$$

### 3 Two Attacks on the Wu-Hsu User Identification Scheme

In this section, we propose two attacks on the Wu-Hsu user identification scheme. The details of the two attacks are described in the following:

#### [Attack 1]

A legal user  $U_i$  can create a valid pair of  $(ID_f, S_f)$  without knowing the secure key  $d$  of the SCPC. If the created  $ID_f$  exists in the identity list of the service provider,  $U_i$  can forge  $U_f$  to login the service provider and request service from the service provider. Now,  $U_i$  has a valid pair of  $(ID_i, S_i)$ , and he/she wants to create a valid pair of  $(ID_f, S_f)$  such that satisfies  $S_f = ID_f^d \bmod N$ . First,  $U_i$  can compute  $ID_f$  as follows:

$$ID_f = ID_i^n \bmod N,$$

where  $n \geq 2$ . After that, he/she can derive  $S_f = ID_f^d \bmod N$ . Although he/she does not know the secure key of the SCPC, he/she can easily create a valid pair of  $(ID_f, S_f)$ . He/she computes  $S_f$  as follows:

$$\begin{aligned} S_f &= ID_f^d \bmod N \\ &= (ID_i^n \bmod N)^d \bmod N \\ &= (ID_i^n)^d \bmod N \\ &= (ID_i^d)^n \bmod N \\ &= (S_i)^n \bmod N. \end{aligned}$$

After that,  $U_i$  can use the self-constructed pair of  $(ID_f, S_f)$  to login the service provider.

#### [Attack 2]

An attacker  $U_f$  can forge a legal user  $U_i$  to login a service provider. He/She can derive the  $S_i = ID_i^d \bmod N$  without knowing the secret key  $d$  of the SCPC. First, the attacker can choose a random number  $r$  such that  $\gcd(r, N) = 1$ . Then, he/she computes  $ID_f$  as follows:

$$ID_f = ID_i^r \bmod N.$$

After that, the attacker submits the  $ID_f$  to the SCPC. The SCPC will assign a secret token  $S_f = ID_f^d \bmod N$  to the  $U_f$ . Now, the attacker can derive  $S_i$  as follows:

$$\begin{aligned} S_f^{-r} \bmod N &= (ID_f^d)^{-r} \bmod N \\ &= ((ID_i^r)^d)^{-r} \bmod N \\ &= ID_i^d \bmod N \\ &= S_i \bmod N. \end{aligned}$$

After that,  $U_f$  can forge the legal user  $U_i$  to login the service provider.

## 4 Conclusion

In this article, we have shown that the Wu-Hsu user identification scheme is vulnerable to two attacks as shown in Section 3. An attacker can forge another legal user to login the service provider.

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