

1 First we would like to thank all the reviewers for their feedback. We address the reviewers' questions below.

2 **Reviewer 1:** "In the related work you mention a lower bound of $(1/\epsilon)^{O(d)}$ for *any* estimator – I didn't quite
3 understand the exact difference from your formulation that allows a poly time upper bound."

4 The $(1/\epsilon)^{O(d)}$ is a bound on the number of independent samples, n , required to learn a d -dimensional logconcave
5 distribution within error ϵ in squared Hellinger distance, and this bound is tight in the worst-case. Our algorithm runs
6 in time polynomial in d , n , and $1/\text{error}$, and computes the logconcave MLE of *any* set of n points in \mathbf{R}^d . The best
7 previous algorithms had runtime polynomial in $n^{\Omega(d)}$.

8
9 "I understand that there is much prior work on this problem and the result seems interesting and significant – but it
10 would be nice to point out any specific applications or directions that could potentially be enabled by this finding."

11 Any application where one might be tempted to model the distribution as a multivariate Gaussian, may also be suitable
12 for the log-concave MLE. Provided sufficient data, the log-concave MLE would capture properties such as asymmetry
13 and skewness in the distribution. For example, this has been used to better predict breast cancer malignancies [1].

14 **Reviewer 3:** "The paper is theoretically interesting and provides a polynomial time algorithm, however, the degree of
15 the polynomial is quite high. For example, step 1 of the Algorithm 2 takes time $O(d^5)$ for d dimensional data. Further,
16 given the sample complexity of the algorithm itself is exponential in d , the advantage of the polynomial time algorithm
17 is not clear."

18 An interesting direction of future work is reducing the d -dependence. The main bottleneck of the current algorithm is the
19 volume computation (step 1 of Algorithm 2). Recent developments in RHMC based methods for volume computation
20 have resulted in much faster algorithms for computing volumes of polytopes [2]. However, the aforementioned
21 algorithms require a different oracle model and do not apply directly in our setting. That said, we are optimistic that
22 similar ideas might apply, and could plausibly lead to a much more efficient implementation of our algorithm.

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24
25 "In lemma 1, tent poles are defined as points X_i , but in line 184 it is defined as pairs (X_i, y_i) "

26 Thank you for pointing this out. It will be fixed in the next revision.

27
28
29 "Is the epsilon in the sample complexity discussion (lines 156 - 170) different than the epsilon in Definition 2? If so,
30 please clarify."

31 Appendix *E* shows that a small value of one implies a small value of the other. Thus, it suffices to think of them as
32 equivalent in the regime where the log-concave MLE has converged.

33 **Reviewer 5:**

34 "The authors could present some more exposition of the sampler."

35 We will add further exposition in the revised version of our paper.

36 References

37 [1] Madeleine Cule, Richard Samworth, and Michael Stewart. Maximum likelihood estimation of a multi-dimensional
38 log-concave density. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(5):545–607,
39 2010.

40 [2] Yin Tat Lee and Santosh S Vempala. Convergence rate of riemannian hamiltonian monte carlo and faster polytope
41 volume computation. In *Proceedings of the 50th Annual ACM SIGACT Symposium on Theory of Computing*, pages
42 1115–1121. ACM, 2018.