



Società Italiana di Fisica

106th online SIF Congress, 14-18 September 2020

Holography, Supergravity and Graphene

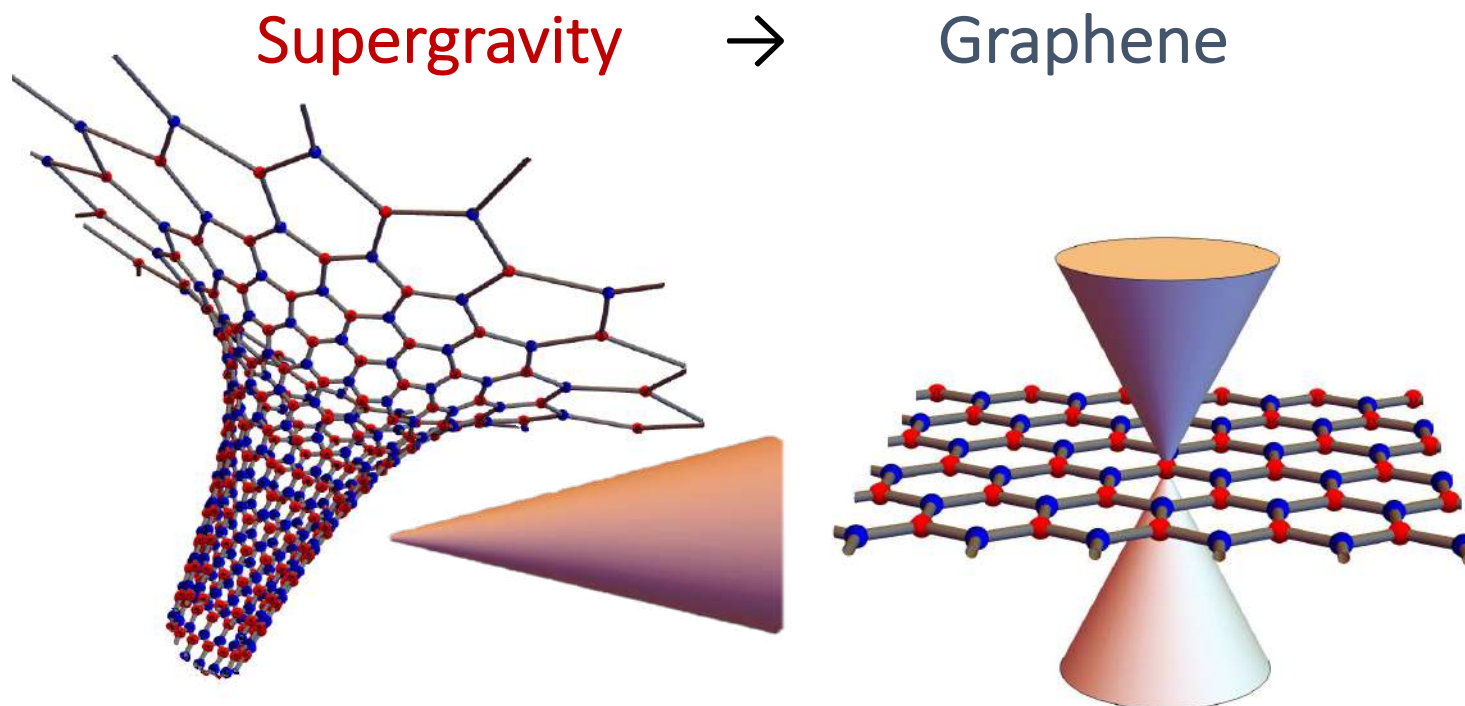
B. L. Cerchiai

(Centro Fermi Roma and Politecnico di Torino)

based on L. Andrianopoli, BLC, R. D'Auria, M. Trigiante, JHEP04(2018)007, arXiv:1801.08081;

L. Andrianopoli, BLC, R. D'Auria, A. Gallerati, R. Noris, M. Trigiante, J. Zanelli, JHEP01(2020)084, arXiv:1910.03508;

L. Andrianopoli, BLC, R. Matrecano, O. Mišković, R. Noris, R. Olea, L. Ravera, M. Trigiante, work in progress

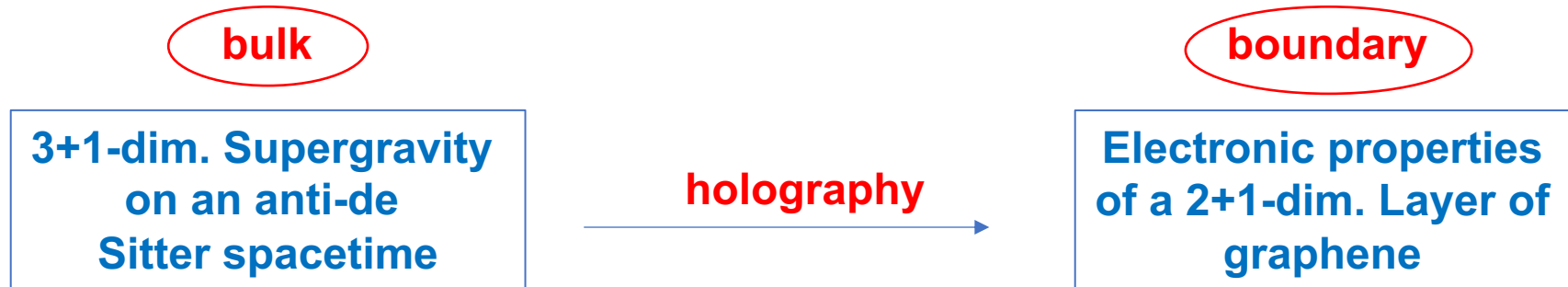


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Main idea

Objective: Application of the dualities of supergravity to the study of graphene-like 2D materials in condensed matter.

- The gauge/gravity correspondence relates a strongly coupled gauge theory to a weakly coupled classical gravity theory in one dimension higher.



- Top-down approach: Large amount of supersymmetry makes the model very predictive

Relation of the electronic properties of graphene to deformations of the lattice geometry

- Relevance of supersymmetry in low-energy physics

Interdisciplinary approach

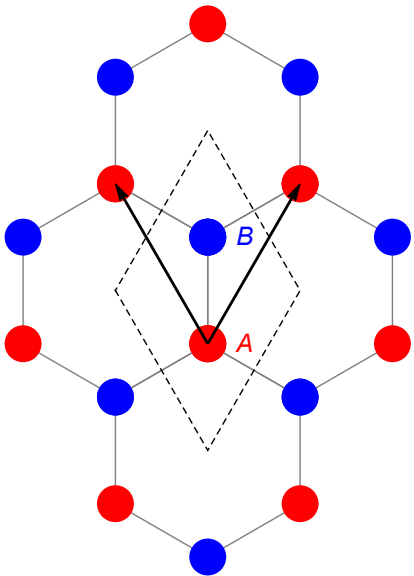
Graphene and the Dirac equation

The graphene honeycomb lattice

Graphene is a two-dimensional layer of carbon atoms (one single layer of graphite).

The carbon atoms in graphene form a **honeycomb lattice with a hexagonal structure**, due to the sp^2 orbital hybridization.

Bipartite lattice composed by two triangular sublattices (sites **A** and sites **B**).

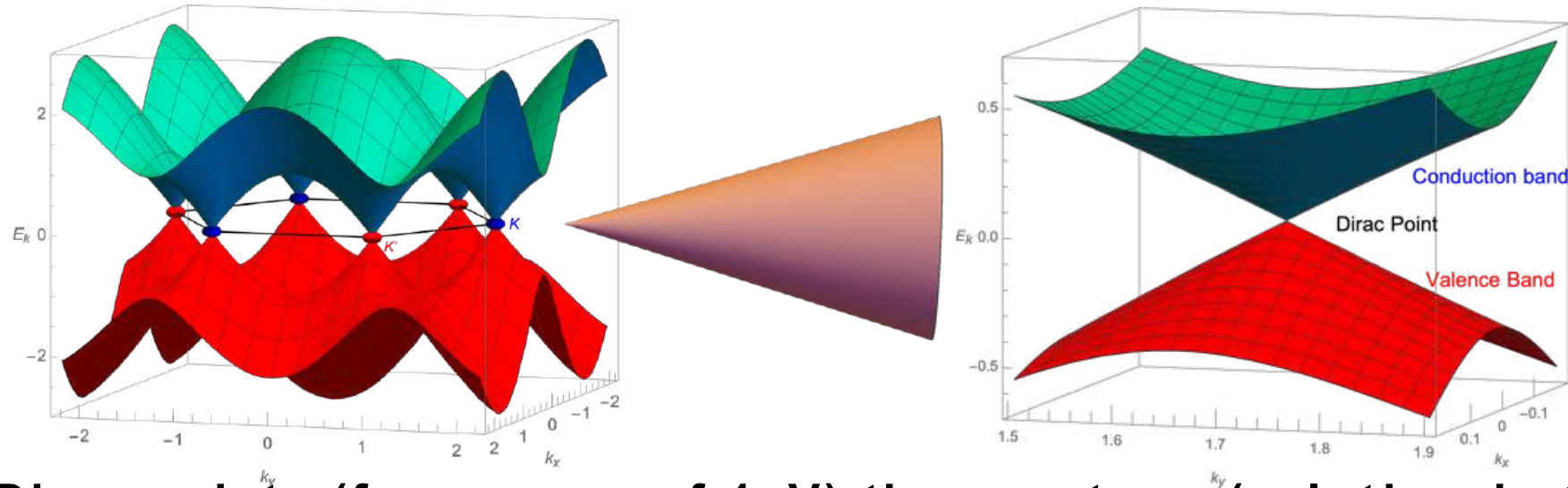


Belonging to site **A** or **B** defines an additional

spin-like quantum number: Pseudospin.

The graphene Dirac cone

The **Electron Band Structure** of graphene



At the Dirac points (for a range of 1eV) the spectrum (relation between the energy E_k and the momentum k) is **linear**:

Dirac cone: $E_k = \pm \hbar c |k|$

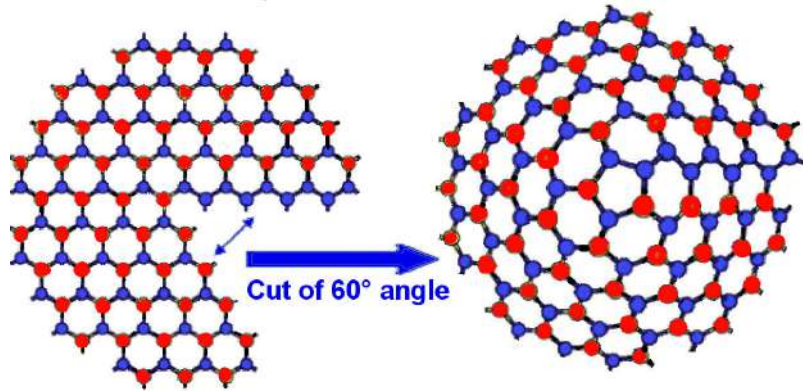
Electrons in graphene obey the same type of equations as

relativistic Dirac massless particles with

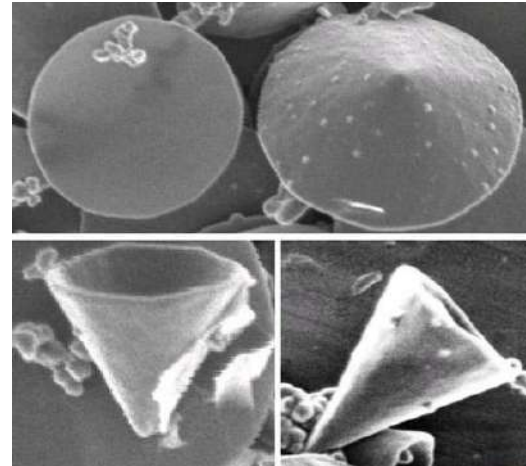
Light speed $c \rightarrow v_F = 10^6 \frac{m}{s} = \frac{c}{300}$ **Fermi velocity**

Analogue relativity in Condensed Matter: Geometry

Lattice disclination



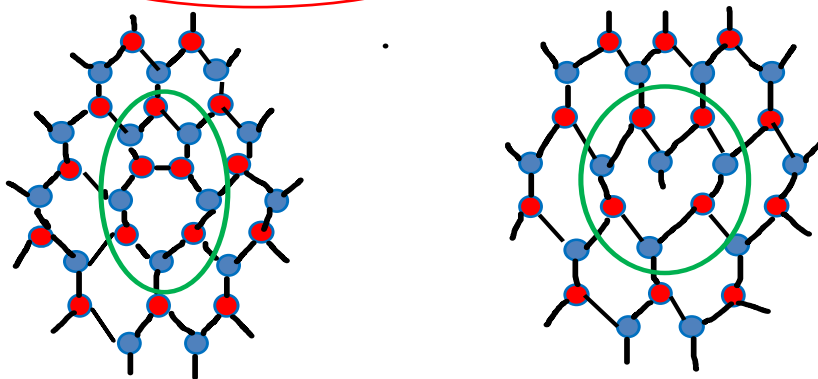
Space Curvature



Carbon nanocones

[Kenneth D. Knudsen,
https://en.wikipedia.org/wiki/Carbon_nanocone,
licensed under https://en.wikipedia.org/wiki/en:Creative_Commons]

Lattice dislocation



Space Torsion

Glide and shuffle dislocations in graphene, obtained from subsequent disclinations

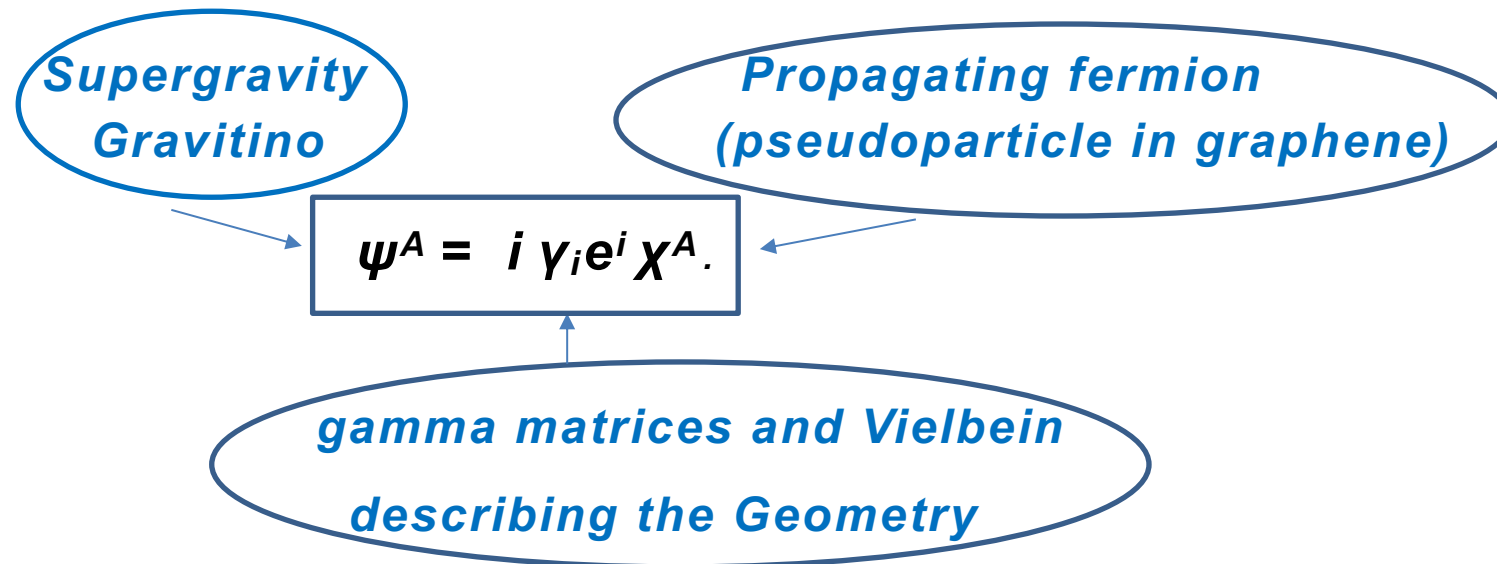
[see e.g. A. Carpio, L.L. Bonilla, F. de Juan, M.A.H. Vozmediano, *Dislocations in graphene*, New J. Phys. 10 (2008); T.L. Hughes, R.G. Leigh and O. Parrikar, *Torsional Anomalies, Hall Viscosity and Bulk-boundary Correspondence in Topological States*, Phys. Rev. D 88 (2013) 025040, arXiv:1211.6442]

Generalized AVZ Model for Graphene

[L. Andrianopoli, BLC, R. D'Auria, M. Trigiante, *Unconventional Supersymmetry at the boundary of AdS₄ Supergravity*, JHEP04(2018)007, arXiv:1801.08081;

L. Andrianopoli, B.L. Cerchiai, R. D'Auria, A. Gallerati, R. Noris, M. Trigiante, J. Zanelli, *N-Extended D=4 Supergravity, Unconventional SUSY and Graphene*, JHEP01(2020)084, arXiv:1910.03508]

In the AVZ model [P.D. Alvarez, M. Valenzuela, J. Zanelli, *Supersymmetry of a different kind*, JHEP 1204 (2012) 058, arXiv:1109.3944] **the fermionic gauge field ψ^A is a composite field, and the propagating fermion χ^A originates from the radial component of the gravitino through the Ansatz:** ($A=1, \dots, \mathcal{N}$, \mathcal{N} number of supersymmetries; $i=0, 1, 2$)



Massive Dirac Equation in the AVZ model

The AVZ model can be obtained at the D=2+1 AdS₃ boundary from a supergravity on a (curved) AdS₄ spacetime in D=3+1 through an ultraspinning limit.

From the **Maurer-Cartan equations** of the **supersymmetry algebra**

Massive Dirac equation

$$\mathcal{D}\chi = -\frac{3}{2}i\tau\chi$$

\mathcal{D} covariant derivative

mass $m = \frac{3}{2}\tau$ ← torsion

Killing spinor equation for the boundary supersymmetry

Solutions of the Dirac equation correspond to supersymmetries of the system.

Electronic properties of the pseudoparticles, such as e.g. optical conductivity, are determined by supersymmetry. We have **ongoing discussions with the condensed matter groups**, both theoretical and experimental, at the Politecnico di Torino.

Some Properties of the AVZ model

- There are no bosonic propagating degrees of freedom:

Number of bosons \neq Number of fermions

Unconventional Supersymmetry

- Supersymmetry is implemented purely as a gauge symmetry

- The **AVZ Ansatz** corresponds to an (unconventional) **gauge fixing of supersymmetry** in the framework of a **BRST quantization** [L. Andrianopoli, BLC, P.A. Grassi, M. Trigiante, *The Quantum Theory of Chern-Simons Supergravity*, JHEP 1906 (2019) 036, arXiv:1903.04431].

- The supersymmetry parameter ϵ_A is proportional to the propagating fermion:

$$\epsilon_A \propto (\bar{\chi}\chi) \chi_A$$

- **Mass is generated by the geometric properties of supergravity, such as torsion.**

Holography in the geometric framework

[L. Andrianopoli, BLC, R. Matrecano, O. Mišković, R. Noris, R. Olea, L. Ravera, M. Trigiante, work in progress]

- **We are explicitly computing the holographic map in a geometric formulation** [for a review on the geometric framework for supergravity, see R. D'Auria, *Geometric Supergravity*, hep-th/2005.13593, review article from the book "Tullio Regge: an Eclectic Genius"; World Scientific Publishing Co. Pte.Ltd].
- **The gauge/gravity (AdS/CFT) correspondence relates a conformal gauge theory on the boundary to a classical gravity theory on anti de Sitter spacetime in one dimension higher.** [J.M. Maldacena, *The Large N limit of superconformal field theories and supergravity*, ATMP 2 (1998) 231, hep-th/9711200]

Non-perturbative Strong-weak duality

- **At low energies it implies a one-to-one correspondence between quantum operators in the boundary conformal field theory and fields of the bulk supergravity, which act as sources for the gauge theory.**
- **The radial coordinate moving towards the bulk is related to the energy of the gauge theory** [A.W. Peet, J. Polchinski, *UV / IR relations in AdS dynamics*, Phys. Rev. D 59, 065011 (1999), hep-th/9809022].
- **The AVZ model should correspond to a topologically inequivalent sector from an unconventional gauge fixing of supersymmetry** [L. Andrianopoli, BLC, P.A. Grassi, M. Trigiante, arXiv:1903.04431].

Final remarks

- In the framework of holography, we have obtained a description of 2D graphene-like materials in a suitable AdS_3 patch at the boundary of an extended supergravity in one dimension higher with \mathcal{N} supersymmetries.
- This **top-down approach is more predictive** than the common bottom-up one, because it is strongly constrained from the supersymmetry of the gravity theory.
- The model features **supersymmetry**, and it can be viewed as a top-down approach to understand the origin of the observed supersymmetric phenomenology in graphene [S.-S. Lee, *Emergence of supersymmetry at a critical point of a lattice model*, Phys. Rev. B76 (2007) 075103, cond-mat/0611658].
- The Haldane and Semenoff-type **masses are identified with geometric properties** of the model, such as torsion.
- In collaboration with O.Miškovic and R.Olea, we are actually explicitly computing the **holographic map**, and we want to apply the **holographic renormalization** scheme to our AdS_4 /graphene correspondence. In this framework the counterterms in the holographic renormalization should sum up to topological invariants [R.Aros, M.Contreras, R.Olea, R.Troncoso, J.Zanelli, *Conserved charges for gravity with locally AdS asymptotics*, Phys.Rev.Lett. 84 (2000) 1647-1650, arXiv:gr-qc/9909015].

Thank you!

